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# SYMPOSIUM PROCEEDINGS

# THE INTERACTION OF **NON-NUCLEAR MUNITIONS** WITH STRUCTURES

U.S. AIR FORCE ACADEMY, COLORADO MAY 10-13, 1983

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## **SYMPOSIUM PROCEEDINGS**

# THE INTERACTION OF NON-NUCLEAR MUNITIONS WITH STRUCTURES

U.S. AIR FORCE ACADEMY, COLORADO MAY 10-13, 1983

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#### CADURD SHOCK PROM PENETRATING CONVENTIONAL VEAPORS

James I. Drake and Charles D. Little, Jr.

U. S. Army Pagineer Meterways Experiment Station Vickeburg, Missinglyi

#### ABITRACT

This paper presents results of an analysis of ground shock data from more than one hundred explosion tests conducted in sell over the past 35 years. Burst positions veried from fully buried to contact detonations in sell and for shallow depths into concrete protective everlays. Soil conditions ranged from losse dry sand to saturated clay. Espirical equations are presented that predict the magnitude and time histories of the expected streames and ground motions as a function of burst position, soil indices and burster layer chickness he

#### BACK/BOUND

Note than one hundred explosion tests have been performed over the part 35 years in soil to characterise the ground shock produced by buried conventional sumitions. Lampon (1) conducted pioneering tests during Moriel War II with buried charges in several soil types from which cube root scaling was developed and verified. Following Lampoon's lead, the MOLE and UET tests (7,3) were conducted in the early 1950's to extend the ground shock data base to other soils and rocks. Since that time many other buried burst tests have been conducted in a wide veriaty of soils with charges from 1 pound to 500 tons (4-21). Hency other small-scale tests have gone wereported.

Tests performed for special projects produced the first measurements of stresses directly besenth mear-surface explosions on burster slabs (12,13). Couoling of shellow explosions from penetrating weapons was investigated by Ingram (3) in the CENER program and by Brake and Little (unreported). Brown, et al (14), investigated the propagation of ground shock through rock rubble owariays. All totaled, more than 50 tests have been conducted just to determine explosive coupling from pertially buried weapons in burster minus.

Oround shock data from these tests were drawn together and analyse! to provide an update to the Army design manual, TH 5-855-1, "Pundamentals of Protective Design for Conventional Meapons." The result of that analysis is the basis for this paper. Due to the limited space provided, only the empirical prediction equations are given.

#### CHOUND SMOCK THREAT

The ground shock produced by bombs exploding on or within the ground mear buried structures generally provides the desinest threat to those facilities. Stresses from buried bursts can be greater in segmitude and much longer duration than corresponding bursts in air.

Significant enhancement of the streams and ground motions will occur as the weapon ponetrates more deeply into the surrounding soil or backfill before it Jamotates. Often, protective layers of concrete or rock rubble are provided over the structure to limit the weapon penetratine thus reducing the effective coupling of the explosion and increasing the weapon standoff.

Important variables affecting the intensity of the loading are: a) weapon size and distance to the structure, b) the wechanical properties of the soil or rock, and c) the depth of penetration of the weapon. Of these factors, the affect of soil or rock properties is least predictable by simple handbook methods. Ground shock intensity may very by more than two orders of magnitude when the soil is varied from low dessity dry soils to saturated clays.

There are two important cases to consider in assessing the ground shock threat to buried facilities: 1) bombs that emplode overhead, generally on or within the protective concrete or rock rubble overlay, causing a direct loading of the roof slab, and 2) weapons that peretrete into the surrounding soil and detonate beside the facility loading the walls and floor. While the same general ground shock prediction equations upply for both cases, the role of the site geology and the protective overlay requires a somewhat different application of these equations. These cases are shown in Figure 1.

#### SOIL PROPERTY EFFECTS

Ground chock propagation in carch media is a complex function of the dynamic constitutive properties of the soil, the emplosive products and the geometry of the explosion. Ho single soil index or combination of indices can elequately describe this process in a single way for all cases.

Meter can have a profound influence on ground shock propagation is cohesive soils, particularly

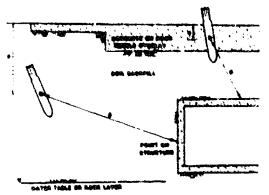


Figure 1. Germatry for emplosion against a buried facility

as saturation reaches 95 percent or greater. Typically water is fully bound with the sheletal structures for these soils, providing significant contribution to the overall stiffness and strength of the soil structure. As saturation approachs 100 percent, prosounced increases in peak atresses and accelerations have been observed in wet clays, clay shales and sendy clays. Stresses similar to shock wever in free water have been noted in esturated clays. Saturation as measured by free standing water in bireboles may not be an accurate measure of the true naturatice depth, particularly where seasonal water table fluctuations introduce small amounts of air into the soil. Seismic surveys generally will show a sharp jump in the wave speed to more than 3000 feet per second at this depth.

Granular soils with high relative descity are generally not strongly Lattuenced by water saturation as are conssive soils. The stiffaces of granular soil is provided by the grain to grain contacts in the skeleton with only a small contribution by the free water. Consequently, controlled laboratory and field experiments in denne meerly caturated cands did not show large influence of the pere water on the resulting shock wave propagation. Movever, the effects of water is les relative density eards can produce similar effects as those seem in cohesive soils (15). In these cases, the soil skeleton can collapse, and the grain to grain contact lost resulting in high pore pressures as the sand liquifies. These sites would not normally be considered for construction of herdened facilities.

Seismic velocity, c, is often used as a crude index of soil or rock properties for ground shock prediction purposes. It provides a simple measure of the stiffness and the density of the soil thru the relationship

c - 
$$\sqrt{\frac{M}{2}}$$

where H is the etiffness or modulus of the soil and p is its mass density. The seismic valocity also provides a relationship between distance and time.

A great deal of caution must be used in generalizing he use of seisoic velocity as a ground shock index. Commetative in granular soils much as dry deart alluvium say result in abnormally high propagation velocities (approaching 4000 feet per second). Yet these meterials may exhibit very high air filled voids and low relative densities—qualities that would classify them as very poor transmitters of ground shock. Low seismic velocities, on the other hand, would generally indicate poor ground shock transmission qualities.

The attenuation rate with range of the ground shock magnitude is nontrolled by the irreversible crushing of the wold volume within the soil matrin by the passage of the streak wave. In cohesive soils, the volume of the air filled wide in an index for attenuation of ground mutions, while the best index for attenuation rates in grounds madin is the relative density. Because relative density is not alway available, dry unit weight can be an effective intex for ground which attenuation. Soils with high relative density (high dry innerty) or low air voids will attenuate the ground shock more slowly than low relative density or high air void materials. Pigure I shows the peak atreas from amplosions in typical soils.

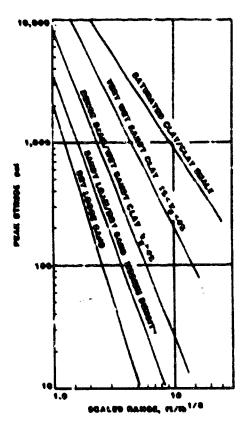


Figure 2. Peak stress from explosions is verying soil types

#### GROUND SINCE PREDICTIONS

Strang and particle velocity pulse: in he characterized by exponential like time histories that decay rapidly in explitude and breaden as they propagate outward from the explosion. The characteristic time for twee time histories can be measured in arrival time from the low ce, t<sub>g</sub>, where

$$t_{\frac{1}{6}} = \frac{h}{c} \tag{1}$$

R is the distance from the explosion and  $\varepsilon$  , the season or propagation velocity. Industry these wave forms rise charply to the plak with the rise time,  $\varepsilon_p$ 

$$t_{T} = 0.1 t_{A}$$
 (2)

this is about 1/10 of the travel time to the target int. From the peak, the pulse decays monoston, ally with time to meanly zero in  $t \in \mathbb{N}$  time; times given by the following exactions

$$V(t) = V_{\alpha}(1 - \alpha t/t_{\alpha}) = - \delta t/t_{\alpha} \qquad t > 0 \quad (16)$$

where P(t) is the atress. V is the particle velocity, and a and c ere time constince. While the time constants generally vary with specific site conditions, they can be laint to

$$y = 1,0 \qquad \qquad x = \frac{1}{2\sqrt{5}}$$

for most applications.  $P_{\rm O}$  and  $V_{\rm O}$  are values of the peak stress and particle velocity to be determined by the following equations. Other waveform persmeters such as impulse, displacement and accelerations may be derived from these functions.

Since the characteristic time is inversely presentional to seismic velocity, explusions in high velocity media such as saturated clay will pre luce very short, high frequency pulses with high eccelerations and low displacements. On the using hand, detonations in dry locas materials will cause much longer duration, low frequency ground motions.

Peak particle velocity and peak atrees are related by

$$P_{c} = cc V_{c}$$
 (4)

whate o is the mass density. Free-field strusses and ground motions from bombs detonating on and within burster layers or in the soil along side the structure are given in the following expressions:

$$-\Gamma_{Q} = 1 + (1/2) + 160 + \left(\frac{1}{M}/2\right)^{-1} \qquad (5.5)$$

$$|\gamma_{n}| = (1 + 180) \cdot \left(\frac{\kappa}{\omega^{1/2}}\right)^{-n}, \qquad (3)$$

$$\omega_{ij} + \mathbf{w}^{2/3} + (t + 50 + c) + \left(\frac{\mathbf{w}}{\mathbf{w}^{1/3}}\right)^{-n-2}$$
 (5c)

$$\frac{d}{\sqrt{1/3}} + t = 500 \cdot \left( \left( \frac{R}{\sqrt{1/3}} \right) \right)^{-0.64} \tag{5.3}$$

$$\frac{1}{\sqrt{V^*}} + f + \dots + 1.1 + \left(\frac{1}{\sqrt{1/2}}\right)^{-n+1} \qquad \text{(Se)}$$

where  $T_0$  is the peak pressure (psi),  $V_0$  is the peak particle rejective (frise),  $A_0$  is the peak acceleration (g's),  $A_0$  is the peak displacement (ft),  $I_0$  is the peak impulse (psi-sec),  $I_0$  is the mass lensity lib-sec (ft),  $I_0$  is the seismit velocity (ft, sec),  $I_0$  is the acoustic impedance (psi/t/sec),  $I_0$  is the distance to the explosion (it),  $I_0$  is the charge weight (lb), and it she coupling factor for near surface detonations. For preliminary design considerations the following table is suggested for solvecting the seismic relocity, acquetic impedance and attenuation coefficients:

#### SING ASTED CHEFFECTENTS IN R. DESCON

Microcky) Description	Nelsonic Nelsonity		Attentiati n Cifficaci
louse, dry sands and gravels with low solutive Jennits	600	;;	1.1.28
Sandy loam, leess, dry mands and backfili	1000	.;	2.18
Penso sand, with high relative density	1600	44	2.5
het man'y clay with air wells (greater than 4 wreent)	1800	••	2.5
Saturated sandy clays such sands with small amount of air voids (less than a percent)	1060	••	4.28-2.8 j
Meavy saturated clays and clay shales	1000	150-180	1.5

A more detailed description is provided in Table 1 for soils encountered in explusion test programs. Simple soil parameters such as wet and dry unit weights, air filled would and seismic velocity are shown to assist 'r relating the explusion effects parameters to the design soil conditions. Note that the attenuation coefficient and seismic velocity are closely related to dry unit weight for granular soils while air void content is important for cohesive soils.

#### GROUND SHOCK COUPLING FACTOR

The magnitude of the stress and ground motions will be greatly enhanced as the weapon panetrates more deeply into the suil or the protective burster layer pefore it detonates. A concept of an equivalent effect coupling factor is introduced to account for this effect on the ground shock parameters and is defined as follows:

The coupling factor, f, is defined as the ratio of the ground shock magnitude from partially to shallow buried weapon to the ground shock magnitude from a fully buried burst in the same medium.

A single coupling factor is applicable for all ground shock parameters that depends upon the depth of burial of the center of the weapon and the medium being penetrated, i.e., soil, concrete or air. It is important to note that the coupling

factor concept used here does not produce an equivalent charge but rather, it is a scale factor to reduce the ground shock computed from a buried burst with the full charge weight to account for the shallow buriel.

Coupling factors are different for bursts in air, soil and concrete and depend upon the scaled depth of burst of the weapon. These factors are shown in Figure 3. The coupling factor for air is a constant

$$f = 0.14$$

and is recommended for contact bursts.

In the case where a weapon penetrates into more than one material, i.e., a long bomb that penetrates the concrete slab and is partly buried in soil, the coupling factor is computed as the sum of the coupling factors in each of the materials weighted in proportion to the charge weight contained within each medium.

$$f = \sum f_1(\frac{w_1}{w})$$
 (6)

where f is the total coupling factor,  $f_4$  is the coupling factor for each component material, i.e.,

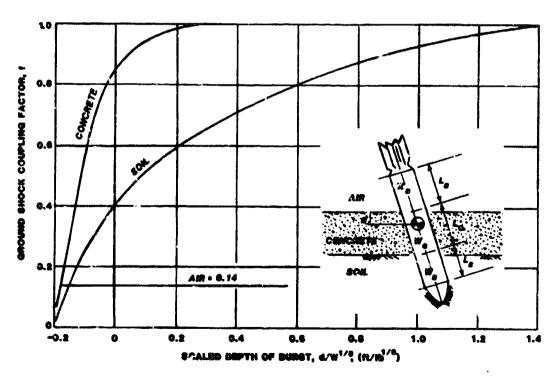


Figure 3. Ground shock coupling factor as a function of scaled depth of burst for air, soil and concrete

air, soil, concrete,  $W_1$  is the weight of the charge in contact with each component material, and W is the total charge weight. Since most bombs are cylindrical, the coupling can also be defined as

$$f = \sum_{i} f_{i} \left( \frac{L_{i}}{L} \right) \tag{7}$$

where  $L_{\rm t}$  is the length of the weapon in contact with each material and L is the total weapon length.

#### DISCUSSION AND CONCLUSIONS

Empirical expressions were derived from a fit to a large body of ground shock data from buried and near-sur ace bursts in soil. Several important observations were made concerning the role of soil properties on scaling of ground shock:

- 1. Near the explosive source, peak particle velocities in soils tend to a single curve that is nearly independent of the soil properties. This observation can be explained in part by the interaction of the detonation wave in the explosive with the soil.
- 2. Peak stresses scale in proportion to the seismic velocity.
- 3. Attenuation of the peak ground shock magnitudes is strongly dependent on the relative dansity in granular soils or to the air void volume in cohesive soils. Because the seismic velocity is also influenced by these parameters, the attenuation coefficient, n, can be estimated from the saismic velocity as

c(fpa)	<u> </u>
500-600	3-3.5
750-1000	3
1000-1400	2.75
1400-1600	2.5
>5000	1.5-2.25

- 4. Time scales in proportion to the time of arrival. Thus, the pulse tends to spread in proportion to the distance traveled, with a rise time of about 1/10 of the travel time and a duration on the order of 2-3 travel times.
- 5. Because of the time scaling, peak accelerations are proportional to the seismic velocity, peak displacements are inversely proportional to the seismic velocity while the peak impulse is only sensitive to density variation.

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TABLE 1 SOIL PROPERTIES FROM EXPLOSION TESTS

Soil Description	Dry Unit Weight Ydry 1b/ft <sup>3</sup>	Total Unit Weight  7 1b/ft3	Air-Filled Voids	Seismic Velocity C ft/sec	Acoustic Impedance pc psi/ft/sec	Attenuation Coefficient
Dry desert alluvium and plays, partially comented	87	93–100	>25	2100-4200 (1)	40	3-3.25
Loose, dry, poorly graded sand	80	90	>30	600	11.6	3-3.5
Loose wet poorly graded sand- free standing water	97	116	10	500-600	12.5-15	3
Dense dry sand, poorly graded	99	104	32	900-1300	25	2.5-2.75
Dense wet sand, poorly graded- free standing water	108	124	9	1000	22	2.75
Very dense dry sand, relative density "100%	105	109	30	1600	44	2.5
Silty-clay, wet	95-100	120-125	9	700-900	18-25	2.75~3
Moist losss, clayey sand	100	122	5-10	1000	28	2.75-3
Wet sandy clay, above water table	95	120-125	4	1800	48	2.5
'Saturated' sand-below water table in marsh			1-4(2)	4900	125	2,25-2.5
'Saturated' sandy clay, below water table	78-100	110-124	1-2	5000-6000	130	2-2.5*
'Saturated' sandy clay, below water table	100	125	<1	5000-6600 .	130-180	1.5
Saturated stiff clay saturated clay-shale		120-130	0	>5000	135	1.5

<sup>(1)</sup> High because of camentation.
(2) Estimated.

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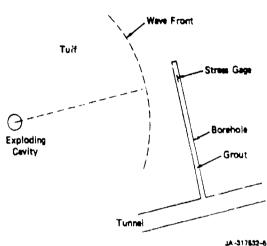
CALCULATIONAL EVALUATION OF THE INCLUSION EFFECTS ON STRESS GAGE MEASUREMENTS IN ROCK AND SOIL

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#### ABSTRACT

rplosion-induced stress waves in rocks and so is are frequently measured by flatpack stress gages grouted in boreholes. The stress gage measurements differ from the free-field stresses if the grout forms on inclusion because of a mismatch of material properties or inadequate bonding with the medium. Calculational results are presented for a tuff medium to illustrate inclusion effects in elastic and elastic-plastic regimes. The main effect occurs if the inclusion-medium bonding is inadequate.



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#### INTRODUCTION

Experiments for investigating the vulnerability of military civil engineering attructures to attack loads applied through the ground involve measuring stresses in rock and soil. Stress gage signals are often difficult to interpret because the gages and the immediate surroundings disturbed by gage installation perturb the free-field stresses to be measured.

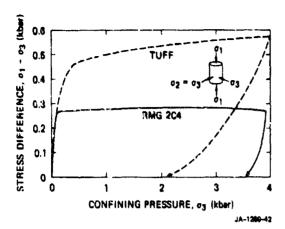
This paper treats the influence of the gage installation procedure on the free-field stresses. For installation in rock, the procedure is to drill from a tunnal, cavity, or ground surface, insert. the gage, and pack the borehole with Lock-matching grout, as illustrated in Figure 1. Because it is impossible to match all the properties of the rock in the neighborhood of the gage and to ensure perfact bonding with the rock, the grout-filled borehole forms a cylindrical inclusion, so the gage is in general not subjected to the same stresses at the far field. To interpret these stress gage signals, one must determine the relationship between the inclusion and medium stress fields. The influence on the stresses of the gage, which is itself an inclusion, is not treated here; that investigation will be the subject of a future publication.

The calculational investigation is simplified by assuming plane strain conditions, by confining attention to the two extreme cases of perfect bonding (no slip) and no bonding (no shear transfer), between the grout and the rock, and by considering proportional static compressional loading, thich prevents bond separation. Illustrative results based on a rock-matching grout (designated 2C4) inclusion in Nevada Test Site (NTS) tuff are presented.

FIGURE 1 IN-SITU STRESS GAGE EMPLACEMENT

#### NATERIAL HODEL

To show how a gage installation procedure can make stress measurement difficult, calculations are performed for a borehole in MTS tuft filled with 2CA grout, as shown in Figure 1. Figures 2 and 3 show the tuff and grout strength properties. A strong tuff is intentionally chosen to magnify the affects of poorly matched properties. Both the grout and the tuff are modeled as Mohr-Coulomb material with the properties listed in Table 1.



F:GURE 2 UNIAXIAL STRAIN RESPONSE OF ROCK-MATCHING GROUT RMG 2C4 AND NEVADA YEST SITE TUFF: STRESS DIFFERENCE VERSUS CONFINING PRESSURE

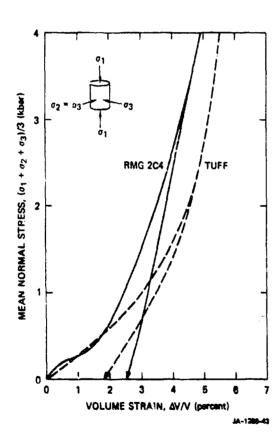


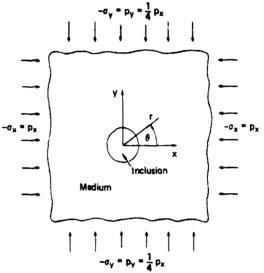
FIGURE 3 UNIAXIAL STRAIN RESPONSE OF ROCK-MATCHING
GROUT RMG 2C4 AND NEVADA TEST SITE TUFF:
MEAN NORMAL STRESS VERSUS VOLUME STRAIN

Toda I
MATERIAL PROPERTIES

Materia)	Young's Modelus (jei)	Poleson's Ratio	Friction Angle  # (deg.)	Cohesion c (psi)	.48; 8m; <sup>(f</sup>
TMT	1.66 x 10 <sup>6</sup>	0.32	6.36	2.85 x 10 <sup>3</sup>	<b>-</b> j
Grout (204)	2.64 x 10 <sup>6</sup>	0.28	1.46	1.91 x 10 <sup>3</sup>	;

#### FINITE ELECENT MODEL

The spherical wave engulfing the borehole and gage is approximated by a quasi-static biaxial stress-plane strein state, as shown in Figure 4.



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FIGURE 4 CIRCULAR INCLUSION UNDER BIAXIAL STRESS AND PLANE STRAIN

For pulses with rise times longer than several inclusion dismeter transit times and where densities of different materials match each other, a quasistatic analyses gives reasonable estimates of the dynamic response. As a further simplification, proportional loading is assumed. The ratio between free-field stresses is chosen as  $\sigma_\chi/\sigma_\psi=4$  to avoid creating tensile stresses across the inclusionmedium interface. Figure 5 shows the two gage locations for measuring the free-field stress components  $\sigma_X=-p$  and  $\sigma_y=-p/4$  (p >0). Because of symmetry, only the first quadrant needs to be modelled. Stresses  $\sigma_\chi$  and  $\sigma_y$  are calculated in the inclusion along the radii on the y and x axes, respectively. The inclusion effect of the gage itself is not considered and these calculated stresses are taken to be the stresses acting on the gage for comparison with the uniform free-field stress.

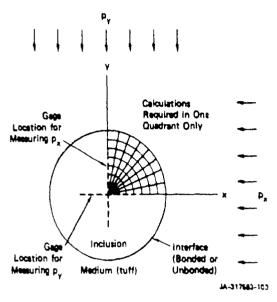


FIGURE 5 GAGE LOCATIONS IN BOREHOLE

The analysis was performed with the finite element code NONSAP. The finite element grid extended to 10 times the radius of the inclusion, as shown in Figure 6. Four node plane-strain quadrilateral elements were used.

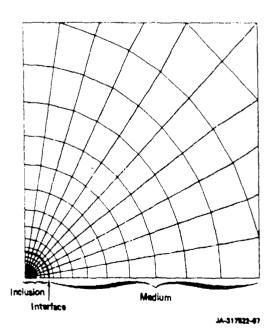


FIGURE 6 FINITE ELEMENT GRID

#### INTERPACE MODEL

Two inclusion-medium interface conditions are investigated. These conditions are perfectly bonded and free-sliding, and they provide bounds on the real sciution behavior. The bonded interface cransfers both compressive and shearing loads. The free-sliding interface transfers compressive loads only.

The perfectly bonded interface requires no special modeling technique because the usual finite element node-element connectivity describes this condition.

The freu-sliding interface is modeled by a thin ring of two-dimensional Mohr-Coulomb quadrilateral elements to transfer compressive load. The elements are weak in shear to eliminate transfer of shearing atress. The thickness of the ring is 5% of the inclusion radius. Young's wodulus and Poisson's ratio of the ring material are the same as the averages of the surrounding material. Humerical tests indicate that cohesion and friction angle values of 10 psi and 0.1° are satisfactory for the tuff-2C4 grout combinations.

#### NUMERICAL RESULTS

Stress distributions along the gage locations for three cases of an inclusion in tuff are calculated. They are

- 1) a perfectly bonded grout inclusion,
- 2) a perfectly unbonded tuff inclusion, and
- a perfectly unbonded grout inclusion.

The first case inlustrates the effect of mismatched material properties; the second case illustrates the effect of an unbonded interface and the third case combines both effects.

In each case, calculations were made for three or four free-field stress levels, the lowest value in each case providing an entirely elastic response.

Shows uniform stress distributions along the x and y axes of the grout inclusion for free-field compressive stress of  $p_X=4$ , 5, and 6 ksi, with  $p_Y=p_X/4$ . The calculated stresses at the gage locations are  $\sigma_X$  and  $\sigma_Y$ . A gage located on the y axis would measure the x component of free-field stress exactly if  $\sigma_X/p_X=-1$ . When  $p_X=4$  ksi, this ratio is  $\sigma_X/p_X=-1.11$ , so the gage would read 11% high. As  $p_X$  is increased, the readings become more accurate. A gage located on the x axis would measure the y component of free-field stress exactly if  $\sigma_Y/p_Y=-1$ . When  $p_X=4$  ksi, this ratio is  $\sigma_Y/p_X=-0.94$ , so the gage would read 6% low. When  $p_X=5$  ksi, the gage would read 9% high and when  $p_X=6$  ksi, the gage would read 9% high and when  $p_X=6$  ksi, the gage would read 9% high and when  $p_X=6$  ksi, the gage would read 9% high and when  $p_X=6$  ksi, the gage would read 9% high and when  $p_X=6$  ksi, the gage would read 9% high and when  $p_X=6$  ksi, the gage would read 16% high. The stress ratio trend is to increase further because the stress components are confined to the yield surface. The mismatch of properties in this example allows a reasonably accurate measurement of  $p_Y$ , the larger component of free-field stress. The mass is true for measurement of

the enalter component under elastic or reall plantic deformations. As the leading increases to produce larger plantic deformations, measurement of  $p_y$  becomes increasingly inaccurate.

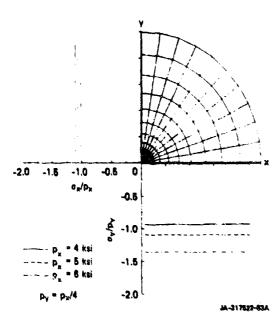


FIGURE 7 GAGE STRESS FOR GROUT INCLUSION WITH BONDED INTERFACE, EXAMPLE 1

case 2. Unbonied Tuff Inclusion. Figure 8 shows the stress distributions along the x and y axes of an unbonded tuff inclusion for free-field compressive stresses of  $p_X=5$ , 7, and 8 ksi, with  $p_Y=p_X/4$ . A gage located on the x or y exis would measure the free-field stresses exactly if  $\sigma_y/p_X$  and  $\sigma_X/p_X$  are unity. The effect of an inclusion/ medium interface that does not transfer shear stress is to produce momuniform stress distributions. When  $p_X=5$  ksi the tuff response is elastic and the stress distributions shown (full lines) are parabolic. At the center of the inclusion, the x and y stress components are 15% higher and 61% lower, respectively, than their free-field counterparts. Increasing the free-field loweding enough to cause yielding in the inclusion flattens the stress distribution at the center. Approximate measurement of the larger free-field stress,  $p_X$ , is possible if the gage does not occupy too much of the inclusion diameter. Heaverment of the smaller free-field stress,  $p_Y$ , on only be regarded as a rough estimate, the value of which depends on the stress level.

Case 3. Unbonded Grout Inclusion. Figure 9 shows the stress distribution along the x and y axes of an unbonded grout inclusion for far-field compressive atreases of  $p_X=1-1/2$ , 4, 5, and 6 ket, with  $p_y=p_X/4$ . This combines the effects of the mismatching of properties of the first case and the lack of bonding of the second case. The main conclusion is that the bonding effect dominates so, as

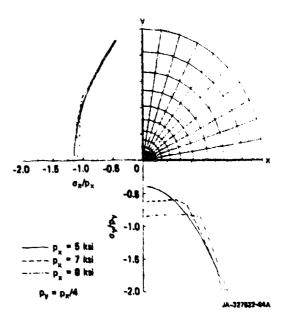


FIGURE 8 GAGE STRESS FOR TUFF INCLUSION WITH SLIP

case 2, approximate measurement of the larger free-field stress  $\mathbf{p}_{\mathbf{x}}$  is possible but measurement of the smaller free-field stress is not.

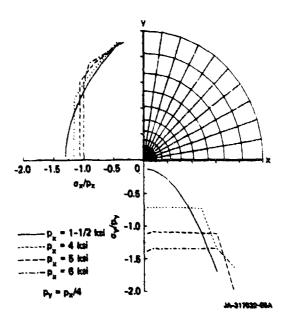


FIGURE 9 GAGE STRESS FOR GROUT INCLUSION WITH SLIP INTERFACE, EXAMPLE 3

#### CONCLUSION

Based on the numerical examples treating a grout inclusion in MTS tuff, we conclude that:

- A nimeatch of the inclusion and medium properties rotains a uniform stress distribution along the gags locations. As loading increases the measurement of the larger free-field stress becomes more accurate while the measurement of the smaller free-field stress becomes less accurate. This occurs because the smaller stress component in the grout becomes relayed to the larger stress component through the yield condition.
- Lack of interface bonding produces non-uniform stress distributions along the stress gage location. As increased loading causes increased plastic flow in the inclusion the stress distributions become more uniform in such a way that the larger free-field stress is measurable but the smaller free-field stress is measurable but the smaller acress component in the grout becomes related to the larger stress component through the yield condition.





# FREE-FIELD CHOURD SHOCK PRESSURSS FROM BURIED DETORATIONS IN SATURATED AND UNSATURATED SOILS

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#### ABSTRACT

Free-field ground shock pressures at verious distances from the buried detonation of high-emplosive charges, morter and artillery rounds, and large bombs have been measured by Southwest Research Institute and independently by Waterways Experiment Station personnel. This paper presents an empirical solution capable of predicting these pressures in unsacurated soils. In saturaced soils, a very different energy dissipation process occurs which is predicted by modifying a hydrodynamic solution, and comparing it to tests on bombs in saturated soils.

#### INTRODUCTION

We have been developing a general solution for predicting ground shock pressures and impulses imported to shelters from the detonation of buried ordnance. Unfortunately, all the results cannot be shown in this short paper; however, one aspect, free-field ground shock pressures, will be presented in detail. Those wishing additional details can refer to reference [1].

Our solution was developed using modeling techniques and test results from a large compilution of ground shock pressure data. Under most conditions, a log-linear curve fit can be used to predict pressures over four orders of magnitude in value. The exception to the general solution arises when soils are saturated. Then, a modified hydrodynamic solution works. In this paper, we will present the general solution, compare results to measured pressures, show that problems can arise and derive the modified hydrodynamic solution.

#### GENERAL SOLUTION

An empirical equation for predicting freefield ground shock pressure from the detonation of buried explosive is given by:

$$\frac{\left(\frac{P}{\rho c^{2}}\right)}{(4.35+\frac{7}{4})\left[0.25+0.75 \cosh \left(0.45\frac{\rho^{1/3}c^{2/3}d}{V^{1/3}}\right)\right]^{3}}$$

$$0.0175 \left(\frac{V^{1/3}}{\rho^{1/3}c^{2/3}R_{eff}}\right)^{3.42}$$
(1)

where P = maximum pressure (F/L<sup>2</sup>)

p mass density of soil (FT2/L4)

c - wpeed of sound in soil (L/T)

d = depth of orderace buried to its C.G. (L)

Y - depth of point below C.G. of ordnence
(L)

W - energy release of explosive (PL)

R<sub>eff</sub> = effective elemt range which accounts for ordesmoe geometry and orientation (L).

All ratios in Equation (1) are nondimensional which means that predictions can be made using ear self-consistent set of metric or English units. The quantity Reff accounts for bomb length 1 and orientation 0. This quantity Reff is a first approximation to where an equivalent point source of the same searcy release should be located so that the same scaled energy W/pc<sup>22</sup> occurs for the distributed energy in a line source of finite length as in the equivalent point source. Reff is given by:

$$\frac{B_{\alpha,f,f}}{L} = \left[ \frac{H - H^2 - \frac{1}{4}}{\frac{H+C,5}{(M+H)^{\frac{1}{2}}} - \frac{H-O,5}{(M-H)^{\frac{1}{2}}}} \right]^{\frac{1}{3}}$$
(2)

where  $H = (R/L)^2 + (R/L)^2 + (Y/L)^2 + 1/4$ 

 $H = (Y/k)\cos \theta + (E/k)\sin \theta$ 

and I = horisontal distance of location in vertical plane through the bomb (L)

X = transverse distance of location (L)

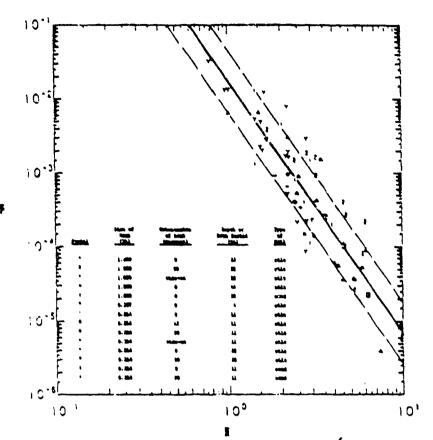
t - length of explosive source (L)

0 = bomb's orientation (0=0 degrees is a vertical bomb).

#### COMPARISON WITH DATA

Equation (1) has a format permitting scaled pressure on the left-head side of the equation to be plotted versus a scaled effective standoff distance on the right-head side. Hamy different symbols are seen in Figure 1 because there were many variations in size of emplosive energy release (1.8, 0.327, and 0.216 1b sources), orientation of the charge (0, 90, and 45 degrees), depth of burial

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Pigure 1. Scaled Pressure Versus Distance in Sukl Tests

of the charge  $(\ell_1, 21)$ , and 22 inches) dupth of burial of transduces, and type of soil (silt and sund). All tests were performed outdoors with a natural variation in soil conditions recorded by measuring soil density  $\rho$  and velocity  $\epsilon$  diving each test.

The solid l'es through the pressure data is Equation (1). The dashed 10 a to each side of the prediction line is a statistical one sigms standard deviation for a normal distribution in log of pressure abo t the prediction line. Although this scatter may appear to be large, it is of the same magnitude for results from other experiments.

Personnel at Unterways Experiment Station [2] have been conducting tests in which free-field ground shock presents were nemitered at various sites around buried C-4 c/arges, mertar shells, howitzer rounds, and bombs. In Figure 2 our solution and its scatter is shown so it can be compared to ground shock pressures for 135-um howitzer shells containing 15.6 lb of TMT, 105-um howitzer shells containing 4.8 lb of Comp-8, and 4.2-inch mertar shells with 7.8 lb of TMT fired at White Sands Missile Emage.

A first converient conducted at White Sands by WES personnel involved 16, 5, and 8-16 explosive C-4 charges. These scaled pressures are compared to Equation (1) in Figure 3. Secause the results seen in Figures 2 and 3 are similar to those seen in Figure 1, the same comments about accuracy and scatter apply.

#### HTDROOTHANIC SOLUTION

At another test site, Fort Knox, Esstucky, MES personnel conductor' ground shock pressure measurements using live MK-82 (500-lib) and MK-84 (2000-lib) bonks. These bonks contain, respectively, 191 lb and 945 lb of tritonal. Heasured pressures were all higher than expected as can be seen by looking at the results in Figure 4. A recron does exist for these pressures being higher than expected, but to understand, we must discuss Fort Knox field conditions.

The soil at Fort Enox is a 10 foot upper layer of soft brown clay overlying a soft clay mined with gravel. The density of both layers is the same average wat density of 125 lb/ft<sup>3</sup> and water content of 22.5 percent. The sajor difference between the layers is that the upper layer has a P-wave velocity of 1200 ft/sec; whereas, the lower layer has a

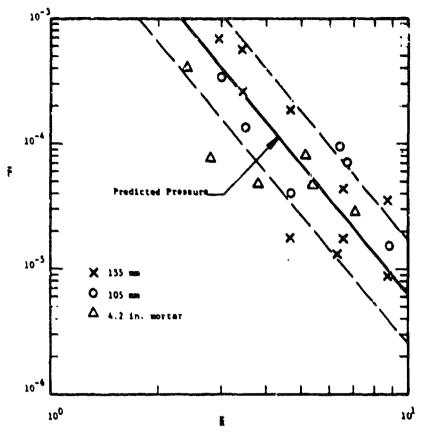


Figure 2. Comparison of Proc-Field Francers Solution to Toot Secults with 155-on Artillery Shells

velocity of 4800 ft/sec. Both soils are essentially saturated with the ground water table at the 10-foot depth separating those liyers. The upper layer is esturated by capillary action. The change in seismic velocity from 1200 to 4800 ft/sec descentrates the existence of the ground water table at the 10-foot depth, because 4800 ft/sec is the speed of sound in water.

All other test sites were such drier than Fort know. Moisture contests did reach 12 percent, but these are low relative to 22.5 percent. When the pores of a soil are filled with water rather than air, an almost incompressible pore fluid exists. Energy dissipation associated with collapse of the pores and shearing of soil grains over each other is not as great, and pressures are, therefore, higher at various standoff distances.

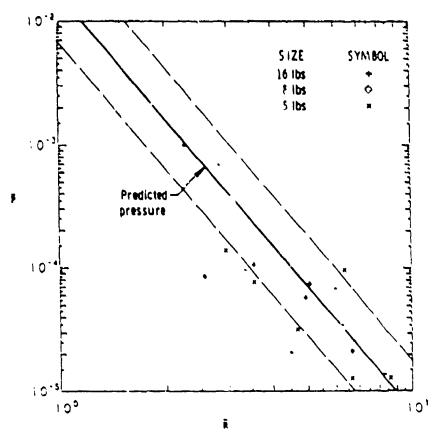
Instead of using a soil solution, the propagation of shock through saturated soils can be approximated by modifying a solution for shocks in unter. In his book on underwater explosions, Cole [3] presents that data which can be curve-fitted using a log-linear approximation to give an equation for shock pressures in water.

$$P(po1) = 24,650 \left[ \frac{y^{1/3}(1b \text{ TST})^{1/3}}{k(2t)} \right]^{1.16}$$
 (3)

By inserting the invarient  $\rho$  and c into Cole's dissessional equation, converting Equation (3) to a self-consistent set of dissessionless write, assuming the:  $\frac{\rho 1/3c^2/3d}{\mu^2/3}$  is large, and that the pressure gauge and bomb are at the same depth, Equation (3) can be rewritten as:

$$\left[\frac{P}{4.350c^2}\right] = 0.04224 \left[\frac{\rho^{1/3}c^{2/3}R}{V^{1/3}}\right]^{-1.16} \tag{6}$$

Equation (4) is the hydrodynamic equation which is shown in Figure 4 and compared to the unseturated sail selution and test data on MK-82 and MK-84 bombs. As can be seen, the hydrodynamic solution works such better and predicts such higher scaled presoures. The Fort East test site with its high ground water table behaves like a liquid. That is to say, provided one unouses that the bombs are in a special "heavy water" with a weight density of 12 lb/ft" cad water that propagates shocks at the measured P-wave velocity, either 1200 ft/sec for shallow burials above 10 feet or 4800 ft/sec



Pigure 3. Pressure Versus Distance for WES C-4 Charges

below the ground water table, energy is not dissipated as rapidly in saturated soils, and test results appear to be predicted by this modified hydrodynamic solution.

Obviously some transition regime must exist between the soil and water solutions. Although the data to demonstrate when and how a transition occurs are unavailable for degrees of saturation equal to or less then 50 or 60 percent, the soil solution is recommended. Further study is required to understand and separate these two colutions.

#### CONCLUBIONS

This paper only presents the results from one small segment of a large report containing information on free-field, oblique, and normally reflected ground shock pressures. In this report, impulse as well as presented are studied and details are presented on how predictive equations and the Reff concept are derived and that results measured.

In this particular discussion, we showed that free-field ground shock pressures dissipate in very different unnears dependent upon whether soils are seturated or unsaturated. Espirical equations are presented which allow free-field pressures to be predicted or various standoff distances in

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saturated and unsaturated soils. Test data from a variety of buried ordnance detonations are presented in dimensionless format to demonstrate the validity of these solutions.

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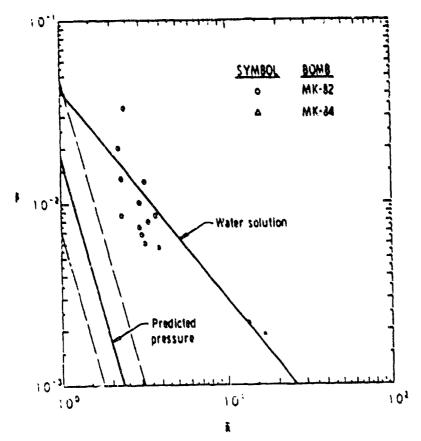


Figure 4. Pressure Versus Distance in Saturated Fort Esca Soils

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HIGH VELOCITY PENETRATION INTO FINE-REINFORCED CONCRETE MATERIALS - PROTECTION OF BUILDINGS

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#### AMETRACT

Fibre reinforced concrete suitable for apraying onto existing structures is being examined to assess its resistance to penetration by 7.62mm diameter armour piercing projectiles. A major test programme is being carried out to examine the .. fluence of aggregate type and fibre type. For - ch addregate/fibre c mbinetion a statistical rethod is being used to plan test series which will read to optimization of the concrete in terms of -ater/coment ratio, fibre content and aggregate/ went ratio. The minimum thickness of optimized concretes to resist penetration by the projectile and minimise spell and scabbing, will be determined The mechanics of the impact and penetration event are being studied and a possible method of deflecting the projectile within the concrete is suggested.

#### INTRODUCTION

During the course of its usefu' life, a structure, particularly a military one, may be subjected to attack from small arms fire, or perhaps indirect impact from close-proximity explosions. Hence, high-risk structures chould be constructed from impact resistant materials, and the capability to rapidly upgrade the protection afforded by an existing structure would be advantagrous. Any such impact resistant material must be able to contain several different facets of the impact event. It must be able to resist perforation from the projectile, it must be of sufficient thickness to resist tensile scalbing from the back face and it must also be cohesive enough to prevent spalling material flying from the front face, both because this material may be dangerous in itself and also because it leads to a local weakening which may then be breached by repeated impact.

Concrete has a resonable resistance to projectile penetration, due to its relatively homogeneous and massive properties. So far as the front and rear face damage is concerned, however, the low tansile strength of an ordinary concrete matrix ensures that a large amount of material is ejected from the slab faces with a velocity high enough to be potentially dangerous. Incorporation of fibres into the concrete matrix has been shown to considerably reduce the scabbing and spalling

essociated with dynemic loading of concrete (1, 2). In general, fibres act to increase the toughness of the cumposite meterial by improving the tensile properties of noisel concrete, absorbing the stress have energy by either pulling out of the matrix or perhaps by necking and breaking, depending upon the characteristics of the particular fibre.

Many different types of fibre are available commercially, the properties of the fibre reinforced concrete being dependent not only on the standard concrete variables such as aggregate size and type, aggregate/cement ratio and water/cement ratio, but also on the type, aspect ratio and proportion of the included fibres. A comprehensive testing programme is being carried out to study the effects of these variables and to optimize the fibre reinforced concrete to minimize prestration by 7.62mm MATO armour piercing bullets impecting at approximately 800 m/s. Attempts are being made to examine the mechanics of impact and penetration, so as to understand the failure modes of the fibre Teinfolded concrete under dynamic loading.

#### VARIABLES CONSIDERED

In order to fully utilise the adaptability of the optimum material, it was felt that a concrete suitable for sprayed application should be developed, since this would be equally useful for new construction and also for quickly reinforcing existing structures.

#### Aggregates

The ensure easy application by either the 'wet' or 'dry' spraying process, and to allow a reasonable fibre distribution through the matrix a Concrete Society (3) recommendation of a maximum aggregate size of 10mm has been adopted.

Tests on rock aggregate/elastomer composites subjected to impact by projectiles similar to those used in this study, showed that resistance to penetration was a function of the rock aggregate hardenes (4). In order to examine the effect of aggregate hardness on the penetration resistance of fibre reinforced concrete, crushed baselt (relatively hard) and crushed limestone (relatively work) were chosen as eggregates. The shape of the aggregate particles has an effect on the concrete bond also, and thus on the homogeneity of the

composite. Since the crushed rock aggregates are both angular in shape, a rounded river gravel in included in the study to give a comparison.
Aggregate/cement ratios vary from 1:3.0 to 1:5.0 in the statistically based test plans.

#### Fibres

Since it is impractical to include all the consercially available fibre types in an experimental series, various constraints had to be used to select the materials to be tested. On grounds of health and/or durability, vegetable, ambestos and class fibre materials were rejected, whilst carbon fibre was rejected because it was considered that the likely high fibre content required for the intended purpose would render the unit cost of the fibrous composite too high to be viable. Finally three types of steel fibre, one type of polypropylene fibre and two lengths of the organic polyamide fibre, KEVLAR 29, were chosen for detailed examination. Where appropriate, a length: diameter ratio of 100 was selected to give a composite which could reasonably be mixed in both a field and laboratory situation.

#### Cement Matrix

In order to ensure that the optimum fibra reinforced concrete can have univarial application, Ordinary Portland Cement is being used and it was initially assumed that the type of fine aggregate used would be unimportant. A range of water/cement ratios between 0.35 to 0.50 by weight is recommended by the Concrete Society (3), for ordinary sprayed concrete. However, due to the apparent docrease in workability caused by the inclusion of large volumes of reinforcing fibra, a range between 0.35 to 0.70 was selected for the main statistical series.

#### OPTIMIZATION OF THE VARIABLES

For each combination of fibre type (mix varieties) and aggregate type (three varieties) it is necessary to optimize the water/cement ratio. aggregate/cement ratio and fibre content. To give a reasonable range of these last three variables it was decided that specimens should be prepared with five levels of each variable. This gives 53 (=125) possible combinations for each particular fibre and aggregate. Since it would be unacceptable to test all of these combinations (a total of 2,250 tests) a statistical method known as surface response theory has been used to plan a programme. Details of this method have been given by Cochran and Cox (5). For each of the eighteen fibre/aggregate combinations a rotatable design utilising 14 extreme combinations and 6 m. 1 combinations of the mix \_\_sign parameters is used to indicate the combination of mix design parameters which will be most effective in "fucing projectile penetration. The response surfac. derived from the actual test results may tot indicate an optimus mix within its (star-shaped) boundaries. Thus the optimum mix design may be indicated as not part of the actually tasted range. In this case a "corner filling" technique

as described by Anderson et al (4) may be used to identify and check the optimus mix.

#### SPECIMEN PREPARATION

In a full scale structure, the fibre-reinforced concrete would be applied over a large area, hence it was conisdered vital that local and global effects were separated in the laboratory tests, only local effects being considered important. For this reason slabs of various plandimensions were tested, using a typical steel fibre reinforced concrete mix to determine the minimum target area required to ensure that gross cracking did not occur in most cases. In conjunction with these tests, slabs of various thicknesses were tested in order to obtain a value at which perforation was unlikely to occur in most cases. As a result of these tests, a standard specimen size of 450 x 450 x 125mm was defined.

Since one and se of this material is to be a capability to rapidly upgrade the potential resistance of a existing structure, a major consideration is that age to gain sufficient strength to resist attack must be minimised. Without using fine-ground cements and/or concrete admixtures, the extent to which the commissioning time may be reduced is limited; however it was felt that an age-to-test of three days represented a reasonable compromise.

All mix designs were developed assuming completely dry aggregages. Since it is not possible to justify this assumption with available material, a moisture content calculation, using a standard siphon-can test (British Standard 812 (7)) is carried out on each aggregate immediately prior to casting. The percentage moisture content by dry aggregate mass is calculated, this contribution being allowed for by an increase in aggregate weight and a decrease in weight of water in the final mix designs.

All mixing is carried out in a horizontal rotating pan mixer; the concrete constituents are charged in a standard order, that is, fine and coarse aggregates mixed together before the cement and water are simultaneously added to the mix. For all the various fibre types it was found that the optimum fibre distribution was established by adding the fibre to the already mixed concrete matrix. This ensures a minimum of 'balling' of the discrete fibre lengths. In the case of both the steel and polypropylene fibres, sufficient separation can be achieved by shaking the fibres slowly into the surface of the rotating matrix, through a large mesh. A more rigorous and timeconsuming process is necessary to persuade the very fine (12µm) KEVLAR-29 single filaments to reparate to an acceptable degree. The procedure adopted is to initially separate the matted fibre by hand to reduce it to reasonably small congloserations. It is then pneumatically injected directly onto the surface of the rotating concrete so as to further encourage it to separate. The more open mat can thus be worked into the concrete by the action of the mixer paddles. Whilst this

method does not ensure a complete separation of all the fibre conglomerations it does give a composite mix of reasonably uniform appearance, becoming less acceptable towards the maximum fibre volumes which can be incorporated. In a field situation it would perhaps be more viable to use a technique in which the sprayed concrete passes through a pneumatically held curtain of fibre, though the practical problems of this kind of approach have not yet been fully considered.

All specimens are de-moulded after one day and stored in a standard high humidity room (20  $\pm$   $1^{\circ}$ C:90% + R.H.) until immediately prior to testing.

#### TEST TECHNIQUE

After curing specimens are rigidly fixed in a target frame offering firm edge support to the back face of the specimen, with the 450mm square cast face pointing towards the projectile firing equipment.

The projectiles are fired remotely in an enclosed 20m long firing range. A 7.62mm diameter rifle barrel is attached to a pressure housing incorporating a breech, firing pin, bolt and trigger mechanism with safety catch. The pressure housing is itself rigidly attached to a steel frame which in turn is bolted to the range floor. The trigger mechanism is connected by a detachable linkage rod to an 11.4kg pullout, 18mm stroke length mains solenoid. For safety reasons the solenoid is activated remotely using a firing box fitted with an arming key and off-biased switch. Connection wires are coaxial and a capacitor is used across the switch to reduce electrical interference with ancillary equipment.

High speed photography is being used in an attempt to capture the detail of the impact event. Using a Barr and Stroud rotating mirror camara, capable of a framing rate up to two million frames per second over 30 frames, a series of photographs of the bullet in flight taken at 1.5µm interframe has been produced. The variable nature of both the bullet detonation and the welocity in flight make it difficult to accurately predict the time to impact of the projectile with any degree of precision (relatively to the camera's capabilities). Bence, any attempt at photographing the bullet in this way must carry only a limited probability

of success. In order to offset this, a rotating prism camera, capable of up to 20,000 frames per second is also being used, though this is not capable of the same amount of detail.

Various types of detector to measure crack valocity, spall characteristics, stress wave propagation and projectile retardation through the target are also under development.

#### POST TEST ANALYSIS

Damage to an impacted target consists of front face spall damage, a burrow and possibly back face scab damage. Spalling and scabbing result in craters being formed, the extent of damage may then be quantified in terms of the dimensions of these depressions. With fibre inclusions a lot of damaged material remains loosely attached to the target. This is removed to expose the true crater whose depth at various grid points can be found using a specially constructed rig with depth gauge connected to a displacement transducer which in turn is connected via an analogue/digital converter to a microcomputer. This automatically produces crater profiles and calculates crater volumes. Details have been given by Anderson et al (6).

Preliminary tests in which target perforation occurred showed that the projectile exit nole was rarely in line with the initial impact hole. Deviation of the projectile from its original flight path must have taken place within the target. Since to assess the resistance of the particular specimen it is necessary to measure the penetration path length, a 150mm diameter core is taken perpendicular to the target front face and containing the damaged section of the sample. If the slab has not been perforated, thin slices are sawn from the rear face of the core, and parallel to it, until the hardened steel tip of the projectile is encountered. Using both this point and the entrance position of the projectile, a most probable path may now be estimated to allow the core to be sectioned, thus exposing the burrow formed in the composite.

#### RESULTS AND COMMENT

This experimental programme is still in progress and vary few statistical series have been completed, those serving only to establish the arithmetical correctness of the microcomputar based unalysis. Various practical difficulties have yet to be overcome, including control of the aggregate soisture content and a valid method of assessing its contribution to the concrete matrix. Since using the dry mix spraying process water/ coment ratio is controlled by the apray gum operator, it is important that a fundamental understanding of the effect of varying weter content is attained. It is considered that, providing a rigorous control of the fibre concrete constituents can be ensured, the surface response theory approach should give an acceptable solution, within the limits dictated by the nature of dynamic testing.

Experimental work is proceeding to establish the mechanisms of failure and also to record the characteristics of the overall impact event.

Examination of a sectioned sample, after penetration, typically shows a crater of approximately 100-130mm diameter and 30-40mm depth developing into a burrow, which may be straight for the first 20-30mm. However, probably at the point where the copper jacket strips from the hardened steel core, the penetration path deviates from the original flight path (i.a. normal to the impact face) by an angle of up to approximately 80°, the position of this deviation is marked both by the presence of the jacket and also by a local widening of the burrow, as shown in Plate 1.

The hardened steel core may then continue along the new straight path for a distance of up to 70-80mm before coming to rest, Plate 2. Alternatively the same sort of distance may be travelled on a curving path, Plate 3, which may, in extrame cases, lead to the projectile coming to rest in a direction totally opposite to its orientation on entry, Plate 4. It should be noted that these targets have been sectioned and the full thickness is not shown in Plates 3 or 4. If the change of projectile direction is extreme, and perhaps dependent upon whether the core is in collision with aggregate or mortar immediately after the copper jacket is stripped, the hardened steel core may undergo a stress which exceeds the material strength, hence the core fractures and rapidly comes to rest, Plate 5.

Preliminary panetration tests carried out on specimens prepared to determine the maximum volume of KEVLAR-29 which could be incorporated in the concrete mix indicated an interesting trend. In several cases it was observed that normal penetration depth, as opposed to penetration path length, was much lower than expected because of gross deviation of the projectile during panetration. This change in path seems to have occurred as the projectile travelled through conglomerations of fibre within the composite. These conglowerations of fibre were a result of trying to incorporate too much fibre in the mix. This behavious suggests that the projectile may be induced to deviate during penetration by incorporating a series of "relative voids" (compared to the desmity of the concrete) into the composite. First indications are that the voids need to be slightly smaller than the projectile length to induce instability.

Some problems exist with this type of approach however, the first being that it is necessary to fully understand the mechanisms involved in the projectile/composite interaction in order to ensure that deviation does occur. Another problem is the reduction in structural integrity which will result from deliberately including voids in the concrete. It may perhaps be necessary to restrict the use of such amaterial, employing it solely for up-grading pruposes or existing structures. The difficulty of ensuring a reasonable distribution of "relative voids" using

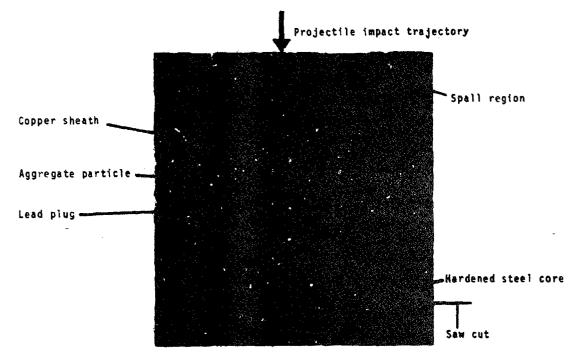


Plate 1 Penetration of hardened steel core projectile through a fibre reinforced concrete target showing deviation of projectile path where sheath is stripped from projectile core



Flate 2 Deviation of projectile along a straight path



Plate 4 Deviation of projectile to complete a U-turn



Plate 3 Deviation of projectile along a curved path



Plate 5 Deviation of projectile causing fracture of the hardened steel core

a sprayed concrete process would also need to be overcome.

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# 1210



ANALYTICAL AND EXPERIMENTAL STUDIES ON PENETRATION INTO GEOLOGICAL TARGETS

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#### ABSTRACT

This paper summarises some recent analytical and experimental work on penetration into geological targets. Results from several elastic-plastic type theoretical models which predict forces on penetrators for normal impact into dry porous rock, concrete, and sea ice targets are presented and compared with measurements from field tests. Rigid-body acceleration data from newly developed laboratory scale experiments for impact velocities between 0.2 and 1.2 km/s are also presented.

#### ANALYTICAL MODELS

In recent papers, Forrestal and Longcope [1,2,3] develop several elastic-plastic type theories to predict forces on conical-nosed penetrators. Constitutive target description consists of a linear hydrostal and a Mohr-Coulomb failure criterion with a tension cutoff [4]. Mathematically,

$$p = K\eta$$
 (la)

$$\sigma_{r} - \sigma_{\theta} = \mu p + \tau_{o}$$
 ,  $\tau_{o} = (1 - \mu/3)Q$  (1b)

$$\sigma_{g} \ge - \Upsilon$$
 (le)

where p is hydrostatic pressure, n is volumetric strain,  $\sigma_r$ ,  $\sigma_\theta$  are radial and circumferential stress components, measured positive in compression, Q is unconfined compressive strength, and Y is tensile strength. As shown in [1,2], these equations provide reasonably accurate data fits to triaxial material test data for dry porous rock, concrete, and sea ice, These analyses use the cylindrical cavity approximation [5] which idealises the target as thin independent layers normal to the penetration direction and simplifies the problem to one-dimensional wave propagation in the radial direction. Governing equations are subsequently reduced to

nonlinear ordinary differential equations with a similarity transformation and solved numerically or in closed form.

Layers of target material are expanded by the penetrator nose which opens a cavity large enough to permit penetration. This expansion produces annular regions of plastic and elastic response. Forrestal and Longcope [1,2,3] develop four target response models; rigidplastic, elastic-plastic, rigid-crackedplastic, and elastic-cracked-plastic. elastic-plastic model is derived first and results show that circumferential target stresses in excess of reported tensile failure values [4] can be developed. To correct for this inadequacy, the rigidcracked-plastic model is developed. This model has three regions of response; a plastic region next to the penetrator nose, a radially cracked region with circumferential stress set to zero, and a rigid region. As typical with rigid regions in plasticity solutions, particle velocity is taken as sero and the Stresses are taken as those from the static solution [6]. For the elastic-cracked-plastic model, the rigid region is replaced by an elastic region.

To calculate penetration resistance, radial stress on the penetrator nose is required as a function of the target material properties, penetrator nose shape, and penetrator axial velocity. As derived in [7], the axial resultant force on a conical nose is given by

$$F = \pi a^2 \sigma_{\underline{r}} \tag{2}$$

where a is the radius of the cylindrical afterbody and  $\sigma_{\Gamma}$  is the radial stress on the ponetrator nose calculated from the target motion analyses described above. Radial stresses on the penetrator nose from the four response models for a sea ice target with  $\rho_{0}=0.92~{\rm Mg/m^{3}},~K=4.0~{\rm GPa},~\tau_{0}=10.5~{\rm MPa},~\mu=0,~{\rm Poisson's}~{\rm ratio}~\nu=0.27,~{\rm and}~\Upsilon=0.86~{\rm MPa}~{\rm are}~{\rm shown}~{\rm in}$ 

in Fig. 1. These data and equation (2) can easily be applied to obtain penetrator rigid-body motion. Radial stress curves of the type shown in Fig. 1 are given in [1] for a concrete target and in [2] for a dry porous rock target.

# COMPARISON OF PREDICTIONS WITH PIELD TEST DATA

Test results for penetration into pack ice targets located in the Lincoln Sea, near Alert, Northwest Territory, Canada, are reported by Young [9]. penetrators had total length 1.07 m, outer diameter 70 mm, a conical nose with length 140 mm, and mass 23 kg. Four penatrators were air-dropped and impacted the pack ice layer at V<sub>g</sub> = 159 m/s. Onboard accelerometers, signal conditioning equipment, and a transmitter were contained within the penetrators. The transmitter package occupied the aft 18 mm of the penetrator and was stripped from the main penetrator by fins which eventually interacted with the ice target near the surface. Thus, the transmitter remained near the ice surface, remained electrically connected to the main penetrator with a trailing line, and transmitted accelera-tion-time data to an airborne receiving station. Four decementation-time records with 1 kHs resolution are presented by Young [8] and one of these records is shown in Fig. 2.

Predictions of rigid-body penetrator decelerations using Nounds on the shear strength data are also shown in Fig. 2. From Fig. 1 and equation (2), deceleration is calculated from

$$m \frac{dv}{dt} = -F \tag{3}$$

where m is the penetrator mass. The penetrator strikes the target at  $V_g = 159 \text{ m/s}$  and the calculation starts when the nose is fully embedded. After nose penetra-tion, t > 1 ms, the theory predicts a slight decay. At t = 8 ms, the penetrator has traveled one body length and it is assumed that the transmitter package with mass 3.2 kg has been suddenly removed by the ice crater. This mass change produces the acceleration jumps shown in Fig. 2. After t = 8 ws, the penetrator progresses with mass 19.5 kg and eventually comes to a sudden stop. The sudden deceleration change coores because a minimum threshold value of radial stress is required to open a cavity and permit penetration. This threshold stress is the quasi-static This solution shown in Fig. 1 for V approaching

Comparison of pradictions and measurement from a field test into Antelope tuff, a dry porous rock target, at the Sandia Tonopah Test Range, Nevada, is shown in Fig. 3. This penetrator has total length 1.56 m, afterbody diameter 0.156 m, mass 162 kg, and an ogival note with 6.0 CRM. The previously discussed theories are developed for conical-nosedpenetrators, whereas this penetrator has an ogival nose. Data from several hundred soil penetration tests [10] indicate that a 6.0 CRM ogival nose and a conical nose with half apical angle  $\phi = \tan^{-1} Q.30$ are nearly equivalent and this is used for the trajectory calculation. For this test the penetrator was propelled with a Davis gun and impacted the Antelope tuff layer at 520 m/s; other test details are reported in [2].

As discussed in [2,9], sliding frictional forces produce an additional source of resistance to penetration and the predictions shown in Fig. 3 include and neglect sliding friction. Prictional resistance is velocity dependent [11] and this machanism is required in order to qualitatively predict deceleration-time profiles into dry porous rock targets.

#### LABORATORY SCALE EXPERIMENTS

Recent laboratory experiments were devised [12] in order to complement field test programs and to obtain data at impact velocities beyond the current field test capability. Gas gums are used to accelerate foundry core targets (a simulated soft mandstone) to steady velocities after which the targets impact 20.6 mm diameter penetrators instrumented with piezoelectric accelerometers. Rigid-body acceleration data are recorded for one ogival and two conical nose shapes over impact velocities between 0.2 and 1.2 km/s. Data from these penetration experi-ments show a departure in the scaling law which relates force to penetrator velocity for all three nose shapes at impact velocities in the neighborhood of 0.5 to 0.6 km/s, which is currently the limiting impact velocity for full scale tests.

Data and a power law fit for a 6.0 CMM nose shape are shown in Fig. 4. Penetration data in Fig. 4 were obtained from experiments conducted on the Air Porve Weapons Laboratory 102 mm bore gas gun and the University of Dayton Research Institute 178 mm bore gas gun. Majurity of the data were obtained with the 102 mm gun and the experiments with the 178 mm gun were conducted in order to demonstrate that sample size did not significantly affect penetration registance.

The analytical models discussed previously are electic-plastic models. However, triaxial test data for the foundry core material [12] indicate no yielding of the material and the existing models are not directly applicable. Work on modeling of the foundry onre material and developing a penetration theory for this target material will be conducted in the future. Since empirical models are widely used as predictive tools, the data in Fig. 4 can be described conveniently in the form

$$P = KV^{T}$$
 , 0.5 < V < 1.2 km/s (4)

where K=109, n=1.29, and F, V have units of kN, km/s. The root mean relative error for the data fit is 0.6 percent.

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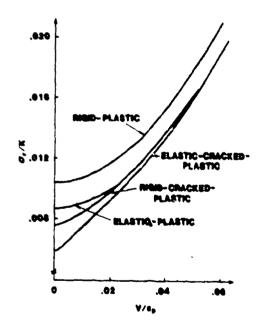
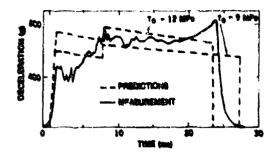
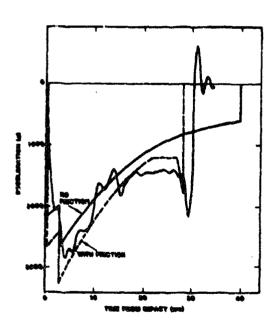


Fig. 1. Radial stress on the penetrator conical nose.  $V = V_{_{\rm Z}}$  tan  $\phi$ ,  $c_{_{\rm p}}^2 = K/\rho_{_{\rm 0}}$  where  $V_{_{\rm Z}}$  is axial panetrator velocity and  $\phi$  is the half apical nose angle.



Pig. 2. Deceleration-time measurement and prediction bounds for a sea ice target.



Pig. 3. Deceleration-time measurement and predictions for a dry, porous roof: target.

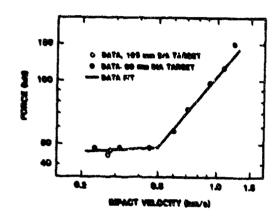


Fig. 4. Leboratory scale data and power law fit for a 6.0 CRM ogival nose.





# PENETRATION REMAVIOUR OF NICKLY DEPORTABLE PROJECTILES IN CONCRETE SLASS

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#### ABSTRACT

Investigations of the penetration behaviour of deformable projectiles in reinforced concrete slake show that "classical"Openetration formulas developed for rigid projectiles are not applicable to describe the penetration at impact velocities between 190 and 600 m/s. The measured crater depths are smaller, the divergence increases with higher velocities, because the projectile deformation itself consumes a considerable amount of the kinetic energy of the projectile.

#### INTRODUCTION

Before and during World War II many experimental investigations concerning penetration and perforation of projectiles into concrete slabs have been performed. The results of these tests formed a data base for many empirical and semi-empirical formulas. However, these formulas are strictly applicable only for these input data.

In recent years special eschasis has been given to the problems of impact of highly deformable projectiles, e.g. airplane crash on a nuclear power plant. The purpose of investigations performed at the Ernst-Mach-Institut, Freiburg, is to study the penetration as well as deformation of highly deformable projectiles within the velocity range between 100 and 400 m/s. The influence of target discussed.

# PACILITY DESCRIPTION, PROJECTILE AND SABOT DESIGN

The launcher (Fig. 1) is a compressed air gun for the low velocity regime (50 - 250 m/s) and a normal powder gun for the higher impact velocities. For both configurations the same launch tube is used. The launcher consists of a pressure reservoir and a smooth-bore 100 mm disester launch tube. A disphragm separates the two parts, mylar or sluminium are used as disphram materials. Pressure reservoir and launch tube are coupled with a hydraulic clamp. The velocity of the test item is controlled by varying the pressure in the case of air gen. The gun is fixed on a stable platform.

The gun fires into a clued range. This range consists of three parts (Fig.2): a blast tank (3), the velocity measurement station (4) and the import tank (5). Sabot separation from the projectile takes place in the blast tank. Measurements of projectile velocity are typically performed on each test using two direct shadowgraph stations with point light sources and an electronic counter. The point spark light sources are triggered by laser light screens or by rupture of a thin copper wire.

Two typical shadowgraph pictures with the nose of the projectile are shown in Fig. 3. The projectile velocity is determined to an accuracy of about ± 0.5 %. The concrete slabe are suspended in the impact tank. The angle of incidence can be varied from 0° up to the ricochet angle by rotating the target suspension. The projectiles are scaled 500 lbeand 1000 lbs general purpose bomb-models (scale factor 1 : 4.5). Bomb-models and targets have been scaled according to the scaling laws [1].

- All linear dimensions of the targets and projectiles should be reduced in proportion to the scale.
- Original and model should have the same geometrical shape.
- The models and the originals should have the same densities and strength properties.
- The impact velocities of full scale and model tests should be equal.

The scaled bomb-models are shown in Fig. 4. Only the mean dimensions of the bomb-models are scaled exactly. Details like fins, fuse etc. have been ignored.

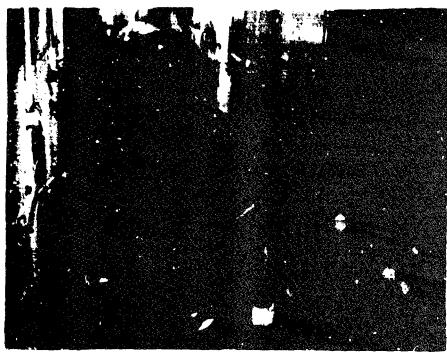


Fig. 1 Photo of impact facility

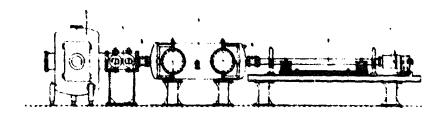


Fig. 2 Schematic of impact facility

The sabot for the 1: 4.5 scaled GP-bomb-models is a four pieces sabot with a poly-ethylene pusher. Its function is to protect the bomb-model from high pressure and to guide and accelerate the projectile in the launch tube. It must serve as a good pressure scaling during the acceleration. The sabot should be as light as possible and as strong as possible. Hard styrofosm is used for the four pieces,

because this material is light and retatively strong. For higher velocities the fear-material can be reinforced with stronger materials, fibers etc. The schot configuration is shown in Fig. 5.

The targets are concrete slabs of quality BM35 with cubic reinforcement. The size of the targets was 80 x f0 x 40cm, thick enough to prevent spallation at the





Pig. 3 Shadowgraphs of the projectile

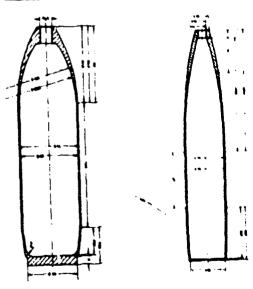


Fig. 4 Bomb models



Pig. 5 Sabot contiguration

rear side of the target. Thus, the target can be considered semi-infinite, because the target thickness was substantially thicker than the crater depth for all tests.

# RESULTS

The measured crater depths produced by the 500 lbs-GP bomb-model are shown in Fig. 6 in comparison with well known penetration formulas: Petry Formula, Corpe of Engineers formula (COR) and Mational Defence Research Committee (HN-MDRC) formula.

Within the velocity range investigated a considerable discrepancy between measured and predicted crater depths is obvious. All experimental data range below the calculated ones, only the Petry formula gives some accordance with the experimental data at low velocities (100 - 150 m/s). The reason for this discrepancy can be derived from Fig. 7. It shows that the projectiles behave as rigid bodies only up to a velocity of about 100 m/s, for higher velocities plastic deformation is of increasing influence. An increasing amount of kinetic energy is needed for the deformation, reducing the energy portion available for cratering. In addition, an

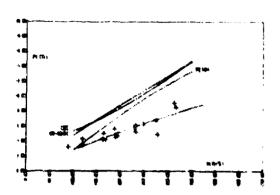


Fig. 6 Penetration depth versus impact velocity (comparison with formulas)

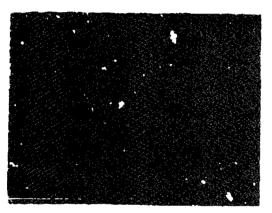


Fig. 7 Deformed bomb models

increase of the projectile cross section is observed, which leads to lower penetration depths. Since 1975 several impact formulas have been developed for deformable projectile penetration. One of them is the Mar-formula [2,3].

In Fig. 8 the Kar formula is plotted together with the penetration depths obtained from the 500 lbs and 1000 lbs model-bembe. It is in good accordance with the experimental data obtained with the 1000 lbs model-bombe having a smaller caliber/wall thickness ratio than the 500 lbs model-bombe. For the more deformable 500 lbs bomb models, however, accordance is only observed at lower velocities (< 150 m/s). The penetration formula of Kar, therefore seems to be valid only for weakly deformable projecties. Parthermore the influence of the angle of incidence on cratering has been investigated. In Fig. 9 corresponding penetration depths for 00, 150 and 100 are plotted varsus the impact velocity. The 100 values are only in

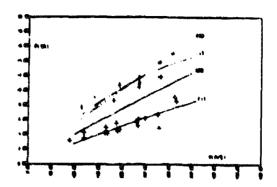
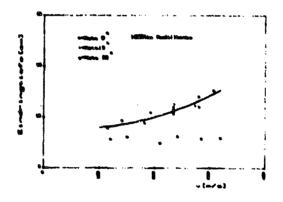


Fig. 4 Penetration depth versus impact velocity (comparison with Rar-formula)



<u>Fig. 9</u> Penetration depth for different impact angles

accordance up to velocities of about 150 m/s. For higher velocities the penetration depths are no longer increasing.

The considerable scatter of data for oblique impact is due to an increasing influence of the reinforcement. It is well known that no invluence of plate thickness on crater depth is measurable if the plate thickness is more than three times the crater depth. For lower values we observe a more or less strong influence of the plate thickness on the crater depth, Only little is known about the influence of the lateral plate dimensions on crater depths. In order to study this influence, plates with different lateral dimensions have been impacted and also plates with identical dimensions were impacted are different distances from the edge of the plates. The results show that in both cases only a small increase of crater depth was observed as long as the crater depths are

much smaller than the thickness of the plates.

#### CONCLUSION

The results demonstrate that the penetration behaviour of highly deformably projectiles in concrete is substantially different from the penetration of rigid bodies and therefore "classical" penetration formulas cannot be applied.

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- (2) Assessment of Empirical Concrete Impact Pormulas G.E. Sliter Journal of the Structural Division (May 1980)
- Projectile Penetration into Buried Structures A.K. Kar Journal of the Structural Division, (Jan. 1978)





#### RAPID RURWAY CUTTING WITH SHAPED CHARGES

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#### ABSTRACT

Research has shown that removal of large, partially damaged, concrete runway slabs is a major element in the time required to perform a runway repair operation. A rapid method for cleanly cutting away damaged sections would significantly reduce overall repair time. Shaped charges are potentially just such a rapid runnay cutting technique. This paper presents the results of field tests designed to evaluate the runway cutting abilities of standard and linear shaped charges. A series of 25 runway cutting tests was conducted on the 1-ft-thick (4 in of asphalt + 8 in of concrete) undamaged taxiway segments constructed for a recent Air Force test program at the Whitu Sands Missile Range. Although TOW warhead charges successfully penetrated well into the subgrade, no cracks were observed between holes, even at the closest charge spacing. Arrays of linear shaped charges were successfully fired to produce a relatively smooth, uniform cut through the concrete. It was found that inexpensive, "homewade" linear charges gave results comparable to commercially manufactured charges,

## BACKGROUND

The U. S. Army Corps of Engineers is charged with responsibility for runway repairs at U. S. Air Force (USAF) airfields damaged by conventional attack when such repairs exceed USAF on-offe capabilities. The importance of this wortime mission is obvious in light of our commitments in both Europe and the Middle East, where rapid serial reinforcement and resupply will be essential. Research on Repair and Restoration of Paved Surfaces (REREPS) has been performed at the Waterways Experiment Station (WES) to develop an improved Army capability for rapid runway repair under combat conditions.

REREPS research has shown that removal of large, partially damaged, concrete runway slabs is a major element in the time required to perform a runway repair operation. A rapid method for cleanly cutting away the damaged portions of these slabs is needed to significantly reduce overall repair time. Some cutting techniques currently under investigation include concrete saws, water jets and shaped charges. This paper presents the results of shaped charge runway cutting tests

conducted by the WES Structures Laboratory (with the assistance of personnel from Company D, 52nd Engineer Battalion (Ft. Bliss, TX)) at the White Sanda Missila Range, NM.

#### OBJECTIVE

The study objective was to evaluate shaped charges as a means for rapidly cutting damaged runways. Specific test objectives were to avaluate the runway cutting abilities of conical shaped charges, and commercially manufactured and "homemade" linear shaped charges.

#### APPROACH

Shaped charge runway cutting tests were conducted on undamaged taxiway segments constructed for recent Air Force quantity-distance experiments at the Queen 15 site on the White Saids Missile Range, NM. The taxiways were built to design standards currently in use at USAF Europe bases in Germany. Pavements consisted of 8 in thick unreinforced concrete slabs overlain by 4 in of asphalt, and underlain by a 6 in stabilized aggregate base course over a compacted subgrade (Figure 1).

WES obtained a number of surplus TOW (Tube-launched, optically-tracked, wire-guided, antitank weapon) werheads. The TOW werhead consists of a conical shaped charge approximately 5 in diameter containing 5.4 lb Composition B emplosive (Figure 2). The werheads were fired individually to determine optimum standoff and in linear arrays to determine if the slab would fracture between penetrations. The charges were statically fired with the windbreak left implace giving a minimum shaped charge standoff of 4.2 in. Standoffs for individual firings ranged from this minimum to a maximum of 2.85 ft. The linear arrays were fired with spacings of 9, 12, and 18 in, all using the minimum stanc.ff.

Commercial linear shaped charges were purchased "off the shelf" from Jet Research, Inc (JR), Arlington, Texas, in 2.5 and 4.5 lb/ft designs. The charges contained Composition B as the primary explosive. The manufacturer's quoted price was \$125 and \$145 per ft length, respectively. The 2.5 lb/ft charge came with an underwater housing

(Figure 3), giving a minimum standoff of 1.75 in. The 4.5 lb/ft charge (Figure 4) could be placed directly on the target surface (0 in minimum standoff, i.e., with no standoff).

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In an earlier study at WES, the effectiveness of nitromathene (NM) as an explosive source in "homemade," conical shaped sharges was investigated. Although it was found that twice as much He was needed to obtain the same shaped charge penetration depth as standard shaped charges using solid explosive, it was felt that NH has several overriding advantages. The advantages of using for example; 1) it is classified as a flammable liquid and is shipped and stored as such, and 2) as a liquid it has uniform properties and assumes the shape of the container used. Conventional shaped charges, on the other hand, use high explosives and are subject to the shipping and storage restrictions of those caterials, with controls such more stringent than those for flammable materials. Because of these reduced restrictions, the use of MM for runway cutting charges could be a distinct advantage at USAF Burope bases, with their congestion and limited munition storage capacities.

The RM linear shaped charge container used in these tests was designed and fabricated at WES. This container is shown in Figure 5 (plan and cross-sectional view). A 3/16 in thick brass liner with 60° included angle and 4 in throat width was selected for this charge. Thus, the liner thickness is 4.7 percent of the throat width, which is larger than the normal range of 0.5 to 3 percent for conical shaped charges. Limited comparative testing with 1/8 and 3/16 in thick liners at WES indicates that the thickness liner performed better for soil penetration. A 4 ft charge length was selected to insure that the detonation would propagate in a linear fashion.

#### RESULTS

Shot geometry and penetration data are presented in Table 1. The holes produced by all TOW warhead firings are skatched in Figure 6. The TOW penetrated the pavement without difficulty, reaching a maxisum hole depth of 7.2 ft at the minimum standoff of 0.35 ft. Typically, the warhead cratered the 4 in thick bituminous surface layer of the pavement, and punched a hole on the order of 2 in in dismeter through the underlying concrete and well into the subgrade. However, no interhole concrete cracking was noted in any of the linear arrays (even with a charge spacing as close as 9 in), although the asphalt layer was usually excavated between shot holes by the blast.

The NH linear shaped charge craters are sketched in Figure 7. These charges showed a capacity to satisfactorily penetrate the taxiway. The maxisum panetration of 1.0 ft was obtained from charges at 4 in standolf, or one throat

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width above the surface. Typically, the crater width in the asphalt was 2 ft, or 3 to 4 times the crater width in the underlying concrete. When individually-boosted NH linear shape, charges were placed end-to-end and detonated through a primacord ring main, they successfully sustained a relatively uniform cutting action over the length of the array.

Crators produced by the JR commercial linear shaped charges are sketched in Figures 8 and 9 (2.5 and 4.5 lb/ft charges, respectively). The charges performed best at the manufacturer's built-in standoffs of 1.75 and 2.25 in for the 2.5 and 4.5 lb/ft charges, respectively. The smaller charge did not completely penetrate the concrete. The larger JR charge, like the NM charge, was just adequate for this purpose. It also demonstrated the capability to excavate a relatively smooth cut over whatever distance might be desired, including a cut around a 90° corner (Shot 25).

#### DISCUSSION AND CONCLUSIONS

An early Picatinny Areenal report (Reference 1) indicates that the conical shaped charge penetration roughly ocales in proportion to the cube root of the explosive charge weight in permafrost. Using the analogy of apherical cratering charges to linear cratering (ditching) charges, square root scaling of linear shaped charge penetration is suggested as a logical extension. The maximum penetration of the 2.5 and 4.5 ft/lb JR charges and the MES 12 lb/ft NM charge are plotted in Figure 10 in an attempt to provide information for prediction of the linear shaped charge necessary to cut various runway thicknesses.

Square root scaling curves are presented in Figure 10 for the 4.5 lb/ft JR charge and the WES 12 lb/ft NM charge. The 2.5 lb/ft JR charge penetration data point falls 38% below the prediction curve. This is probably due to the fact that the smaller JR charge was not an exact physical model of the larger charge, and partly due to normal data scatter. A larger sample of penetration versus optimum standoff data is necessary before a statistical scaling relation can be determined.

The TOW warheads are not by themselves usefull in cutting runway slabs. Linear shaped charges are a feasible method for rapidly cutting runways so as to permit removal of damaged slabs. Final proof of this awaits a full scale demonstration to include removal of a slab.

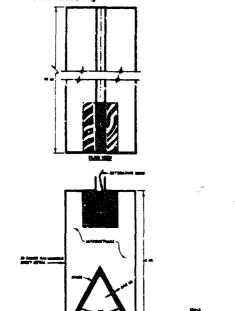
#### REFERENCES

 Rlamer, Oscar A., "Shaped Charge Scaling," Technical Mamorandum 1383, March 1964, Ammunition Engineering Directorate, Picatinny Arsenal, Dover, NJ.

igure ). Typical DISTANT NUMBER taximay cross-section.
"CE-55" refers to a standardised compactive offort
developed by the Aberican Association of Highmay



Figure 3. Two 2.5-1b/ft JR charges with underwater housing.



Pigure 5. Design of 12.0-16/ft am Sineer stoped :harpe.



Figure 2. TON warhead being placed nose down on pavement for firing.



Figure 4. Two 4.5-1b/ft JR charges mounted end-to-end on manufacturer-furnished standoff.

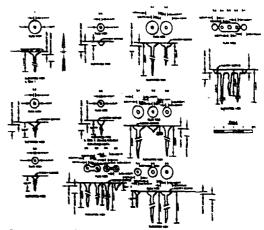


Figure 6. Barults of TON warhoad shats. "COSC" and "ASP" identify concret

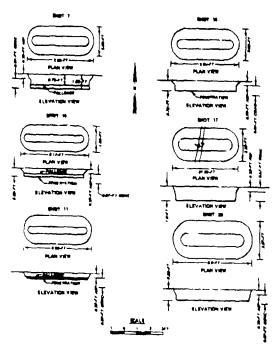


Figure 7. Results of 101 charges.

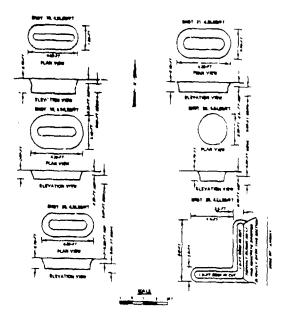


Figure 9. Results of JR 4.5-16/ft charges.

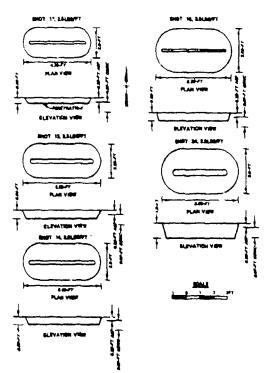
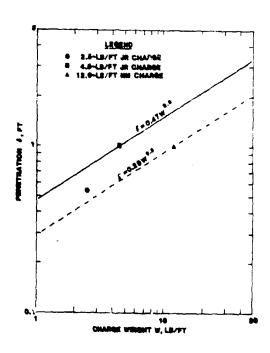


Figure 8. Results of JR 2.5-16/ft charges.



PIGGRE 16. LINEAR SHAPES CHARGE TAXINGY PRINCIPATION

					Shot Geometry			Panulta		Floure
Day/flox	<b>-</b>	<b>-</b>	Charge Type	Locations	Standoff	Shot G	Description	Penetration	Description	Figure Ro.
August 15		No.		LOCAL TON-	ft	it.		ft	441,000	
4/0958	٠,		TON	2-12	Q. 358e		Nose cone on pavement	7.17	0.17 ft diameter	
10/1104	2	-1	TON	E-17	0.83			••	Full over during detonation; shallow crater	•
		-2	TON	k-13	1.33			5.23	0.17 ft diameter	
		-1	TON	I-13	1.05		••	3.47	G.12 ft disseter	
		-4	TON	8-14	2.35	••		0.42	Hole plugged	i
		~3	TOW	E-14	2.85			3.33	0.12 ft dismeter	•
16/1200	3	-1	TOW	C-13	0.15	1.00	None come on pavement		Malfunctioned?	
		-2	TON	C-13	0.35	1.00	Nose cone on pavement	4.83	0.21 ft dismeter; shallow connection to 3-3	٠
		- 3	TON	(-13	0. 35	1.00	Nose come on povenent	4,42	0.17 ft diameter; shallow connection to 3-2	٠
		-4	TON	C-13	0.35	1.00	Nose cone on pavement	5.42	0.2) ft dismeter; shallow connection to 3-5	
		-5	TOW	C-13	0.35	1.00	Nose come on pavement	0.71	0.21 ft diameter; shallow connection to 3-4	•
16/1330	4	-1	TON	C-17	0.35	1.5	None come on pavement	5.83	0.25 ft dimmter	
		-2	TOW	C-12	0.35	1.3	Nose come on pavement	1.25	0.21 ft diameter	8
		- 3	TON	C-12	0.35	1.5	Nose come on pavement		Mai funct toned?	
		-4	TON	C-17	0, 35	1.5	None come on payement		Hel functioned†	
		-5	TOW	C-13	0. 35	1.1	Mose come on payement	••	Halfunetioned?	
16/1447	5	-1	TON	C-12	0.35	1.5	Mose come on pavement	5.75	0.33-ft diameter	
		-2	TOW	C-12	0.35	1.5	Nose cone on pavement	0.47	0.21-ft dismter	
		- 1	TOM	C-12	0.33	1.5	Mose cone on pavement	5.50	0.33-ft diameter	
		-4	TON	C-12	Q. 33	1.5	Nose cree on payment	1.58	Q.12-(t dismeter	
		-5	TON	C-13	0.35	1.5	Mose cone on pavement	5.42	0.33-ft diameter	
		-6	TOW	C-12	0, 33	1.5	Nose come on pavement	5.42	0.25-ft diameter	•
17/09 14	•	-1	1000	V~15	0.35	0.75	Nose come on pavement		Shallow crater through amphalt only	
		-2	TON	W-13	0.35	0.75	Home come on pavement	4.83	0.29-ft diameter; connected to 6-3 by trench through apphalt	•
		-1	TON	W-11	0.35	0,75	Nose cone on pavement	2.25	Q.38-ft dismater; connected to 6-2 and 6-4	•
		-4	TOW	W-13	0.35	0.75	Nose come on pavement	4.50	0.25-ft dismeter; connected to 6-3 by tranch through asphalt	•
		-5	TON	W-17	0.35	0,75	House come on payment	••	Shallow crater through amphalt only	8
17/1103	:	••	101	E-11	0, 13		••	1.0	0.25 ft fallback	9
17/12/19	8	-•	NN	E-11	0.67	••	**		Hisfire	
17/1323	,		101	E-11	0,67		••		Niefire	
17/1405	10		101	E-11	0.67			0,58	Some fellback	•
17-1453	11		101	C-11	1.50			0.46	Some fallback	•

Table 1. Concluded

							Resulta				
Shot			Charge			Shot Geometry				Figure	
August 1	₩^.	No.		Туре	Location*	Standoff	Spacing ft	Description	Penetration ft	Description	No.
8/1036	13		JR	2.5 W/ft	¥-11	0.15	End to end	4 charges	0.42	Some cracking below penetration	10
8/1127	13		JI N	2.5 lb/fe	W-12	0.48	End to end	2 charges	0.54		10
8/1250	14		AI.	2.5 1b/ft	C#-11	0.31			0.50	••	10
8/1337	15		J R	2.5 1b/ft	E-11	0.15	••		0.50	Concrete cracked below penetration	10
8/1430	16		164		CM-12	1.00		**	0.75		9
8/1522	17		ĸ	,	C-10	0.33	<b>E</b> nd to end	5 charges	1.00	-	9
9/*015	18		JR	4.5 1b/ft	C-11	0.19	and to end	2 charges	0.79	••	11
9/1050	19		3 R	4.5 1b/ft	C-10	0.00	and to end	3 charges	0.47		11
9/1127	20		ЭR	4.5 1b/ft	C-11	0,38	End to end	2 charges	0.79		11
9/1248	21		JR	4.5 1b/ft	C-10	0,56	<b>B</b> nd to end	2 charges	0.79		11
9/1327	22		JR	4.5 1b/ft	E-10	0.28	and to end	2 charges	0.75	<b></b> .	11
9/1413	23		121		C-10	0.00	••	Single charge	0.83	••	9
9/145!	24	••	JR	2.5 lb/ft	E-11	-0.19	<b>Ind</b> to end	2 charges placed over crack in concrete from shot 15 (below original auriace).	1.00	Total penetration shots 15 and 24	<b>'</b> 0
20/0944	25		12	4.5 16/fc	B- 9	G. 19	End to end	Charges in "L" formation. 5 charges in each leg.	1.00		11

Expansion-joint "coordinates": east, center, west (E, C, W)--joint no.
 Includes built-in atandoff in mose (0.35 ft).
 Apparently detonated, but produced no penetration or crat.r.



K

MODELING THE BURN-TO-VIGLENT REACTION TO SIMULATE IMPACT-DAMAGED OF WARHEADS

الوالمتوالية المتار المعطرات أج والمتاري المهار

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#### **ABSTRACT**

Impact forces from hardened, concrete targets to a General Purpose Marhead (bomb) can in some cases cause outer-case failure and breakup of the high explosive (ME) filler prior to fuse initiation. The detonation that is expected to occur under reliable penetration and for totally confined conditions can be reduced to that of a rapid deflagration with reduced damage to the target/structure. This paper presents the solution to the dynamic equations of motion for gas-particle systems that simulate in one-dimension, the high pressure, subdetonation speed reactions in such beds of fragmented high explosive. It is clear from the results presented that initiation of a damaged, fragmented explosive will not necessarily result in a strong detonation if the mass and momentum losses from side vents (caused by the impact) are sufficiently large.

#### INTRODUCTION

The application of GP warheads on expensive, high priority sorties against hardened targets requires maximum reliability of penetration and detonation. Conditions can exist (off-axis impact; superior hardening) in which the conventional munitions fail to penetrate and detonate. The warhead failures are most often case failures (where the loads during impact cause rupture of the case and fragmentation of the high explosive) prior to fuse functioning. The result can be low-order detonation or unsteady deflagrations within the damaged explosive itself. However, such "explosive" reactions can still exhibit measurable lethal effects against substantial concrete structures, especially if the explosive is partially contained (by the surrounding soil, for example.)

Figure 1 is a sketch of a GP bomb that has cratered a concrete surface by impact only, causing partial case failure, and more importantly, causing sections of the high explosive to be fragmented into a configuration

which is similar to a packed bed of explosive grains.

What is envisioned to follow the impact and fragmentation is initiation of the fragmented explosive either by the fuse at one end or by friction/rapid shear at the case-filler interface. By separating the impact and material breakup/fracture from the initiation process, it is possible to perform the unsteady two-phase reactive flow analysis in order to predict whether DDT (deflagration to detonation transition) can be expected.

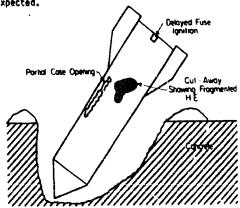


Fig. 1. Cratering of concrete surface by GP bomb impact

## ASSUMPTIONS

- (1) The analysis considered in this paper explicitly assumes that at time t = 0, initiation by the fuse ar rapid shear mechanism will allow a deflagration with the supporting pressure buildup to penetrate into the damaged (rubblized) explosive.
- (2) The deflagration and possible detonation occurs in only one dimension, x.
- (3) The surface-to-volume ratio of the

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packed particles (explosive) is sufficiently high to be equivalent to spheres of the millimeter and submillimeter diameter size (i.e.  $S_p/V_p$ 

- = 6/d<sub>p</sub>)

  (4) The possibility of mass, momentum and energy loss is treated by psuedo-<u>side</u> venting from cracks of prescribed sizes, located at prescribed distances along the bed. (Details are presented below.)
- (5) The separated two-phase flow analyses previously developed in Refs. 1 and 2 represent the basis on which we build the modeling effort presented in this paper.
- paper.

  (6) The decision on whether the fragmented bed of explosive will transit into a deconation is based on the transient reacting flow events occurring in the first 10 to 20 cm of length. A run-up of length greater than 20 cm requires times well beyond established experimental DDT events.
- (7) The explosive particles, ignited in a critical prescribed energy is transferred to the solid, will burn at a rate, r ap", where a and n are known values for typical warhead explosives (tritonal or H-a).
- (8) The porosity of the fragmented bed (gas volume/total volume) is uniform and typically of the order of 0.2 to 0.3.

# THE FLUID MECHANICS MODEL (MITH VENTING)

Our analysis of the ruptured shell casing problem represents an extension of previous work done at the University of Illinois for the analysis of two-phase, one-dimensional reactive flows [1, 2]. Modifications were made to account for the mass, momentum and energy losses occurring through the shell opening. A detailed derivation of the governing equations for totally confined (no loss) conditions can be found in Ref. 1.

In the analysis one must describe the conservation of mass, momentum and energy throughout the domain for both the solid particle phase as well as the gaseous products phase. Each phase separately its assumed to be a continuum and the system of governing differential equations can be expressed as:

#### Gas Continuity

$$\frac{3\rho_1}{3\xi} = \frac{-9(\rho_1 u_q)}{3x} + \Gamma - \rho_q \tag{1}$$

#### Solid Continuity

$$\frac{3\xi}{36\xi} = \frac{-3(6\xi^{0})}{3x} - L - 8^{b}$$
 (5)

#### Gas Momentum

$$\frac{3(p_1u_0)}{3t} = -\frac{3(p_1u_0^2)}{3x} = -\frac{3p_0}{3x} = 0 + \Gamma u_0$$

## Particle Momentum

$$\frac{a(\rho_{p}u_{p})}{at} = -\frac{a(\rho_{p}u_{p}^{2})}{ax} - (1-a)\frac{ap_{p}}{ax} + 0-pu_{p}$$

$$-\frac{a}{p}u_{p}$$
(4)

# Gas Enginery

$$+r[E_{GHEM}^{GHEM}, \frac{h}{n}] - h^{d} (E^{dL} + \frac{h}{h})$$

$$+r[E_{GHEM}, \frac{h}{n}] - h^{d} (E^{dL} + \frac{h}{h})$$

$$+r[E_{GHEM}, \frac{h}{n}] - h^{d} (E^{dL} + \frac{h}{h})$$
(2)

# Particle Energy

$$\frac{a(o_2E_{PT})}{at} = -\frac{a(o_2u_pE_{pT} + (1-\phi)u_pF_p)}{aF} + r[E_{CHEM}^b - \frac{a_p}{2}] + Dv_p + 0 - a_pE_{pT}$$
(6)

Here, the relations for the total internal energy in each phase are

$$E_{gT} = C_{vg}T_g + \frac{1}{2}u_g^2$$

and

$$E_{pT} = C_{vp}T_{p} + \frac{1}{2}u_{p}^{2}$$
 (7)

The subscripts g and p denote gas and particle, respectively. In Eqs. (1)-(6), the phase densities  $\rm p_1$  and  $\rm p_2$  are defined as

$$\rho_1 = \rho_{\alpha\beta}$$
 and  $\rho_2 = (1-\mu)\rho_{\beta}$  (8)

The porosity  $\phi$  is defined as the ratio of the instantaneous gas volume to the mixture volume. Hence, the solids frection is  $1-\phi$ .

In addition to the six conservation equations, three constitutive relations are needed in order to solve for the nine unknown variables.

Because of the restricted length of this manuscript, it is not possible to include a

discussion and description of the constitutive relations in any detail. However, in functional terms these represent:

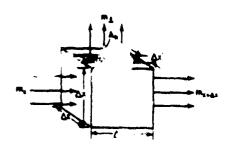
- (1) An equation of state (E. O. S.) for the product gases of the explosive, P = P (o , E ) . The particular equation of state used was discussed in Ref. 3.
- (ii) An equation of state for the solid phase, P = P (p, E), specifically the Tait Equation of State (see Ref.
- (111) A heat transfer coefficient which fixes Q in Eqs. 5 and 6 (see Ref.
- 2, 3)
  (iv) A ges-particle drag coefficient which determines D in Eqs. 3 and 4 (see Ref.
- (v) An ignition criterion, Tignit ≥ Tcrit (Ref. ?)
  (vi) A burning rate relation (as discussed above)

In equations (1-6) a represents the loss of mass (gas phase) as a result of the hole present in the shell casing. The appropriate variation of this term also appears in the momentum and energy equations.

# Mess Loss Due to Exterior Opening

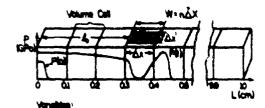
Figure 2 shows the fregmented bed being modeled. I imposed on the front face of the illustratio are the expected pressure-distance industriation, we the expected pressure-discence profiles unowing the pressure drop associated with the opening in the case well  $(x=0.3\ cm)$ . A simplified derivation for the mass loss throughout the bed length is as follows:

Consider the control volume shown below with gas being ejected out the hole:



The mass rate of gas lost per unit volume (9)

= ges density
= velocity of ges leaving the control volume. \* area of hole



4-detence from Ignitition and of bad to hate Co+(Ax/Ax), width of hole, Ax', may be varied n - number of volume calls with hos

Fig. 2. Schematic of fragmented bed being modeled

Due to the extremely high gas pressures in the bed, the gas escaping the control volume will always be choked. Hence u will equal the local speed of sound:

$$u = \left[ \left( \frac{2p}{8n} \right)_s \right]^{1/2} = u_s$$
 (10)

The area of the hole is defined as: A = 4 x 4 x 4 where 4= gas phase volume fraction. The volume of the control cell is given

Substituting into the definition of  $|\mathbf{g}_{\alpha}|$  , one

$$a_g = \frac{a}{V_{C,V}} = \frac{\rho_g u_g \Delta x \Delta x + \rho_g u_g \phi}{\Delta x^3} = \frac{\rho_g u_g \phi}{\Delta x} \left(\frac{\Delta x}{\Delta x}\right) \quad (11)$$

or.

$$g_{q} = \frac{\rho_{q} u_{q} \phi}{\Delta x} C_{q} \qquad (12)$$

where  $C_{\alpha}$  is an assumed "opening ratio",  $0 \leq C_{\alpha}$ 

If one is to consider entrainment of the unburned solid particles in the gas escaping through the hole, the mess loss per unit volume for the solid phase becomes

$$\beta_{p} = \frac{\rho_{p} u A_{h}}{\Delta x^{3}} + \frac{\rho_{p} u_{q}^{D} D_{q}}{\Delta x} C_{q}$$
 (13)

where D<sub>O</sub> is a drag factor between entrained

particles and escaping res. The parameter  $\theta_0$  has a range from zero to unity.

# Numerical Solution

The system of differential conservation equations described in the previous section, because of their nonlinearity, do not edmit an enalytic solution. In order to obtain a solution to the time-dependent differential equations, we chose to discretize the governing equations over the domain and write the x-deriva' res as center differenced first order approximations with the appropriate artificial smoothing to assure stability for the hyperbolic problem. The partial differential equations are then reduced to ordinary differential equations for a given time step and solved by a standard ODE numerical solver. The preceeding steps are repeated for each time step.

The results of two-phase reactive flow calculations are presented in the following section. A CDC Cyber 175 computer was used to numerically integrate the equations. A "typical" computer run consisted of a tid domain with 100 nodes and a total elapsed time of over 200 CP seconds.

## Computed Results

The solutions to the conservation equations (Eqs. 1-8) with their required constitutive relations will (a) show that even with a fragmented explosive bed, a detonation could occur if the container walls remained intact; (b) show that the over pressures could still be significantly high, and (c) most importantly, that a vented bomb condition could prevent a strong detonation and severely limit the overpressurization.

In all cases the container (see Figure 2) walls remained fixed. The pressures that are predicted (in the calculations to be presented) would obviously result in eventual explosion of the case wall with additional cratering and demage of nearby structures.

Figure 3 presents the predicted pressure development history for a completely confined accelerating deflagration process ( $C_0=U_c$  thus s and s = 0). The effective surface-to-volume ratio of the explosive (fragmented) particles was 6/dp = 120 cm<sup>-1</sup> loaded at  $(1-\phi_0)=70\%$  solids volume fraction.

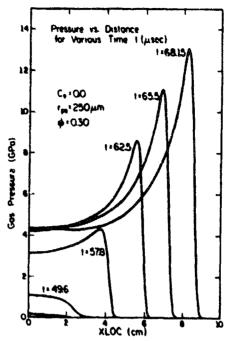


Fig. 3. Pressure history for completely confined accelerating deflagration.

At time t = 0, only 4 mm of the bed is assumed ignited at an initial low pressure of 1 MPa. The results show that within 70 µsec a detonation is about to form and the peak pressure (at the 9 cm location) is almost 14 GPa (140 kbar = 2 x  $10^6$  psi). The detonation (CJ) pressure for this overall density ( $\rho_{\phi}$ ) explosive is only somewhat greater than this value.

Of course this result is greatly dependent on the assumed particle size, d<sub>pe</sub>. If the particles averaged out to be even smaller, the gas pressure

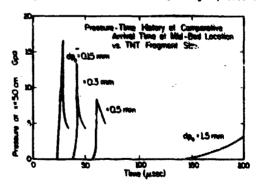


Fig. 4. Pressure-time profiles for varying size propellant particles.

shock would form even somer. Figure 4 shows the pressure-time profile at the bed midpoint,  $(x=5\,\text{cm})$  for four different average particle diameters. (The results shown in the previous figure, Fig. 3, assumed  $d_1=1/2$  mm.) When the average fragment diameter exceeds approximately 1 mm the resultant pressures will be approximately too low to allow a detenation.

too low to allow a detenation. The effect of even a small crack which can relieve the pressure and weaken the developing deflagration front is significant, as shown in the results presented in Figure 5. There, only one "hole", 4 mm in length, located at  $\chi_0/L=1/4$ , with an "opening ratio",  $C_0=1/2$  is considered. The mass loss is evident in the indented pressure profiles at the hole site.

The reduction in peak pressure, at the bed midpoint is also severe, depending on the crack opening ratio,  $C_0$ , as is shown in Figure 6, where the pressure-time history predictions are compared.

The effect on the rate of deflagration as C<sub>0</sub> is increased is evident in the results shown in Figure 7. Again, only one hole is assumed, located at  $\chi$  = 2.5 cm. Note that the slope of the flame-front location versus time locus, which is the reaction front speed, has reduced the detonation front velocities, (those evaluated at x = 8 cm) from 5.3 mm/ µsec (C<sub>0</sub> = 0) to 4.3 mm/ µsec (C<sub>0</sub> = 1/2), a 19% reduction.

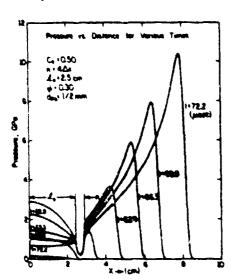


Fig. 5. Pressure history for packed bed with hole at x = 2.5 cm ( $C_0 = 0.50$ )

Extending the size (length) of the creck [from the value of 4 mm (M = 0.04) considered in the results shown in the previous two figures] to 0 mm and 16 mm has an even more pronounced eifect on reducing the pressure front development.

Figure 8 shows the comparisons. Note the crack opening ratio,  $C_0$  is only 0.10, 1/5 the value considered in earlier calculations shown in Figure 5.

More importantly there is a marked reduction in the speed of the detonation front, as can be seen in the comparison shown in Figure 9. For the condition of M = 0.16 (a 16 mm long crick) one obtains the speed of only 2.7 mm/ $_{\rm MS}$ ec., a velocity that could be interpreted to be a "low-order" detonation.

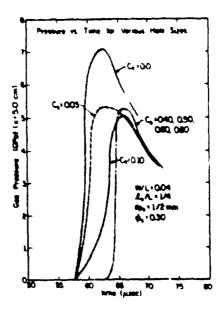


Fig. 6. Effect of hole size on pressure-time history at x = 5.0 cm.

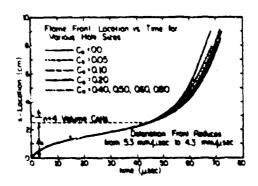


Fig. 7. Reduction in flame front welecity due to increased hole size.

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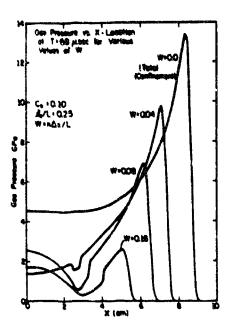


Fig. 8. Effect of hole size on pressure development (t-68 usec )

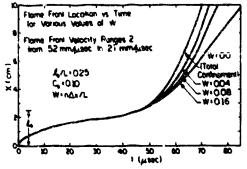


Fig. 9. Flame front velocity for varying hole sizes.

# Erupting West Holes

A final set of calculations considered an alternate constraint. Instead of prescribing in advance the location, length and the opening ratio of the vent holes, the opening is not assumed to take place until some critical pressure,  $P_{\rm grade}$ , is attained. Figure 10 shows the pressure development history when  $P_{\rm grade}=0.5$  GPa (5 kber). That is, when the "htternal pressure reaches 0.5 GPa, a "vent hole" occurs instantly to relieve the pressure. We have specified for this hole that  $C_{\rm m}=0.10$  and M=AM/L=0.01. The

pressure reductions caused by the mass, mammentum and energy losses are significant for this particular case.

While the oscillations in the weveforms of the P vs R plot for this case may appear to be caused by numerical instabilities. they are actually being caused by the intermittent rupturing of the propellant casing caused by bed areasurization. Each trough on a particular waveform represents a point along the propellant bed where the casing was ruptured due to high prassure at some time during the burn, while each neak represents a location where the casing did not rupture. One can note that as a perpondicular is dropped to the abscissa from a peak (or trough) on any waveform, all waveforms passing by that perticular poin: in the bed wil: also exhibit a peak (or trough). This is of course due to the fact that once the rupturing pressure is exceeded at any point along the bed, a hole forms in the casing at that time and remains for all subsequent time thereafter. To further insure that these oscillations were not caused by numerical instability, these calculations were repeated utilizing a time step. At , equal to one-helf the previous time step. The results were identical.

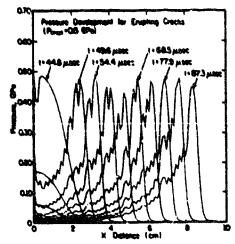


Fig. 10. Pressure history for shell rupture at P = 0.5 &Pa.

Figure 11 again shows the locus of deflagration fronts as a result of the pressure history shown in the previous figure. Note that if the internal pressure can repture the case at pressures less than 1 GPa the result (at t = 70  $\mu sec$ ) is a "low-order detonation", moving to D < 2 mm/ $\mu sec$ . Also shown in Figure 11 is the locus of the erupting vent holds which occur about 5 to 10  $\mu sec$  after the reaction front has passed. Obviously, internal pressures can more easily r viture an already damaged werhead case, so that the results shown in Figures 10 and 11 may not necessarily be unreasonable. Additional

calculations in which the "size" of the erupting holes are increased show the expected result of "quenching" the detonation wave that would have resulted had there been total confinement.

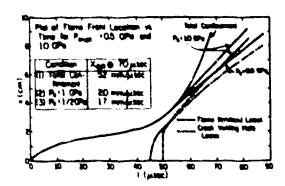


Fig. 11. Flame-front velocity and venting-hole locus for shell rupture at P = 0.5 GPa and P = 1.0 GPa.

# Concluding Remarks

The results presented in the last section verify the fact that a frecture of the exterior casing of a GP warhead with breakup of the explosive can reduce the effectiveness of the explosive filling. Cases were presented where the accelerating flame propagates through (a) a shell casing intact, (b) a shell casing which has fractured due to ground impact, and (c) a shell casing which has fractured due to localized internal pressurization.

Given the proper surface-to-volume ratio of the totally confined explosive, pressures exceeding 10-15 GPa can be predicted as the ignition front propagates through the porous explosive bed. However, when the shell casing is epsned and product gases are allowed to escape, the overall pressure profiles are greatly reduced.

The final cases presented in this paper modeled a casing fracture occurring at a prescribed stress on the exterior walls. Future work on this problem should couple the stress mechanics of the encasing structure with the applied stresses caused by the burning explosive grains.

A final point which should be discussed deals with the one-dimensional analysis made to simplify the numerical model. Given the proper computer resources, a detailed two-dimensional analysis would probably lead to canclusions which are lost in the CAR-dimensional version.

Our engoing work will also include enalysis

# which will consider:

- (e) Strong shock initiation (at x = 0), instead of weak shock flame initiation now assumed.
- (b) Variation in the axial (gropagation) direction of particle size and/or bed parosity.
- (c) Coupling of internal pressures to case wall stresses in order to predict actual time delays prior to fracture of the case.
- (d) A two-dimensional deflegration to detenation transition model, as proviously mentioned, which will allow for more accurate side vent loss calculations.
- (e) Variations in explosive chemical and physical properties.

# References

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PREDICTING RESPONSE OF HUNITIONS TO MASSIVE SECONDARY FRAMMENT IMPACT
A Proposed Analytical Method

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# ABSTRACT

This paper presents an analytic method for studying the mechanisms that lead to the detonation of cased munitions filled with moltan explosives when impacted by large concrete fragments, representing falled well sections. This is a single degree of freedom dynamic structure; analysis method which makes use of predetermined, nonlinear load-deflection characteristics of the shell casing. In the analysis described, the method was applied to predict the pressuretime history in the moltan explosive when subjected to impact. A reasonable comparison between analytic and experimental results was obtained.

#### INTRODUCTION

At one state of the munition production process, molten explosives are poured into empty shell casings. At this, and most stages of the production process there is a finite probability that an accidental explosion may occur. To limit the propagation of an accidental explosion, the pouring area is subdivided into smaller areas separated by reinforced concrete wells. This does not completely eliminate the danger of propagation because an explosion in a cubicle can cause some oreakup of dividing wells, producing energized frequents which may impact shell casings in neighboring cubicles thus possibly producing additional detenations. Whether or not an explosion is produced by such impact depends on the explosive, which in turn depends on the mass of the impact, which in turn depends on the mass of the impacting frequent, its impact velocity, point and angle of the impact, etc. The size of frequents produced by a separation well depends on the physical characteristics of the well, i.e. reinforcement details, concrete strength, aggregate size, thickness, span, support conditions, etc. It also depends on the intensity and distribution of the blast load produced by the donor charge on the dividing well.

This paper describes a project (Ref. 1) whose objective was to study the smethanisms controlling

the impact sensitivity of shell casings filled with molten explosives when impacted by secondary fregments. (It was determined in earlier experimental investigations that a shell in the molten or just-poured state was more sensitive to initiation than when the explosive was cool and hardened). The project was jivided into two parts.

The first part was an analytic effort whose purpose was to predict the pressure buildup within the molten explosive when the casing and the contained explosive interact with a secondary fregment. It is hypothesized that pressure buildup (or the rate of pressure buildup) and the resulting rise in temperature is a good measure of explosive detonation sensitivity.

The second part was an experimental effort whose aim was to ascertain the credibility and accuracy of the analysis. Instrumented, full scale experiments were performed to obtain quantitative data for comparison with analytic results. The experiments also provided an insight into what was occurring during the impact process and thus helped guide the analysis.

AMALYSIS OF SHELL EXPLOSIONS DUE TO IMPACT BY LARGE CONCRETE FRAMERITS

Figure 1 is a schemetic showing the shell-frequent configuration analyzed. The shell casing, open at its apex and completely filled with molten explosive, is stationary on the ground plane. At the time of impact the explosive is at a sufficiently high temperature to be in a liquid state. The fragment, a concrete cylinder, is moving in a horizontal direction with velocity. V. The conditions are assumed to be such that during impact the shell casing will be plastically deformed and will experience an acceleration. The plastic deformation of the casing will cause the molten explosive to be pressurized and to be forced to flow up and through the filling orifice at the apex of the casing. This pressure buildup during the time of impact and the associated temperature rise, is hypothesized to be a measure for detarmining if the explosive will detonate. The analytic procedure used to obtain the pressuretime relationship in the explosive during impact is described next.

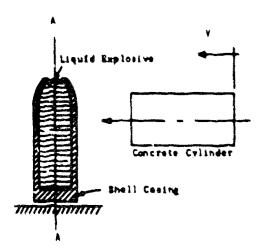


FIG. 1. - Shell-Frequent Configuration

# Analytic Solution Apoulrements

The analytic solution is a single-degree of freedom dynamic analysis which requires certain postulated explosive, shell casing, and frequent interaction characteristics which are the following:

- Force-deflection characteristics (resistance function) of the shell casino
- function) of the shell casing 2. Yolume versus deflection characteristic of the shell casing
- 3. Orifice area versus deflection characteristics

for the purpose of determining the forcedeflection characteristics, the shell casing was assumed to be restrained in the horizontal direction only, all along the line formed by the intersection of the midplane of the shell surface and the vertical plane whose edge view is indicated by line A-A in Fig. 1. Making use of the shell symmetry, one quarter of the shell surface is modeled for finite element analysis as shown in Fig. 2. Thickness is veried along the height in discrete intervals. ARSYS (Ref. 2) finite element computer program which meets the requirements of large deflection and plastic deformation of the casing material, was used in the analysis. Forcedeflection characteristics were obtained by imposing deflections and them computing the corre sponding forces required to produce them. Deflections were imposed on the shell casing at nodes representing an area approximately equal to the contact area between the casing and the impacting concrete cylinder. Load deflection characteristics were determined for three pressures applied to the interior of the shell. Results are shown in Fig. 3. Along with force-deflection characteristics of the shell casing, volume-deflection and orifice area-deflection characteristics were obtained from this analysis. These results are shown in Fig. 4 and Fig. 5 respectively. It will be noted that both of these characteristics are independent

of internal pressure. Also, at least for this shell casing, there was essentially no change in the orifice area with change in deflection, see fig. 5.

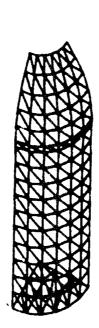


Fig. 2.-Finite Element Mesh of One Quarter of the Shell

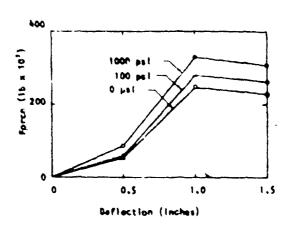


FIG. 3.-Force Versus Deflection Characteristics of the Shell Casing for Indicated Internal Pressures

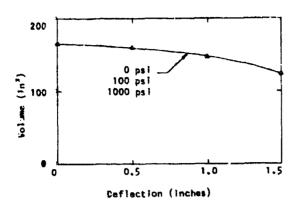


FIG. 4.-Volume Versus Deflection Characteristic of the Shell Casing

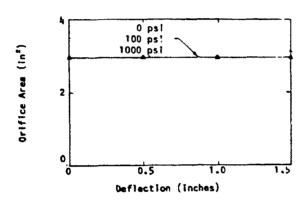


FIG. 5.-Grifice Area Versus Deflection Characteristic of the Shell Casing

Next, we were concerned with the flow characteristics of the molten explosive through the filling orifice of the casing. The flow is dependent on the orifice area, the fluid pressure, viscosity and the orifice coefficient. The following formula (Ref. 3) was used to relate the flow rate, Q to the internal pressure, p of the liquid explosive and other parameters.

$$Q = C_c A \sqrt{2gp/\gamma}$$
 (1)

where  $C_{\rm c}$  = the orifice coefficient, taken as 0.64

- the orifice area

acceleration due to gravity weight density of the molten explosive, taken as approximately 85 lb/cu ft

Flow characteristics are shown in Fig. 6 for three orifice areas.

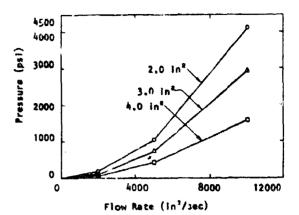


FIG. 6.-Pressure Versus Flow Rate for Three Orifice Areas

In the initial analysis it was assumed that the molten explosive was incompressible. Analytic results using this assumption showed large rapid changes in the liquid explosive pressure, suggesting compressibility. The analysis was modified to take into account fluid compressibility. In the modified analysis the characteristics shown in Fig. 6 are still used, however the corresponding internal pressure is modified on the basis of the bulk modules of the explosive, i.e.

$$B = \rho \frac{\Delta p}{\Delta \rho} \qquad . \tag{2}$$

where B = the bulk modulus taken as 580,000 psi

p = the weight density of the molten explosive

Ap = change in internal pressure

#### Analytic Solution Procedure

As indicated earlier, the analytic solution is a single-degree of freedom analysis. Referring to Fig. 1, assuming that the concrete cylinder and the shell move in a straight line, the equations of motion and initial conditions are given as follows:

$$M_{c} \chi_{c}^{*} = -F \tag{3}$$

$$N_S N_S = F \tag{4}$$

where Mc and Ms represent the mass of the cylinder and the shell casing respectively. F is the inter-action force between the shell and the concrete cylinder, and  $\dot{x}_c$  and  $\dot{x}_s$  are the center of gravity accelerations of the concrete cylinder and the shell respectively.

The initial conditions for the concrete cylinder and the shell are (at t=0, impact is initiated)  $x_c$ ; the initial velocity of the cylinder is equal to  $v_1$ ,  $v_2$ , the initial velocity of the shell is equal to zero. The initial displacements  $x_{\rm C}$  and  $x_{\rm S}$  , of the cylinder and the shell are equal to zero. Euler equations were used in the integration process, i.e.

$$\dot{x} (t + \Delta t) = \dot{x}(t) + \dot{x}(t)\Delta t$$

$$x (t + \Delta t) = x(t) + \dot{x}(t)\Delta t$$

(6)

(5)

The solution procedure is detailed below.

#### Solution Procedure

- Read data describing the system
- Set time to zero (t=0) and displacements and velocities to their initial values. Set initial invernal pressure to zero, and the orifice area and the casing volume to the initial values.
- Print out time and pressure
- If time exceeds maximum value, stop.
- From force-deflection-pressure curves (Fig. 3) determine the interaction force, F. Note that the casing deflection 6, is the difference in the cylinder and shell motions
- (displacements), i.e.  $\delta = x_c x_s$ .

  6. Compute cylinder and shell accelerations, see
- equations (3) and (4).

  7. Use the Euler integration formulas. expressions (5) and (6), to determine velocities and displacements of the cylinder and the casing at time  $t + \Delta t$ . Update time to t + At.
- Determine shell casing volume using volume-deflection-pressure curve (Fig. 4). Compute volume rate of flow from difference in volume from previous time step divided by time step.
- 9. Determine orifice area from orifice areadeflection-pressure curves (Fig. 5).
- 10. Determine new internal pressure from pressure-volume flow rate-area curves (Fig. 6).

Steps 11 through 13 represent an iterative procedure used to take into account the compressibility of the liquid explosive.

- 11. Determine the change in pressure over the time step at and compute the change in the weight density of the liquid explosive, see Eq. (2),
- 12. Determine the new weight density.
- 13. Determine the change in volume due to the change in the weight density. Compute the volume rate of flow.

Continue the iteration until the change in volume is smaller than a preassigned value.

14. Return to step 3 and continue.

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#### EXPERIMENTAL EFFORT

The purpose of the experimental effort was to measure the pressure-time history within the molten explosive when the shell containing it is impacted by a concrete fragment. The experimental setup is depicted in Fig. 7. A shell casing, containing a liquid, Glycerol, of the

same density as moltan composition B explosive is mounted (propped) on a pedestal, see "target" in Fig. 7. An air gun is then used to launch the concrete fragment at the shell casing to impact at a specified aiming point. The concrete fragment is in the shape of a cylinder. Two-sizes and weights were used in this study (Ref. 1), 2-ft and 4-ft long and weighing 200-lbs and 400-lbs respectively. The instrumentation consisted of a pressure sensor located within the liquid for measuring the pressure-time history during impact. Photographic coverage was provided to measure the impact velocity of the concrete cylinder.

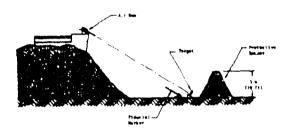


FIG. 7.-Secondary Fragments Impact Test Site

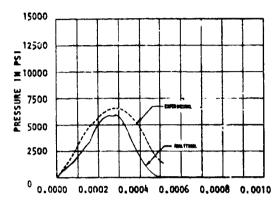
## Selected Results

Figure 8 shows an experimentally determined and the corresponding analytic pressure-time history. This particular experiment dealt with a 4.2-in. mortar shell filled with Glycerol and water at ambient temperature. A concrete cylinder, simulating a wall fragment and weighing 200 lbs., impacted the shell at 272 ft/sec at a point 4.25 in below the filling orifice. In terms of the shape of the pressure-time history, duration and peak pressure, the comparison between experimental and analytic results appears to be favorable. Similar comparisons were obtained for other experiments conducted in the course of the study.

## CONCLUSIONS AND RECOMMENDATIONS

A simple analytic method was formulated for predicting pressure-time histories in shell casings filled with molten explosives when impacted by secondary fragments. Analytic results compared favorably with experiments.

Additional analyses are required to study the sensitivity of results for a larger set of experi-ments with the objective of improving the accuracy of the predictive method. To date four other experimental programs have been conducted on the sensitivity to impact, by large concrete fragments, of a variety of molten and ambient temperature explosive-filled shells. For these previous experimental programs analytical predictions of time curves should be performed. With a larger number of curves, and hence larger number of test conditions, one would be able to distinguish between pressure-time conditions for explosion and no reaction. The scope of this method needs to be further expanded to study whether the peak pressure in the liquid explosive, rate of pressure rise, etc. are parameters which individually or in combination will predict the onset of detonation.



TIME IN SECONDS

FIG. 8.-Pressure Versus Time Graph for Experiment 4 (Concrete Projectile 200 lb. at 272 ft/sec Velocity)

# **ACKNOWLEDGMENT**

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MICROPLANE HODEL FOR FRACTURE ANALYSIS
OF CONCRETE STRUCTURES

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#### ABSTRACT

Dynamic fracture analysis of concrete structures necessitates a triaxial stress-strain relation that describes gradual strain-softening with reduction of tensile stress to zero. A new model which does that and is applicable under general loading, including rotating principal stress directions, is proposed. It is based on accusulating stress relaxations due to micro-cracking from the planes of all orientation within the microstructure. Comparisons with tensile test data are given.

#### Introduction

Fracture analysis of certain brittle haterogeneous materials, such as concretes and many rocks, requires consideration of progressive microcracking in the fracture process some as the fracture is being formed. This type of fracture may be efficiently modeled with the crack band approach, in which the material behavior in the fracture process some is described by a strain-softening triaxial stress-strain relation, provided that the strain-softening behavior is associated with a some of a certain characteristic width that is treated as a material property or is determined in advance by stability analysis. A suitable triaxial stress-strain relation of the total strain type (deformation theory type) has been recently formulated and has been shown to lead to satisfactory agreement with essentially all existing fracture test data available in the literature [1, 2]. This stress-strain relation is, however. limited to situations in which the direction of the maximum principal stress does not significantly rotate during the fracture formation. This is not so in certain important situations, especially various dynamic problems. Here, a longitudinal wave may produce only a partial tensile fracture (i.e., distributed microcracking) and the fracture may be completed subsequently when a shear wave arrives, causing a principal tensile stress in a different direction. For such situations of progressive fracturing, it is necessary to develop a triaxial strain-softening atress-strain relation which is path-dependent and is formulated incrementally. A model called microplane model is de veloped to fill this need. We propose here a model in which the constitutive pronerties are characterised by a relation between the stresses

and strains acting within the microstructure on planes of various orientation, called the microplanes. This formulation involves no tensorial invariance restrictions. The restrictions can then be satisfied by a suitable combination of planes of various orientation. E.g., in the case of isotropy, each orientation must be equally frequent. Thus, one circumvents the difficulty of setting up a general nonlinear constitutive equation in terms of proper invariants.

The idea of defining the inelastic behavior independently on planes of different orientation within the material, and then in some way superimposing the inelectic effects from all planes, appeared in Taylor's work [3] on plasticity of polycrystalline metals. Batdorf and Budienski [4] formulated the slip theory of plasticity, in which the stresses acting on various planes of slip are obtained by resolving the macroscopic applied stress, and the plantic strains (slips) from all planes are then superimposed. The same superposition of inelastic strains was used in the socalled multilaminate models of Zienkievics et al. [5] and Pande et al [6, 7] and in many works on planticity of polycrystals. While the previous works dealing with plasticity of polycrystals [3, 4, 8, 9, 10-14) or soils [15,16] the atresses on various microplanes were assumed to be equal to the resolved macroscopic stress, this new model uses a similar assumption for part of the total strains.

## Fundamental Hypotheses

The resultants of the stresses acting on the microplanes over unit areas of the macroscopic continuum will be called the microstresses  $\mathbf{s}_{ij}$ , and the strains of the macroscopic continuum accumulated from the informations on the microplanes will be called the microstrains,  $\mathbf{e}_{ij}$ . With regard to the interaction between the micro-and macro-levels, one may introduce the following basic hypotheses.

<u>Hypoteheis I.</u> - The tensor of macroscopic strain,  $\epsilon_{ij}$ , is a sum of a purely elastic mecrostrain  $\epsilon_{ij}^{a}$  that is unaffected by cracking, and an inelastic macrostrain  $\epsilon_{ij}$  which reflects the stress relaxation due to cracking, i.e.,

$$c_{ij} = c_{ij}^{a} + e_{ij} \tag{1}$$

Here, latin lower case subscripts refer to cartesian coordinates  $\mathbf{x}_i$  (i = 1,2,3).

Hyp-sthesis II. - The normal microstrain en which governs the progressive development of cracking on a microplane of any orientation is equal to the resolved macroscopic strain tensor en for the same plane, i.e.,

$$\mathbf{e}_{\mathbf{n}} = \mathbf{n}_{\mathbf{i}} \ \mathbf{n}_{\mathbf{j}} \ \mathbf{e}_{\mathbf{i}\mathbf{j}} \tag{2}$$

in which  $n_i$  = direction cosines of the unit normal  $\vec{n}$  of the microplane and the repeated latin lower case subscripts indicate a summation over 1, 2, 3.

Hypothesis III. - The stress relaxation due to all microcracks normal to  $\vec{n}$  is characterised by assuming that the microstress  $\mathbf{e}_n$  on the microplane of any orientation is a function of the normal microstrain  $\mathbf{e}_n$  on the same plane, i.e.,

$$s_{K} = (2\pi/3) \ \mathbb{P}(s_{n})$$
 (3)

The factor  $(2\pi/3)$  is introduced just for convenience, as it will later cancel out.

The last hypothesis is similar to that made for shear microstresses and microstrains in the slip theory of plasticity. Hypothesis II is however opposite. There are three reasons for hypothesis II.

- 1. Using resolved stresses rather than resolved strains on the microplanes would hardly allow describing strain-softening, since in this case there are two strains corresponding to a given stress but only one stress corresponding to a given strain.
- The microstrains must be stable when the macrostrains are fixed. It has been experienced numerically that, in the case of strain-softening, the model becomes unstable if resolved stresses rather than strains are used.
- 3. The use of resolved strains rather than resolved atresses seems to reflect the microstructure of a brittle aggregate material more realistically. The use of resolved stresses is reasonable for polycrystalline metals in which local slips scatter widely while the stress is roughly uniformly distributed throughout the microstructure. By contrast, in a brittle aggregate material consisting of hard inclusions embedded in a weak matrix, the stresses are far from uniform, having sharp extremes at the locations where the surfaces of aggregate pieces are nearest. The deformation of the thin layer of matrix between two aggregate pieces, which yields the major contribution to inelastic strain, is determined chiefly by the relative displacements of the centroids of the two aggregate pieces, which roughly correspond to the macroscopic strain. The microplanes may be imagined to represent the thin layers of matrix and the bond planes between two adjacent aggregate

pieces, since microcracking is chiefly concentrated there.

In Hypotehsis III, the relaxation of shear microstresses a caused by the shear and normal microstrains e and e is neglected. This assumption is probably quite good for very small crack openings, since it has been deduced from test data on shearing of cracks in concretes that no relative shear displacements on the rough interlocked cracks is possible before a certain finite crack opening is produced, and that the shear stiffness of the cracks decreases rather slowly as the crack gradually opens. One must admit, however, that Eq. 3 (Hypothesis III) is also justified by its simplicity. It would be much more complicated to assume a general relation between the normal and shear microstresses and microstreins on each plane.

#### Tangential Stiffness Matrix

The virtual work of streams per unit volume may be written, according to Eq. 1, as  $\delta W = \sigma_{ij} \ \delta \epsilon_{ij} = \sigma_{ij} \ \delta \epsilon_{ij}^a + \sigma_{ij} \ \delta \epsilon_{ij}^a$ . Summing the virtual work due to  $\delta \epsilon_{ij}^a$  and  $\delta \epsilon_{ij}$ , we further have  $\delta W = \sigma_{ij}^a \ \delta \epsilon_{ij}^a + \epsilon_{ij} \ \delta \epsilon_{ij}^a$ , in which  $\epsilon_{ij}$  is the macrostress tansor resulting from  $\epsilon_{ij}$  on all planes, and  $\sigma_{ij}^a$  is the stress tensor corresponding to  $\epsilon_{ij}^a$ . Since both expressions for  $\delta W$  must hold for any  $\delta \epsilon_{ij}^a$  and any  $\delta \epsilon_{ij}^a$ , we must have  $\epsilon_{ij}^a = \sigma_{ij}^a = \sigma_{ij}^a$ .

Equilibrium conditions may be expressed by means of the principle of virtual work:

$$\delta \mathbf{w}^{c} = \frac{4}{3} \times \sigma_{ij} \delta \mathbf{e}_{ij} = 2 \int_{S} \mathbf{e}_{n} \delta \mathbf{e}_{n} f(\mathbf{n}) dS$$
 (4)

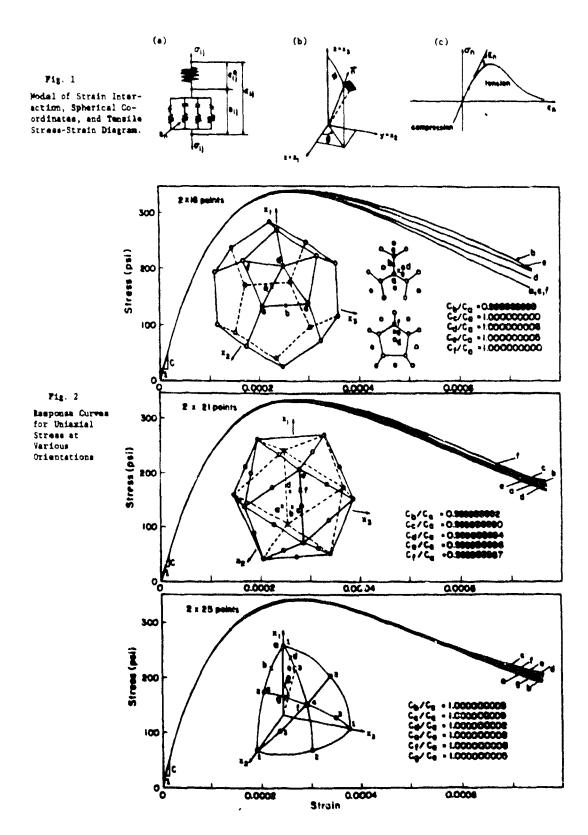
in which S represents the surface of a unit hemisphere, the factor  $(4\pi/3)$  is due to integrating over the surface of a sphere of radius 1, and dS = sined0d $\phi$  (Fig. 1b). Note that we do not need to integrate over the entire surface of the sphere, since the values of  $\sigma_n$  or  $\sigma_n$  are equal at any two diametrically opposite points on the sphere. Function  $f(\vec{n})$  defines the relative frequency of the planes of various orientations  $\vec{n}$ , contributing to inelastic atrees relaxation.

Substituting Eqs. 2-3 into Eq. 4, we get  $\sigma_{ij}$   $\delta e_{ij} = \int_{\mathbb{R}} F(e_n) \ n_i \ n_j \ \delta e_{ij} \ f(n) \ dS$ , and because this must hold for any  $\delta e_{ij}$ , we must have

$$\sigma_{ij} = \int_{0}^{2\pi} \int_{0}^{\pi/2} \mathbf{F}(\mathbf{e}_{\mathbf{n}}) \, \mathbf{n}_{i} \, \mathbf{n}_{j} \, \mathbf{f}(\mathbf{n}) \, \sin\phi \, d\phi \, d\theta \qquad (5)$$

Furthermore, according to Eq. 2,  $dF(e_n) = F'(e_n)de_n = F'(e_n)n_k n_k de_{km}$ , and thus differentiation of Eq. 5 finally yields

$$d_{ij}^{c} = D_{ijkm}^{c} d_{km}$$
 (6)



in which
$$D_{ijkm}^{c} = \int_{0}^{2\pi} \int_{0}^{\pi/2} a_{ijkm} F'(e_n) f(\vec{n}) \text{ ein} d\phi d\phi, \text{ with}$$

$$a_{ijkm} = n_i n_j n_k n_m$$
(7)

 $D_{ijkm}^{C}$  may be called the tangent stiffnesses of the microplane system. Note that the sequence of subscripts of  $D_{ijkm}^{C}$  is immaterial; therefore, there are only six independent values of incremental stiffnesses. Eq. 7 applies to initially anisotropic solids. For isotropic solids, we may substitute  $f(\vec{n}) = 1$ .

The mathematical structure of the present model may be goomstrically visualised with the rheologic model in Fig. 1a.

The compliance corresponding to the additional elastic strain  $\sigma^a_{ij}$  must estisfy isotropy conditions, and so

$$C_{ijkm}^{a} = \frac{1}{9k^{a}} \delta_{ij} \delta_{km} + \frac{1}{2c^{a}} (\delta_{ik} \delta_{jm} - \frac{1}{3} \delta_{ij} \delta_{km})$$
 (8)

in which  $K^R$  and  $G^R$  are certain bulk and shear raduli which cannot be less than the actual initial bulk and shear moduli K and G. For fitting of test data, it was assumed, with success, that  $1/G^R = 0$ .

Recalling Eq. 1 (and Fig. 1s), we may now write the incremental atress-strain relation as

$$d\sigma_{ij} = D_{ijkm} dc_{ij}, with [D_{ijkm}] = [(D^{c-1})_{ijkm} + (C^{a}_{ijkm})]$$
(9)

Applying Eq. 7 to elastic deformations (with f(n)=1), one finds that the matrix in Eq. 7 always yields Poisson's ratio  $\nu=1/4$ . This is because the slips on all microplanes are neglected. Since  $\nu=1/4$  is not quite true for concrete, the additional elastic strain must be used to make a correction. Let us now determine the value of K needed to achieve the desired Poisson's ratio  $\nu$ . Let superscripts c and a distinguish between the values corresponding to  $\frac{B^n}{13 \, \mathrm{km}}$  and  $C^n_{13 \, \mathrm{km}}$ . For uniaxial strang we have  $c_{11} = \sigma_{11}/9K^n + \sigma_{11}/K^n$  and  $c_{22} = \sigma_{11}/9K^n - \nu^n \sigma_{11}/K^n$  in which  $\nu^n = 1/4$  and  $\kappa^n = 2\nu E_n/5$ ,  $\kappa^n = F^n(0) = initial normal$  stiffness for the microplane. Since  $c_{22} = -\nu c_{11}$ , we must have

$$R^{a} = \frac{1+v}{9(v^{c}-v)} g^{c}$$
 (for  $v \in v^{c}$ ) (10)

This is, of course, under the assumption that  $1/G^2 = 0$ .

The atress-strain relation for the microplanes, relating  $\sigma_{\rm m}$  to  $\varepsilon_{\rm m}$ , must describe cracking all the way to complete fracture, at which  $\sigma_{\rm m}$  reduces to zero. In view of the kinematics visualized in Fig. 1b, it is clear that  $\sigma_{\rm m}$  as a function of  $\varepsilon_{\rm m}$  must first rise, then reach a maximum, and their gradually decline to zero. We choose the final zero value to be attained asymptotically, since  $\pi \sigma$  practice information emists on the final strain at which  $\sigma_{\rm m}=0$ , and since a smooth curve is convenient computationally. The following expressions were used in computations [19] (Fig. 1c);

for 
$$c_n > 0$$
:  $\sigma_n = E_n e_n e_n^{p}$ ,
for  $c_n \le 0$ :  $\sigma_n = E_n e_n$  (11)

in which  $E_n$ , k, and p are positive constants; k = 1.8 x 10<sup>7</sup> n = 2.

The integral in Eq. 7 has to be evaluated numerically, approximating it by a finite sum:

$$D_{ijkm}^{c} - \sum_{\alpha=1}^{N} v_{\alpha} [a_{ijkm} F^{*}(e)]_{\alpha}$$
 (12)

in which a refers to the values at certain numerical integration points on a unit besimphere (i.e., certain directions), and  $\mathbf{v}_{\mathbf{q}}$  are the weights associated with the integration points.

Since in finite element programs for incremental loading the numerical integration needs to be carried out a great number of times, a very efficient numerical integration formula is needed. For the slip theory of plasticity, the integration was performed using a rectangular grid in the 6-4 plane. This formula is, however, computationally inefficient because the integration points are crowled near the poles, and also because in the 6-4 plane the singularity arising from the pole takes away the benefit from a use of higher-order integration formula.

Optimally, the integration points should be distributed over the spherical surface as uniformly as possible. A perfectly uniform subdivision is obtained when the microplemes normal to the u-directions are the mides of a regular polyhedron. A regular polyhedron with the most sides is the icombedron, for which H = 10 (belf the number of sides). Such a numerical integration formula was proposed by Albrecht and Collatz [18].

Numerical experience revealed, however, that 10 points are not enough when strain-softening takes place; it was found that the strain-softening curves calculated for uniaxial tensile strasses oriented at various angles with regard to the additections significantly differ from each other, even though within the strain-hardening range the differences are angligible. Therefore, more than 10 points are needed, and then a perfectly unifor:

Table 1 - Direction Comines and Weights for 2 x 21 Points (Orthogonal)  $O(h^{\frac{1}{2}})$ 

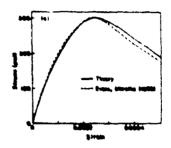
•	x,	x <sub>2</sub>	x <sub>a</sub>	y.ª
1	1	0	0	0.07652141274
2	0	1	0	*
3	C	G	1	•
4	0.7071067812	0.7071047812	0	0.01993014153
3	0.7071067812	-0.7071067812	0	•
6	0.7071067812	0	0.7071067812	•
7	0.7071047812	0	-0.7071067812	*
	0	0.7071067812	0.7071067812	n
•	0	0.7071067812	-0.7071067812	•
0	0.3879072746	0.3879072746	0.8360936240	0.02507124272
1	0.3879072746	0.3879072746	-0.8360936240	•
2	0.3879072746	-0.3879072746	0.8360936240	Ħ
3	0.3879072746	-0.3879072746	-0.8360936240	**
4	0.3879072746	0.8360956240	0.3879072746	*
15	0. 3879072746	0.8340934240	-0.3879072746	*
6	0.387907274%	-0.8360936240	0.3879072746	*
7	0.3879072746	-0.8360936240	-0.3879072746	<b>#</b>
18	0.8360936240	0.3879072746	0.3879072746	#
9	0.8360956240	0.3879072746	-0.3879072746	#
to	0.8360936240		0.3879072746	•
21	0.8360956240	-0.3879072746	-0.3879072746	R

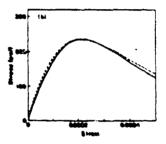
8 - 33.269905°

Table 2 - Direction Cominem and Weights for 2 x 25 Points:  $O(h^{1.0})$ .

a	z <sub>l</sub>	x <sub>a</sub>	x <sub>q</sub>	v <sup>a</sup>
1	1	0	0	0.01269841038
2	0	1	0	×
3	0	0	1	•
4	0.7071067812	0.7071067812	0	0.02257495612
5	0.7071067812	-0.7071067812	0	
6	0.7071067812	0	0.70/1067812	
7	0.7071067812	0	-0.7071067812	
8	0	0.7071067412	0.7071967812	•
•	0	0.7071067812	-0.7071067812	#
10	0.3015113354	0.3015113354	0.9045346396	0.02017333557
11	0.3015113354	0.3015113354	-0. 9045340398	-
12	0.3015113353	-0. 3013113354	0.9045340398	•
13	0. 3015113354	-0. 3015113354	-0.9045340398	*
14	0.3015113354	0. 9045340396	0.3013113344	*
15	0.3015113354	0.9043340366	<b>-0.301511335</b> 4	
16	0.3013113354	-0.9045340398	0. 3015113354	*
17	0.3013113354	-0.904534 <b>0396</b>	-0.3013113354	#
18	0.9045340398	0. 3015113354	0. 3015113354	•
19	0.9045340398	0. <b>30</b> 13113354	<b>-0.301</b> 5113354	•
20	0.9045340398	-0. 3013113354	0.3015113354	*
21	0.9045344396	-0. 3015113354	-0. 3013113334	*
22	0.57735C2692		0.5773502692	0.02109375117
23	0.5773302692	0.5773502692	-0.5773 <b>502</b> 592	
24	0.3773502692	-0.3773302692	0.3773 <b>3026</b> 92	•
25	0.3773302692	-0.5773502692	-0.3773502492	<b>A</b>

8 - 25.239401°





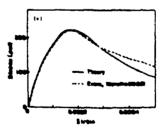


Fig. 3 Comparison with some of the Teat Data of Evans and Maratha (1968)

spacing of a- directions is impossible.

Balant and Oh (17) developed numerical integration formulas with more than 10 points, which give consistent results even in the strain-softoning range. The most efficient formulas, with a nearly uniform spacing of o-directions, are obtained by certain subdivisions of the sides of an icosahedron end/or a dodecahedron [17]. Such forsules do not exhibit orthogonal symmetries. Other formulas winch do were also developed [17] Taylor series expansions on a sphere were applied and the weights wa associated with the integration points were solved from the condition that the greatest possible number of terms of the Taylor series expansion would cancel out. The angular directions of certain integration points were further determined so as to minimize the error term of the expansion. Formulas involving 16, 21, 25, 33, 37 and 61 points were derived, with errors of 8th, 10th and 12th order [17]. Table 1 defines two of these numerical integration formulas, with 21 and 25 points, one without, and one with orthogonal symmetry. These formulas give accuracy that suffices for most pratical purposes. For crude calculations, a formula with 16 points [17] may sometimes also suffice. The directions of integration points are illustrated in Fig. 2. Also shown one stress-strain diagrams calculated with the formula for uniaxial tension in various directions with regard to the intergration points (directions a, b, c, d,...); the spread of the curves characterizes the range of error.

#### Numerical Algorithm

The following numerical algorithm may be used for the microplane model in each loading step.

- 1. Determine  $e_0^{(n)}$  from Eqs. 1 and 2 for all directions  $n=1,\ldots N$ . In the first iteration of the loading step, use  $\epsilon_{i,j}$  for the end of the previous step, and in subsequent interations use the value of  $\epsilon_{i,j}$  determined for the mid-step in the previous iteration. In structural analysis, respect this for all finite elements and for all integration points within each finite element.
- 2. For all directions  $R^{(n)}$ , evaluate  $F'(e_n)$  for use in Eq. 7. Also check for each direction whether unloading occurs, as indicated by violation of the condition  $s_n a_n \ge 0$ . If violated, replace  $F'(e_n)$  with the unloading staffness (which may be approximately taken as  $E_n$ ; however, a better empression exists.)
- 3. Evaluate Dink from Eq. 7 and Dink from Eq. 9. In structural analysis, repeat this for all elements ead all integration points in each element. Wher solving atress-strain curves, calculate then the increments of unknown straines and unknown strains from Eq. 9. In structural analysis, solve (by the finite element method) the increments of nodal displacements from the given

load increments, and subsequently calculate the increments of  $\mathbf{c}_{ij}$  and  $\mathbf{c}_{ij}$  for all elements and all integration points in each element. Then advance to the next iteration of the same loading step, or advance to the next loading step.

In simulating uniaxial tensile loading of fixed direction, the unloading cirtarion is not important since the only unloading occurs at moderate compressive stresses, for which a perfectly elastic unloading may be assumed.

The microplane model can be calibrated by comparison with direct tensile tests which cover the strain-softening response. Such tests, which can be carried out in a very stiff testing machine and on sufficiently small test specimens, have been performed by Evens and Maratha (20) as well as others [21-23]. Optimal values of the three parameters of the model, I, k, and p, have been found [19] so as to achieve the best fits of the data of Evans and Marathe. Some of these fits are shown as the solid lines in Fig. 3, and the data are shown as the dashed lines. A better test of the model would, of course, be a tensile test under rotating principal stress directions, but such tests have not yet been performed.

Note that with this theory, one has only two material parameters,  $\mathbf{E}_n$  and  $\mathbf{k}_n$  to determine by fitting test data. Trial and error approach is sufficient for that.

#### Conclusion

The microplene model is capable of simulating realistic tensile stress-strain curve with strain-softening and reduction of stresses all the way to sero. Combined with the blunt crack hand concept, in which the strain-softening is restricted to a region of a certain characteristic width that is a material property [1, 2], this model should give a realistic representation of fracture. The model is general and does not praclude application to stress histories in which the principal stress directions rotate. These features are particularly attractive for the analysis of the response of concrete structures subjected to dynamic loads.

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# A PLASTIC-FRACTURE MODEL FOR CONCRETE MATERIALS

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## ABSTRACT

Recent research in atructural concrete under static and dynamic loading has been moving toward the development of three-dimensional acress-acrain relatone based on the principles of plastias well as elesticity. Although city significant progress in this area has been made in recent years, no unified treatment of the various existing mathematical models of concrete has been attempted from which a comprehensive electic-plastic-fracture stress-strain relationship for memorate can be formu-This lated. unified approach attempted in the present work.

In this theoretical development, the five-parameter failure surface of Willam-Warnke model, the technique of mixed hardening for cyclic leading, the concept of cruehing coefficient and the dual criterion fortrushing, cracking, and mixed types of Tailue of concrete will be considered as the basis for this comprehensive development.

#### 1. INTRODUCTION

For the most part, analytical etu-of the nonlinear response of reipforced concrete etructures have been focused, by macassity, on the behavior of isolated simple structural elements each as beens and columns. As quantitetive information on the lead-deformation behavior of concrete developed and computing capability expanded, the scope of monlinear analysis has broadened to include such triaxially loaded concrete structures as flosting vesicle, offshore platforms, submerged ettactures, the usual land-based or underground containment vessels, prestressed concrete reactor vessels and dams. Although largescale finite-element software packages now have a wide range of applications in many areas of stress analysis, inade-quate material models are often one of the major factors in limiting a Structural enalysis. Thin is especially true for reinforced concrete, where basic characteristics of reinforced concrete materials do not exist. The problem of codaling the mechanical behavior of T. Y. P. Chang

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Akron, Ohio concrete for use in analytical studies of reinforced concrete, structures remains one of the most difficult challenges in the field of structural concrete engineering.

Current analysis procedures f or problems relaferced cencrata ander short-term leading are essentially eaeor two-dimensional. A common approach uses two concrete parameters: concrete sodulus and concrete fracture strength. Various empirical equations for thean have been established by curve fitting biexial-leading-test data. 8427 The best known of those expressions is probably either the one proposed by Liu, Nilson, and Slate, of Cornell University, or the sac proposed by Coratle ot al of the University of Co? .ado (see Ches, 1981). Their equivalent onetwo-dimensional approach is appealing because of its simplicity, its broad ite broad and the correlations that data bese, have been catablished between the concrete modulus and a variety of chacrete strength and strain characteristics. It is well known that these models are mainly applicable to pleast problems such as bears, panels, and thin shells, where the etrose is predeminantly biazial.

At present, multi-dimensional anslyses are usually made by taking the concrete to be incrementally elastic. Then this is done, Pelsson's ratio must defined. Neverer, it is not possible describe the three-dimensional giaris-asers behavior of concrete materials accurately in the framework of an incremental Hooke's law with variable moduli which are functions of the enzand/or strain imum stress levels. Retent research in structural concrete under static and dynamic leading has been moving toward the development of three-dimensional atress-strain relations beend on the principles of plasticity as woll as elasticity. Although work in this area has been done in recent years, as unified treatment of the various existing mathematical models of concrete has been made from which a comprehensive elastic-plastic-freeture etresu-strain relationship for concrete can be formulated. This unified unified approach is accompted in the present paper.

In this paper, empirical equations for modulus as fracture strongth under bioxial leading, ampirical expressions for bulk and sheat modelus under multioxisi stress states, erthetropic elastickty, perfect and work-hardening place .. .. , which have been treated individual technique in the mathematical nedeling of concrete behavior, are coneldered in relation to a common structure. Some of the inverrelationships between the empirical equations, slasting city, and pleaticity are exemined critically and synthesized in order to formulate a comprehensive elastic-pleatic-fracture etress-etrain relationship for teacrete. In particular, the five-perameter failure surface of Willem-Warnke model, the technique of mixed hardening for cyclic leadings, the einple concept of cruehing coefficient and the dual criteries for crushing type, the crecking type and the mixed type of failure of concrete are considered as the besie for this comprehensive development.

It is also expected that the fielte element three-dimensional enalysis pregram currently under development at Purdue University will be the foundation for a general purpose nonlinear reinferced concrete analysis, atcol-temprate interaction program. In this development, the comprehensive con-stitutive equations developed in the present work for concrete material will be implemented inco the computer code in the form of subroutines, which can be readily adopted by any monlinear finite element computer program in which the solution method to based on the incremental approach with a tangent modulus formulation for selving elesticplantic-fracture problems.

# 2. THE LITERATURE ON THE STATE-OF-THE-

No attempt will be made here to ruview the vest literature on the nathematical wodeling and monlinear analysis of reinforced concrete atructures. A comprehensive state-of-the-art submary on the constitutive modeling of reinforced concrete materials based on the theories of linear and nonlinear elasticity as well as the theories of perfect and work-hardening planticity together with their finite element applications is given in a recent comprehensive beak entitled "Planticity in Reinforced Concrete" by Chem (McGrow-Rill , 1981). Further, a comprehensive state-of-the-art review on

constitutive modeling of materials and finite-element amalysis of reinforced concrete structures with typical emacples of recent applications, together with an extensive list of references, and compilation of available computer programe in contained in the report of the AECE Committee (1982) on finite element analysis of reinferced concrete atructures (A. H. Hilson of Cernell University, Chairman). In perticular, the materials presented in Chapter 2 of the ASCR Report entitled "Constitutive Relations and Failure Theories by W.F. Chen (Chairman), 2.P. Bazant, O. Buyukosturk, T.T. Chang, D. Dervin, T.C.T. Liu and K.J. Willan provide a valuable source of information on state-of-the-art is t he current mathematical modeling of reinforced concrete materials. Detailed and extensive discussions of the three-dimensional elastic-plastic-fracture constitutive equations for concrete are given in the two references mentioned above and therefore will not be repeated here. Instead, a discussion of the particular features to be included in the present formulation of a comprehensive electicplantic-fracture atraca-strain relationship for concrete is given in the forthconing.

It is worth mentioning here that strong impetus to research in this general area has been the studies required for the dealgn of prestressed concrete reactor vessels. Note recent work in this area can be followed through the Proceedings of the International Conference on Structural Mechanics in Reactor Technology, published regularly since 1971. Special proceedings dealing with the nonlinear finite-element analysis of relaforced concrete structures have been published by IASS (1978), Politecaice di Milano (1978), and IABSE (1979). Most recent proceedings that have just been published are the two-velume IABER publication on "Advanced Mechanics of Reinforced Concrete" (Colloquium, Delft, 1981) and the Workshop on Constitutive Relations for Concrete held in Albu-querque, New Mexico, on April 28-29, 1981 spuncored and published by the Air Force Weapone Laboratory and the Hev Mexico Engineering Research Institute.

## 3. CONSTITUTIVE EQUATIONS FOR CONCRETE

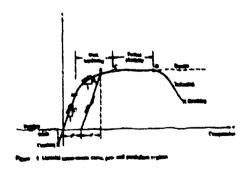
Concrete, like many other engineering materials, exhibits brittle behavior for tensils and small compressive strasses and becomes ductile in the presence of large hydrostatic pressures. It is therefore meaningful and convenient to seek yield criteria and plantic stress-strain relationships for contic

trate in the <u>dustile</u> state and to seek fracture criteria and atrees-atrain relationships for fractured concrete in the <u>brittle</u> state. These brittle and ductile models can then be combined to provide a proper description of the pro- and poet-failure behavior of concrete in the ductile-brittle state.

In the following, we expected the special features in formulating an electic-plastic-fracture model for the finite-elecet analysis of concrete structures. Based on the recent developments, we adopt the five-parameter fracture (or yielding) eritorion of Willem-Warnhe (1973) as the failure model for concrete. Isotropic electic and assectropic electic theories are applied for the description of the initial loading and the post-failure behaviors of concrete. A pleetic model displaying mixed hardening is used to describe the concrete behavior between the initial yielding and the fracture failure. Incremental atreas-strain teletionahips are then derived based on the essociated flow rule and mixed hardening rule of isotropic and Rimsuffic models. In the present development, three different types of failure modes are considered. A simple cruching coefficient is defined based on a dual criterion to identify the cruching type, the crecking type and the mixed type of failure. Detaile of this development are given in the forthcoming.

#### 3.1 Blastic-Plactic-Fracture Hodel

Different stages of the 3-D model mentioned above can be illustrated schematically in a typical uniaxial stress-strain curve for a plain concrete shown in Fig. 1.



For tensile failure, the behavior is essentially linearly electic up to failure lead, the .Aximum etreesed ceimcide with the manimum etrains, and as plastic strains eccur at the failure mement. For compressive failure, the material initially exhibite almost linear behavior up to the proportional limit at point A, after which the material is progressively weakened by internal microcracking up to the end of the perfectly plastic flow region CD at point B. The nonlinear deformations are basically plastic, as one malestically plactic, as one recovered from the total deformation t. It is cleer that the phenomenon in the region below point A, in the region AC, and in the region CP corresponds exactly to the behavior of a linearly elastic, a workhardening elastoplastic, and an elastic perfectly plastic solid, respectively. The use of an elastic-verh-hardening-plastic model to describe the strace-strain behavior of concrete materials is therefore very attractive in view of these appearant einilarities.

We shall therefore assume a linear or monlinear elactic etrese-strain relactionship until the combined state of stress reaches as initial yield surface. The initial yield criterion is assumed to have the same geometrical shape in the stress space as the failure criterion. The five-parameter failure criterion of Willam-Warnhe is used to define the ultimate state of stress. A further discussion on the choice of the Willam-Warnhe's five-parameter model is given in Sec. 4.2.

Between the initial yielding state and the failure etate, an incremental stress and strain relationship is assumed to define the plantic behaviors. The plantic relations are developed on the basis of a mixed-hardening rule and the classical associated flow rule. This development is discussed in Sec. 4.3.

For the post-failure models, the concrete behaviors are defined by three types of failure modes, namely, creaking, crucking, crucking, and a sized mode. A crucking coefficient based on a dual criterion has recently been proposed by Boich et al (1982) to identify each of the failure modes. This feature of the development is described in Sec. 4.4.

For a fractured concrete, procedures have been developed to handle the otroso-otrain redistribution of a fractured element (Susuh: and Chen, 1981). These procedures are tailored for the finite-element analysis of concreto structures. For the fractured concrete stress-strein relation, an animatropic electic model is used. Details of this are given in Sec. 4.3.

#### 3.2 Failure Critotte

In early finite-clement analyses the von Misse or Treacs type of yield surface for ductile metals is generally used for concrete under compressive atreages. This type of pressure-independent yield surface corresponds to a pure shear or octabuleral shear.

dependence. To account for the limited tensile capacity of concrete, the von Missa or Tranca surface usually is sugmented by a separate tension-failure surface, e.g. the maximum-principal-atreas surface or tension-cutoff surface.

The Drucker-Prager surface is probably the simplest type of pressure-dependent yield or failure criterion where the pure shear or octahedral shear act depends linearly on the hydrostatic pieseurs I, or octahedral normal

atreas e. It can be looked upon as a smooth NBRP-Coulomb surface. The latter has frequently been used as failure surface for concrete, while the Drucker-Prager surface has most frequently been used for soils. The Brucker-Prager surface has two basic shortcomings in connection with concrete modeling: the linear relarisoship between toct

of and the independence of the angle of similarity 6 (see Fig. 2). The Toct — ect relation has been experientally shown to be curved, and the trace of the failure surface on deviatoric sections is not circular. Two-persector models with straight lines as meridians are therefore insdequate for describing the failure of concrote in the high-compression resse.

The generalized Drucker-Preger surface proposed by Bresler and Pister (1938) assumes a parabolic dependence of the second that the deviatoric second that the second that the

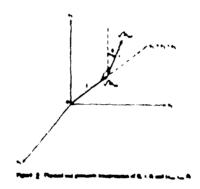
tions are independent of 0. On the other hand, the early version of the three-parameter surface developed by William-Warnte (1975) retains the linear test oct

sections exhibit 6-dependence. The feur-parameter models of Ottosen (1977) and Hoich et al (1982) and the refined five-parameter model of Willem-Warnhe

renatitute both a parabolic to ect oct oct relation and a b-dependence. Note of these refined models give a close estimate of the relevant experimental data (1981), contain all the three stress invariants, reflect all the required characteristics concerning smoothness, convexity, symmetry, curved meridians, etc. But the Willem-Marnhe's five-parameter model includes most of the earlier ones, two- and three-parameter models as special cases and becomes increasingly popular in recent years. We therefore adopt the five-parameter feilure model of Willem-Marnhe as the basic surface for the development of the present electic-plestic-fracture model for concrete.

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The five-parameter model is illustrated in Pig. 3, where it is compared with triaxial test data. Close agreement can be observed for both hydrostatic and deviatoric sections. In the lew-compression regime the surface atrengly resembles a tetrahedros, the plane of which bulges with increasing hydrostatic compression approximating a circular come asymptotically.

In oumsey, the Willes-Watske's five-parameter model reproduces the principal features of the triaxial failure surface of concrete (Chen, 1982). It consists of a tonical shape wit curved meridians and moncircular base sections as rull as someffine sections in the deviatoric plane. In view of the fluctuations of experimental there is little need for recults, further refinements of this model. Thus, we choose this surface as the basic forms for yielding, leading and failure Further discussions will surfaces. therefore be focused on the development of etress-strain relationships of coacrete under general etrese states.

## 3.3 Mixed Hardening Rule

It is convenient to assume a criterion for initial yielding to have the same functional form as the failure criterion. In the present model based on the five-parameter failure criterion of Willam and Warnke (1975), the material constants are also assumed to remain the same, except that the nondimensional constant, the compressive strength  $f_{\rm c}$  is replaced by a different value  $f_{\rm c}=0.3=0.6f_{\rm c}$ . The exact value of  $f_{\rm c}$ 

The initial yielding criterion and the failure criterion define the limits of the elastic region, the plastic region, and the post-failure region. Within the elastic region and the post-failure region, theories of linear elasticity and nonlinear anisotropic elasticity can be applied to concrete from the

can be taken from the uniaxial compressive stress-styain curve of the specific

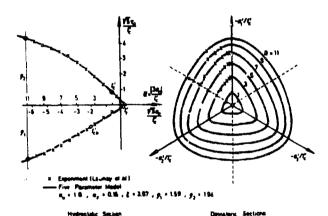


Figure 3 Comparison of test results for Willam-Warnke Failure Mode. (Willam and Warnke, 1974)

macroscopic point of view (Cher and Saleeb, 1982). For a state of stress beyond the initial yielding irreversible deformations become significant. It is convenient to follow the workhardening plasticity theory to develop the required incremental form of stress-strain relationships. This requires the consideration of a hardening rule.

The hardening rule defines the motion of the subsequent yield surfaces during plastic loading. A number of hardening rules have been proposed to describe the growth of subsequent yield surfaces for work-hardening materials. The choice of a specific rule depends on the ease with which it can be applied and its ability to represent the hardening behavior of the material being considered. Three types of hardening rules are most frequently considered:

- 1. Isotropic hardening (Hill, 1950)
- Kinematic hardening (Prager, 1955; Ziegler, 1959)
- 3. Mixed hardening (Hodge, 1957)

The imptropic-hardening rule assumes a uniform expansion of the initial yield surface. It applies mainly to monotonic proportional loadings; for cyclic and reversed types of loadings for materials with a pronounced Bauschinger effect, the kinematic hardening rule is more appropriate. It considers the Dauschinger effect in an idealized manner and also the development of anisotropy due to plastic deformation. Combinations of isotropic and kinematic hardening are called mixed hardening, which is found to be more suitable for concrete materials.

In the present model, we consider the plastic strain increment in the form

$$d\varepsilon_{ij}^{p} = d\varepsilon_{ij}^{pi} + d\varepsilon_{ij}^{pk}$$

$$= M d\varepsilon_{ij}^{p} + (1-M) d\varepsilon_{ij}^{p}$$
(1)

and introduce a constant parameter M to define the isotropic hardening effect  $d\epsilon_{1j}^{p1} = M d\epsilon_{1j}^{p}$ . The remaining plastic

strain increment  $d\epsilon_{ij}^{pk}$  is then due to the

kinematic hardening. The strain increment  $d\epsilon_{1,j}^{p,i}$  is related to the isotropic

hardening function through the concept of effective stress - effective plastic strain which makes it possible to extrapolate from a simple uniaxial compression test into the multidimensional

situation. The strain increment  $de_{ij}^{pk}$  is

related to the kinematic hardening rule of Prager's or Ziegler's.

In this mixed hardening model for concrete, the weighting coefficient M (0 < M < 1) is introduced to allow the freedom of selecting different proportions of isotropic and kinematic effects

in the mixed model. M can also be a negative value, so that isotropic softening can also be considered. The advantage of using the concept of mixed hardening have been demonstrated by Axelsson and Samuelsson (1979) in describing the loading cyclus of metals and by Haieh et al (1982) in describing the reversed loading behavior of concrete materials.

In developing an elastoplastic model for work-hardening material, three basic assumptions are general employed:

- The existence of initial yield surface and subsequent loading surfaces.
- The formulation of an appropriate hardening rule that describes the evolution of subsequent loading surfaces.
- A flow rule that specifies the general form of the stress-strain relationship.

In the present work, the first assumption is satisfied by the choice of the five-parameter model of Willam and Warnke (Sec. 4.2). As for the second assumption, we have chosen the mixed hardening rule as described here.

The third assumption states that for an idealised plastic material, it is possible to define a plastic potential function  $\mathbf{g}(\sigma_{ij}, \ \mathbf{c}_{ij}^{\mathbf{p}}, \ \mathbf{k})$ ,

$$d \epsilon_{ij}^{p} = d \lambda \frac{\partial g}{\partial \sigma_{ij}}$$
 (2)

The gradient of the potential surface defines the direction of the plestic-strain increment, while the length is determined by the loading parameter  $d\,\lambda$ .

The flow rule is associated if the plastic potential has the same shape as the yield condition

$$g(v_{ij}, c_{ij}^{p}, k) = f(\sigma_{ij}, c_{ij}^{p}, k)$$

$$dc_{ij}^{p} = d\lambda \frac{\partial f}{\partial v_{ij}}$$
(3)

The associated flow rule is applied here for practical reasons, since there is very little experimental evidence on subsequent loading surfaces. In a few cases observations are available, e.g. on the volume change during plastic flow, we may use this information, in the subsequent development to construct

a plastic potential independently of the yield surface for controlling dilatency or compection (Chen, 1907).

With the help of these three assumptions, we can now determine uniquely the stresses which arise during any iteration in a numerical analysis in which known, finite changes in strain as are imposed. This is the subject

of a later discussion.

# 3.4 Post-Fracture Modeling

Concrete fails or fractures in extremely complex modes. Aggregate types, mixed design, and loading conditions among many other factors all play roles in the cause of failure. It is difficult to classify and define precisely the failure modes. However, in a general sense, the mode of failure may be categorized into three types, namely, the cracking, crushing and a mixture of cracking and crushing. Documented results for tension-rension or tensioncompression biaxial conditions show the cause of fracture is primarily a brittle splitting in the plane normal to the maximum tensile strain direction (see for example, Chen and Ting, 1980). For the triaxial compression tests, depending on the magnitude of continement pressure, it seems that all the three types of mode are possible. When the confinement pressure is such lower than the axial compression, rough crack surfaces can be formed in the direction normal to the maximum tensile strain, possibly due to the connection of numerous microcracks. For nearly uniform hydrostatic condition, crushing failure is more common, possibly due to the rupture of morter in the concrete.

In view of the failure modes due to various types of loading conditions, a crushing coefficient a has been proposed to identify the mode being either a pure cracking, a pure crushing, or a mixture of the above (Heich et al. 1982). The coefficient can also be used to estimate the proportions of the cracking effect of the crushing effect in a mixed type of failure. This concept is found to be particularly appaaling when the postfailure behaviors of the fractured concept are considered. This concept is further refined in the present work.

The concept of crushing coefficient is based on the consideration of a dual criterion in defining the pure cracking zone and the pure crushing zone in the overall spectrum of failure mode. In the early development, the pure cracking zone is assumed to satisfy the maximum

# tensile stress condition

$$\sigma_{i} > 0$$
 (4)

which can be written in terms of the stress inverients as

$$J_2 \cos \theta + \frac{1}{2\sqrt{3}} I_1 > 0 \qquad \theta < 60^{\circ} (5)$$

where

I m o m the first stress invariant

- the second deviatoric stress invariant

$$J_3 = \frac{1}{3} *_{ij} *_{jk} *_{ki}$$

- the third deviatoric attess invariant, and

$$\cos 3\theta = \frac{3 \setminus |3|}{2} \frac{J_3}{J_2^{3/2}}$$

= angle of similarity, Fig. 2.(6)

It may be shown that the upper limit of the pure cracking condition satisfies the uniaxial and the biaxial compression failure test data, see Tig. 4. For the pure crushing type, it was assumed, as a first approximation, that all three principal strain components are all compressive strains, so that the crack machanism can not be developed in the light that no tensile strain could appear in any direction. This implies that the maximum principal strain is non-positive

Using the Hooke's law, this condition may be expressed in terms of the stress invariants as

$$\sqrt{J_2}\cos\theta + \frac{(1-2\nu)}{2\sqrt{13}(1+\nu)}I_1 < 0$$
 (8)

combining these two conditions for cracking and crushing, a crushing coefficient a may be defined

$$\alpha = \frac{I_1}{2 \setminus |J_2|} \qquad 0 < 60^{\circ} \qquad (9)$$

such that

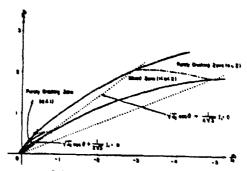
i. pure cracking mode, when a < 1

ii. pure crushing mode, when  $a > \frac{1+\nu}{1-2\nu}$ 

111. mixed mode, when

$$1 \leq \alpha \leq \frac{1+\nu}{1-2\nu} \tag{10}$$

If Poisson's v is taken to be 0.2, we have the simple values of a m 1.0 and 2.0 as the boundary values separating the three different failure zones. This is illustrated schematically in the octahedral normal and shear stress space as shown in Fig. 4.



Po.4. Police areas or constraint where and control stress plants.

Note that in obtaining the simple crushing coefficient  $\alpha$ , Hooke's law of elasticity was employed to obtain the streas criterion. Strictly speaking, this is inconsistent in an elastic-plastic-fracture model; Hooke's law may not apply immediately before crushing. However, judging by the complex nature of concrete failure and the simplicity in the application of the concept of the crushing coefficient, the elasticity assumption may represent an acceptable first approximation. For more accurate descriptions, the original dual criterion, i.e.  $\alpha_1 > 0$  and  $\epsilon_1 < 0$ , may also

be used. A further refinement on the concept of crushing coefficient will be made in the subsequent work.

To complete the constitutive model for the post-fracture behaviors of concrete corresponding to each of the failure modes, we use the following possible approaches for the mathematical modeling.

For the pure crushing sone, the crushed concrete may be viewed to behavior like a granular material under the confinement of meighboring materials. Material stiffness in compression or shear, although reduced, should still exist. For simplicity, we may neglect the residual stiffness and the residual

strength of a clushed concrete element completely in an analysis. A more refined model may consider the orientation of failure planes and use a partially collapse failure surface in the form of no-tension, no-cohesion or no-friction models (Argyris at al, 1976). This aspect of modeling is not considered in the present work.

For the pute cracking some, the customary procedures is to assume that the cracked concrete remains a continuum, i.e. the cracks are ameared out in a continuous fashion. It is assumed that the concrete becomes orthograpic (or more accurately, transversely isotropic) after the first cracking has occurred, one of the meterial axes being oriented along the direction of cracking. Such formulations easily allow for gradual build-down of strength in the direction of tension (tension stiffening). Also shear-strength reserves due to aggregate interlocking and dowel action of reinforcement can be accounted for by retaining a positive shear The continuous model for modulus. cracking has been used in most of the computational models for concrete and is therefore adopted here for further development. An extensive discussion of the kinematics of a cracked concrete element has been reported by Chen and Suzuki, (1980).

For the mixed failure zone, the value of the crushing coefficient is between 1.0 and 2.0 for  $\nu=0.2$ , for example. If the crushing coafficient is adopted as a measure of the degree of crushing in this partially cracking and partially crushing concrete element, then we may view that the post-failure behavior is also a linear interpolation of the perfectly deformable behavior and the anisotropic electic behavior. Rence ': is proposed that the concrete plumps will lose its rigidity in the rracked plane according to the maximum tensile strain direction and the anisotropic stiffness of the fractured element will also be proportionally reduced according to the magnitude of  $\alpha$ . Note that for  $\nu$  = 0.2, mixed failure lies between a = 1.0 and 2.0. Thus, the value, of a behind the decimal point represents the percentages of crushing and also the percentages of stiffuess reduction.

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THE EFFECTS OF CURING AND AGING ON THE TRIAXIAL PROPERTIES
OF CONCRETE IN UNDERGROUND STRUCTURES

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### ABSTRACT

To accurately predict the response of a concrete structure for a given loading condition some knowledge of shear strength and compressibility is required. Several studies have shown that these properties vary as concrete cures and ages; therefore, the response of a concrete structure changes with time. In order to address this problem, Sandia initiated a material test program to study the curing and aging of underground concrete structures. Material properties were obtained from cores taken periodically from two underground concrete structures constructed at the Sandia Tonopah Test Range, Nevada. Results of this continuing study are presented.

### INTRODUCTION

The effect of curing and aging on the material properties of concrete is always a design consideration. However, most research in this area is driven by construction considerations and, normally, only the effects of these factors on the uniaxial compressive strength are studied. The effects of curing and aging on the response of concrete structures to munition type loadings require additional considerations. For munition type loadings, the multi-dimensional response of concrete is important. Also, concrete structures are cured under in situ rather than laboratory conditions. Since it is difficult to test large structures, it is common to test laboratory cured scale model structures which are only several months old. To accurately apply structural response and munition effectiveness results from these models to the prototypes requires that the difference between the multiaxial properties of the model and the prototype be defined. Therefore, in the interaction of munitions with concrete structures, the effects of the variation in curing and aging on the multiaxial properties of concrete are very important. One of the most common types of defense structures is the buried concrete structure which has been used in many applications. Depending on the geologic material in which a buried structure is constructed, the in situ curing conditions can vary from dry to saturated and at other than optimal curing temperatures. Since it is difficult to obtain samples or cores from buried structures, little data is available to date on the effect of these types of in situ curing conditions on concrete properties.

In support of concrete penetration programs, Sandia constructed several buried concrete structures at the Tonopah Test Range, Nevada. In order to determine the effect of in situ curing and aging on concrete properties for these structures, Sandia has periodically cored two of these structures. With this test program, we hoped to determine the rate at which these structures cure and the maximum strengths attained.

### TEST PROGRAM

Two buried structures constructed for concrete penetration studies were tested in this program.

The first structure (Structure A) consists of several layers of heavily reinforced concrete slabs which were two to three feet thick and buried from six to 27 feet deep. The concrete was nominally 34 MPa (5000 psi) unconfined compressive strength at 28 days with one inch maximum size aggregate. The second structure (Structure B) is eight feet thick, ten feet in diameter, non-reinforced, and buried eight feet deep. The concrete was nominally 14 MPa (2000 psi) unconfined compressive strength at 28 days with no coarse aggregate. Structure A was constructed at Antelope Dry Lake and Structure B was constructed in Pedro Dry Lake. The material properties of the soil in both of these dry lake beds down through

the levels at which these structures were built are listed in Table I.

All material property tests were conducted by Terra Tek, Salt Lake City, Utah. The data obtained included physical properties (density, porosity, and saturation) and hydrostatic and triaxial compression data to confining pressures of 400 MPa (58000 psi). Concrete samples were taken as each structure was constructed. These samples were tested at the time of the first penetration test into each structure which, in both cases, was a few months after construction. After construction, each of these structures was cored at approximately two year intervals so that material properties of the aging concrete could be obtained. Structure A was constructed in 1980 and was cored in 1982, while Structure B was constructed in 1979 and was cored in 1981 and 1983.

### Physical Property Data

A summary of the physical property data for the concrete in these two structures is presented in Table II. Included in this table are the average density, porosity, and saturation of each concrete sample at each time interval. An examination of these properties indicates that density and porosity vary slightly from sample to sample in each structure. These data also indicate that the saturation of the concrete has decreased with time for both structures.

### Hydrostatic and Triaxial Compression Data

Figures 1 and 2 show the results of the triaxial and hydrostatic compression data for the concrete in Structure A. The triaxial compression data indicate that the triaxial strength of the concrete increased dramatically over a 24 month period. The hydrostatic compression data indicate that the compressibility of the concrete had increased slightly over the same 24 month period. These results are indicative of a material that obeys the effective stress theory and has a decrease in saturation.

Figures 3 and 4 show the results of the triaxial and hydrostatic compression data for the concrete in Structure B. The triaxial compression data indicate that the triaxial strength of the grout increased dramatically over a 24 month period; however, triaxial strength decreased slightly over the 24 to 46 month period. The hydrostatic compression data indicate that compressibility of the grout increased continuously over the same 46 month period. The results up to the

24 month age of this grout also are indicative of a material that obeys the effective stress theory and has a decrease in saturation over this period. The physical properties of the grout is Structure B show that the saturation of the grout did not change from the 24 to 46 month period. This could explain why there is little difference in the triaxial compression data over this period. The grout probably did not continue to decrease in saturation since it had already reached the saturation level of the surrounding soil.

In order to compare the hydrostatic ... and triaxial compression data of the concretes in Structures A and B, the data is normalized and presented in Figures 5 and 6. In Figure 5, the triaxial com-pression data from Figures 1 and 3 are normalized by the design unconfined compressive strength at 28 days, f'c, of the concrete in each structure. The normalized data show that the strengths of each congrete at each age are similar, which indicates that the rates of curing of these buried structures are similar. This might be expected since these two structures were constructed near the same location at similar depths in soil with similar saturation. In Figure 6, the hydrostatic compression data from Figures 2 and 4 have been normalized by the design unconfined compressive strength at 28 days and the average porosity of the concrete in each respective structure. The data plotted in this form shows volumetric strain increases nearly bilinearly with confining pressure with the slopes of the two linear portions nearly constant in all cases. The transition occurs near the point at which the air voids are eliminated and the samples become saturated. These data show that the rates of change of the hydrostatic compression of these concretes are mimilar.

### Conclusions

Results indicate that these concretes obey the effective stress theory and that the saturation of the concrete strongly influences triaxial strength and compressibility. The data also show the saturation of the concrete slowly decreases to the saturation level of the surrounding medium for buried structures.

TABLE I. Near surface soil properties of Antelops and Pedro Dry Lakes, Tonopah Test Range, Hevada.

### detailers Dry Labe

			faturation (1)	Cisseification
	1.92	40	78	
10	- 1.94	39	78	milty oley
	1.94	35	82	

### todro bry Lake

Depth _(ii)	Density (E/99)	Poresity _[9]	Saturation (1)	Soil Classification
10	7.92	38	•3	sandy silt
12.5	1.91	40	73	sandy silt
26	2.00	34	75	sandy silt

TABLE II. Physical properties of the concrete in Structures A and

<u> triveture</u>	Age (MALAS)	Demaity (9/90)	Poresity	Sat-Tation (9)
	{ 4	2.24	17	*1
۸	_{34	2.10	30	84
	1 3	2.10	29	82
. ~	- 24	2.00	31	74
	14	2.00	30	74

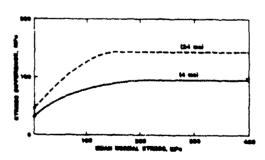


FIGURE 1. Triaxial compression data for Structure A at two different ages

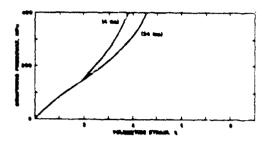
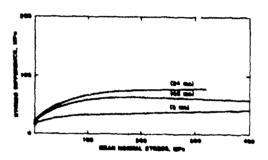


FIGURE 2. Hydrostatic compression data for Structure A at two different ages



PIGURE 3. Triaxial compression data for Structure B at three different ages

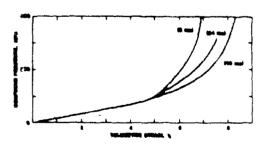


FIGURE 4. Bydrostatic compression data for Structure B at three different ages

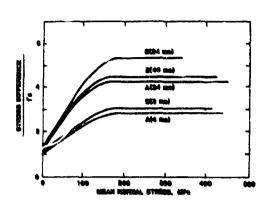


FIGURE 5. Normalized triaxial compression data for Structures A and B

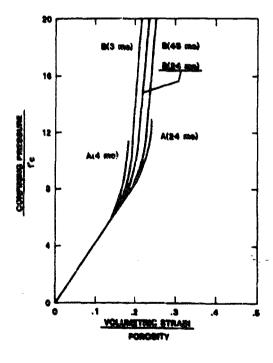


FIGURE 6. Normalized hydrostatic compression data for Structures A and B

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### STRENGTH CRITERIA FOR AMISOTROPIC MATERIALS

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### ABSTRACT

In this paper, the criteria of strength for some anisotropic materials are investigated. The existence of a strength function, which is a function of invariants of a stress tensor, is assumed. The invariants for each class of anisotropic materials are obtained.

### INTRODUCTION

For the purpose of material characterization and design, a rational simple strength criterion for composites is essential and important. As pointed out by Tsai and Mu [1], the majority of proposed criteria are limited in their ability to include the correlating stress effects. In order to remove such a limitation, Gol'denblat and Kopnov [2] proposed a new criterion of strength for anisotropic materials. They investigated explicitly the form of strength criterion for orthotropic materials. In particular, they verified their results for glass-reinforced plastics experimentally and showed the suitability of the proposed criterion of strength for practical usage. In this paper, the criteria of strength for some anisotropic materials are investigated. We assume the existence of a strength function [3] which is a function of invariants of a stress tensor. The invariants for each class of anisotropic materials are obtained. Consequently, the strength functions proposed by Tsai and Wu [1] for triclinic and rhombic (orthotropic) materials, by Gol'demblat and Kopnov [2] for rhombic, and by Hill [4] for orthotropic materials can be obtained readily from the appropriate invariants given in this paper.

### Strength Criteria for Anisotropic Materials

Consider a strength function [3]

$$F(\sigma_{\frac{1}{2}}) = 0 \tag{1}$$

which is required to be invariant under a group of transformations  $\{t_{ij}\}$ , characterizing the material anisotropy, i.e.,

$$F(\overline{a}_{1j}) = F(a_{1j})$$

and 
$$\overline{\sigma}_{ij} = t_{im}t_{jn}\sigma_{mn}$$
 (2)

Invariants for each system of enisotropic materials are obtained in the followings by using Eq. (2), [4,5]. The contracted notation is used; ( $\sigma_{11}$ ,  $\sigma_{22}$ ,  $\sigma_{33}$ ,  $\sigma_{23}$  "  $\sigma_{32}$ ,  $\sigma_{13}$  "  $\sigma_{31}$ ,  $\sigma_{12}$  "  $\sigma_{21}$ ) " ( $\sigma_{11}$ ,  $\sigma_{22}$ ,  $\sigma_{33}$ ,  $\sigma_{4}$ ,  $\sigma_{5}$ ,  $\sigma_{6}$ ).

### 1. Triclinic System

For crystals having triclinic symmetry, there is no restriction on the orientation of the preferred direction; any rectangular coordinate system can be used as a reference frame. Thus, the invariant  $\{I_{\underline{t}}\}$  for both classes are

$$I_1^{(1)}; \quad \sigma_1, \ \sigma_2, \ \sigma_3, \ \sigma_4, \ \sigma_5, \ \sigma_6 \ .$$
 (3)

### 2. Rhombic System

### 3. Treverse isotropy

It is supposed that the material is transversely isotropic with respect to an axis  $\mathbf{x}_n$ . Thus, the transformations characterizing transverse isotropy are I and

$$R_{\alpha}(x_1^2 + ix_2^2 = e^{-i\alpha}(x_1 + ix_2), x_3^2 = x_3)$$
 for all values of  $\alpha$ ).

Therefore, the inverients are

When the terms of degree three  $\{I_i^{(3)}\}$  for f are omitted, the results (Eq. (3), (4), (5)) yield the forms of the quadratic strength function. In particular, the strength function for an orthotropic material can be written readily from Eq. (4) with the  $I_i^{(3)}$  omitted. This is

$$(F_{1}^{\sigma_{1}} + F_{2}^{\sigma_{2}} + F_{3}^{\sigma_{3}})^{\alpha} + (F_{11}^{\sigma_{1}^{2}} + F_{22}^{\sigma_{2}^{2}} + F_{33}^{\sigma_{3}^{2}})$$

$$+ 2F_{12}^{\sigma_{1}^{\sigma_{2}}} + 2F_{23}^{\sigma_{2}^{\sigma_{3}}}$$

$$+ 2F_{13}^{\sigma_{1}^{\sigma_{3}}} + F_{44}^{\sigma_{4}^{2}} +$$

$$+ F_{55}^{\sigma_{5}^{2}} + F_{66}^{\sigma_{5}^{2}})^{\beta} = 1 \qquad (6)$$

This result can be reduced to the result in the Ref. [1] by taking  $\alpha=\beta=1$ , and in the Ref. [2] by taking  $\alpha=1$  and  $\beta=1/2$ . Furthermore, if the absence of a Bauschinger effect is assumed and the material constants  $\alpha$  and  $\beta$  are taken to be unity, Eq. (6) yields the Hill criterion [6];

$$F(\sigma_2 = \sigma_3)^2 + 6(\sigma_3 = \sigma_1)^2 + H(\sigma_1 = \sigma_2)^2 + 2L\sigma_4^2 + 2H\sigma_6^2 + 2H\sigma_6^2 = 1.$$
 (7)

where the coefficients of the strength function are defined as;

$$F = -F_{13}$$
,  $G = -F_{23}$ ,  $H = -F_{12}$ ,  $2L = F_{44}$ ,  $2M = F_{55}$ ,  $2M = F_{66}$ ,  $F_{11} = G + H$ ,  $F_{22} = H + F$ , and  $F_{33} = F + G$ .

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7

## CONSTITUTIVE PROPERTIES OF STELL FIBER REINFORCED CONCRETE IN HULTIAXIAL LOADING

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### ABSTRACT

The constitutive perperties of steel fiber reinforced concrete (FRC) are being studied experimentally in a unique fluid cushion multi-axial cubical test cell at the University of Colorado. In the first phase of the program, the behavior of FRC was tested under three-dimensional compressive loading. The strength and stress-strain properties are analyzed by using constitutive models available in the literature. In the second phase, a modification to the existing test apparatus was made for testing cubical specimens under direct tension loading. The modification consists of brushes with individual bristles glued to the specimen. In this paper, results are shown from the biaxial tension-compression test program to demonstrate the strength interaction.

### INTRODUCTION

The addition of fibers to cementitious materials improves many of the engineering properties by providing for a different deformation and failure mechanism from that of the plain matrix material. Although a significant amount of research has been cerried out on steel fiber reinforced concrete (FRC) in the past two decades, there is still a considerable void in the knowledge of the strength and stress-strain behavior of FRC under complex states of stress. This stams mainly from a leck of suitable equipment for applying multidimensional stress and, in particular, for simul-taneously applying combinations of tension and compression. Thus, most FRC applications to-date have been limited to situations where the predominant stress condition can be simulated in the laboratory, e.g., flexural loading in bridge deck overlays, highway and airfield pavements. It appears that the improved properties of FRC over plain Portland cement concrete were also desirable of FRC could only be brought about if a better understanding of its engineering properties under complex stress states is available.

A research program, spensored by the Air Force Office of Scientific Research has been underway at the University of Colorade at Beulder for the past few years to examine the strength and behavior of steel fiber reinforced concrete subjected to both three-dimensional compressive load-

ing and blaxial tension-compression loading. In this paper, the results of the test program are presented.

### MATERIAL

From a preliminary test series in which several types of steel fibers were used in conjunction with one common plain concrete mix, Egging [1] selected for the test program the Dramix 30/0.4 fibers manufactured by Bakaert Steel Wire Corp. These fibers are streight, round wires with patented hooked ends to increase their resistance to pullout. The wires, 30 mm in length and 0.4 mm in diameter, are available in collated clips, held together by a water soluble glue. The glue dissolves within une minute after the clips are added to the plain concrete, allowing dispersion of the individual fibers. A volume fraction of 0.6 percent was used in the mixing of the FRC. This value may appear low in comparison with those used for straight fibers without bent ends. However, it was selected on the basis of manufacturer's claim of the higher pullout resistance afforded by the deformed fibers. With this volume fraction, no balling or segregation of the fibers was observed during mixing and good workability was obtained.

The plain concrete mix design consisted of the following parameters:
water/cement ratio = 0.5
coment content = 770 lb/cu yd
maximum size of coarse aggregate = 3/8 in fineness modulus = 2.5
percent of fine aggregate = 53% of total
aggregate

This plain concrete mix has a uniaxial compressive strength of 7,900 psi, while the FRC obtained by adding fibers at 0.6 percent by volume has a strength of 9,150 psi.

### TEST EQUIPMENT AND PROCEDURE

The multiaxial cubical test cell developed for compressive testing of concrete, rocks and composite materials (Ko and Sture [2]) was used for the test program on FRC. For the combined tension-compression testing, a new addition to the test cell was made. The equipment is briefly described in the following.

٧,

The test cell consists of a rigid frame onto which are mounted six walls. The frame has three orthogonal square holes mechined through it as shown in Figure 3. The intersection of these holes forms a cubical cavity in the center of the frame, within which the 4 in, cubical test specimen resides. The six square openings in the frame, together with the adjoining walls, act as pressure chambers. Each face of the test specimen becomes the interior wall of one chamber. A fluid cushion system is established in each chamber through the use of a flexible polyurethane membrane attached to the inside face of each wall. This membrane, which fits into the square opening in the frame, retains the hydraulic fluid pumped into the chamber. The fluid pressure generated within the membrane is resisted by the specimen and exterior wall. A typical wall assembly with the fluid cushion is also shown in Figure 1.

On the interior face of each well and within the fluid cushion system is mounted a set of three proximity transducers, manufactured by Bentley Nevada Corp., for detecting the movement of brass targets glued to the surface of the test specimen. The pressurizing medium in the fluid cushions is silicon fluid, chosen for it. inert properties and moninterference with the performance of the proximity probes. The pressures to the three pairs of opposite fluid cushions are generated by three hand pumps, and the plumbing is arranged in such a way that each pump can be used to deliver the pressure to one, two or all axes in the test cull. The design capacity of the system is 25,000 psi.

The fluid cushion loading system employed in the test device has been shown to provide the least boundary constraint on the test speciman, and to have distinct advantages over other methods of load application (e.g. rigid platens with or without lubrication) in the testing of concrete materials [3,4]. In essence, the application of a known, uniform normal compressive stress through the flexible membrane in the fluid cushion system ensures complete control of the applied three-dimensional stress state. In addition, since the specimen is unrestrained by the fluid cushions, the mode of deformation and failure in the test specimen is uninhibited by the test equipment. Thus, the response measured in testing with this equipment reflects the true material property.

The system described above has been used in the constitutive characterization of many concrete and rock materials under arbitrary, compressive loading. To accommodate the needs of the cirrent project on FRC, an additional feature was installed to provide the capability of tension testing in one axis, Maier [5]. The tension loading device adopted utilizes a pair of brush platens glued to the apposite surfaces of the test cube for applying the tension load. One half of the tension loading device is shown schemetically in relation to its mounting on the frame in the cubical test cell in Figure 2.

Each brush platen is made of 225 aluminum bristles, erranged in a square pattern and keyed into an aluminum anchoring block. This block is connected to a double acting hydraulic cylinder through a spherical seat assembly designed to accommodate rotation and translation of the test cube, and to maintain concentricity of the applied tension force.

The tension generated by the hydraulic cylinder to pull on the brush platen is resisted by a pair of stand-offs mounted on the cubical cell frame. The specimen deformation in the direction of the applied tensile stress is measured by proximity transducers that monitor the movement of targets mounted on the brush block.

The brushes are glued to the fRE test specimen by means of a commercial structural concrete epoxy (Sikadur 31 Hi-Hod Gel). The gaps between bristles in a brush platen are filled with a silicone rubber material to prevent penetration of the epoxy. The rubber is soft enough so as not to restrain the lateral movement of the bristles. After each test, the brushes are cleaned by sandblasting the tips of the bristles in order to prepare a clean surface for the epoxy bonding for the following tests. The epoxy develops its full strength in 24 hours.

Data acquisition in the test system is handled by a multiplex scanner controlled by a HP 9830 calculator. The output signals from the 18 proximitor transducers are scanned and sent in digital form to the calculator which then computes the changes from the initial conditions. The specimen deformations are then computed by reference to a calibration curve. It is necessary to allow for the flexibility of the test system which is not negligible in comparison to the deformations of the FRC test specimen. The system is calibrated by testing a dummy aluminum cube of known properties.

### MARGORY TEST

Two phases of the test program have been completed, as described in the following.

In Phase 1, three-dimensional compressive loadings were applied along the stress paths as shown in Figure 3. These stress paths consisted of hydrostatic (isotropic compression) loading to the selected mean stress level of 4, 6 or 8 ksi, followed by deviatoric (pure shear) loading in that deviatoric plane in the direction of triaxial compression (TC:  $\sigma_1 > \sigma_2 = \sigma_3$ ), triaxial extension (TE:  $\sigma_1 = \sigma_2 > \sigma_3$ ), or simple shear (SS:  $\sigma_1 > \sigma_2 > \sigma_3, \sigma_3 = constant$ ). During the deviatoric loading, the mean stress, 1/3 ( $\sigma_1 + \sigma_2 + \sigma_3$ ), remained constant. For each test path, several replicate experiments were performed.

In Phase 2, biaxiel tests were performed along the stress paths as shown in Figure 4. There were two groups of biaxial tests in this

Phase. The first group consisted of biaxial compression tests with proportional loading with the stress ratio  $\sigma_1/\sigma_1$  equal to 0/1, 1/10, 1/3, 2/3, and 3/3, while  $\sigma_2$  remained at zero. The first stress ratio represents uniaxial compression, while the last represents equi-biaxial compression. The second group of biaxial tests consisted of combined tension-compression leading, with the compressive stress first applied, to be followed by tensile leading in a transverse direction. The compressive preloading was taken to 0.1, 0.3, 0.4, 0.5, 0.65, 0.68 and 0.65 of the unconfined compressive strength. Of course, direct tension loading without any compressive preloading was also employed.

The objectives of the Phase I test program were to obtain both the strength and the benevior of the FRC under multiaxial compressive loading for constitutive modeling. Similar test programs have previously been conducted on plain concrete 13,43, so that the new results on FRC could be examined and compared with existing data, despite the difference in materials. In the Phase 2 program, attention was focused on obtaining the biaxial failure envelope and on the effects of combined loading on the tensile strength of FRC.

### RESULTS

### Phase 1

Typical stress-strain curves obtained from Phase I are shown in Figure 5 where the major principal stress normalized with respect to the mean stress is plotted versus the principal strains in the x, y and x directions, and the volumetric strain  $\epsilon_{\rm V}$ . The first portion in each stress-strain curve represents the hydrostatic loading to the ratio of  $\sigma_{\rm I}/\sigma_{\rm CM}=1$ , where in the case shown  $\sigma_{\rm CM}=8$  ksi. The three principal strains showed almost equal magnitudes under hydrostatic loading, indicating an isotropic material. However, any assumption regarding isotropy must be based on more extensive investigation in which different directional loadings are used.

The behavior shown for the TC test path in Figure 5 is typical of all reviatoric loadings used in Phase 1. At point A identified on the volumetric strain curve, volume dilation began to occur. This point, sometimes referred to as the point of discontinuity, has been taken to represent the condition under which uncontrolled crack growth would develop, eventually leading to physical failure of the specimen if sufficient time is allowed. Under normal testing conditions, where the rate of loading is fast in comperison to the crack growth rate, continued increase in the applied load leads to physical failure at a level 15-20 percent above the point of discontinuity.

In Phase 1 of this investigation, the points of discontinuity obtained under different stress paths were plotted in principal stress space to define a f flure envelope. Two different cross-sections or this envelope are shown in the deviatoric plane in Figure 6 and in the Rendulic (tri-

axial) plane in Figure 7. Three sets of data are plotted in Figure 6, from the tests on the 4, 6 and 8 ksi deviatoric planes, respectively. In addition to the leboratory test data, "igures 6 and 7 also show the feilure envelope predicted by the Willam-Marnke theory, which was obtained in the following manner.

A theory commonly used in representing the failure conditions of concrete under multiaxial stress states has been proposed by Willem and Warnke [6], which prescribes a conical surface in principal stress space with curved, parabolic meridians ami a deviatoric cross-section that has an elliptical variation between the extremes of TC and TE conditions within a typical 60" sector. The theory containing five parameters is usually calibrated with input information from (1) uniexial compressive strength, (2) equi-biaxial compressive strength, (3) unleafel tensile strength, (4) shear strength in TC at high compressive stress level and (5) shear strength in TE at high stress level. In Phase I of the present test progress, only shear strength data along TC, TE and SS paths were available. Using TC and TE data in the three deviatoric planes, the Millam-Marake model was calibrated (Egging, [1]). The parameter values obtained from the calibration are shown in Figures 6 and 7. It can be seen that reasonable Figures 6 and 7. It can be seen that reasons representation of the test data is obtained, comparison along the SS test path provides a measure of the accuracy of this model.

The strength data from Phase I were also used to fit the model proposed by Lade [7], while the stmiss-strain data were fitted to the formulation proposed by Gerstle [8]. While reasonable success obtained in both efforts, the reader is referred to Egging [1] for (urther details.

### Phase 2

The strength results from the Phase 2 test program are shown in Figures 8 and 9. The data points in these figures represent the stress states at which physical failure occurred. In the tension-compression tests, volume dilation occurred throughout the tensile portion of each stress path, which precludes the use of the point of discontinuity as a definition of failure.

In Figure 9, the tension-compression results are shown normalized with respect to both the uni-axial compressive and tensile strengths in order to show the trend in the strength behavior more clearly. The most significant feature in Figure 9 is the well-defined inflection point in the strength envelope. Although an inflection point has been seen in past investigations on plain conc.ete [9,10], the rate of change in slope in Figure 9 is significantly greater than has? The seen previously. An explanation for this is a new next.

In direct tension, failure of the FRC was the result of the fibers pulling out of the concrete matrix shortly after the matrix failed. As a

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result, the tensile strength of the FRC was only ten percent greater than that of an identical mix of plain concrete. The application of a small transverse compressive stress, while doing little damage to the concrete matrix, increases the resistance of the fibers to pullout by providing a clamping force. Therefore, at stress levels less than approximately 40 percent of the uniaxial compassive strength, the decrease in strength normally seen in plain concrete is offset by the in-or resistance to pullout. In comparison, at me unlaxial compressive strength, the plain concrete strength was 25 percent less than in uniaxial tension. At compressive stress levels above 0.4, however, crack propagation is initiated under the influence of the compressive stress. Pre-existing flaws at the fiber-matrix interface will begin to extend and the pullout resistance is quickly lost, resulting in a sharp drop in strength which tends toward the strength of the plain concrete as the compressive stress level is

In summary, the strength benefits afforded by the addition of the fiber reinforcing are greatest in biaxial tension-compression situations where the compressive stress is small in comparison to the uniaxial compressive strength.

### ACKNOWLEDGE WENTS

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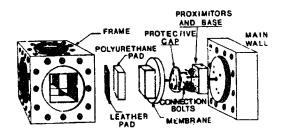


Fig. 1. Exploded View of Test Cell

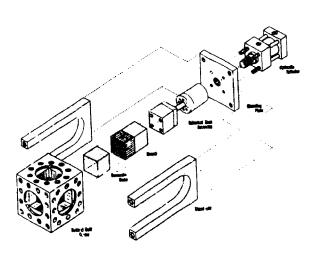


Fig. 2. Tensile Loading Apparatus

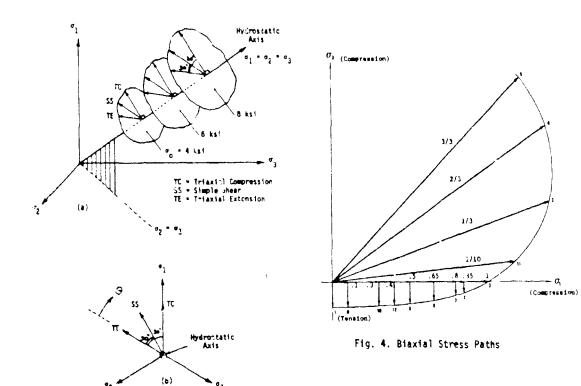


Fig. 3. Stress paths in (a) 3-D Stress Space; (b) Davitoric Plane

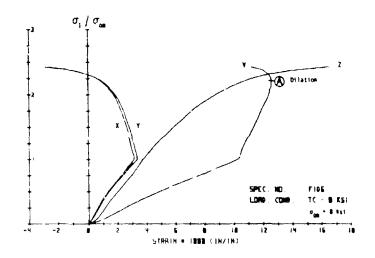


Fig. 5. Typical Stress-Strain Data

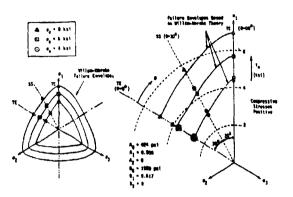


Fig. 6. Failure Data in Deviatoric Plane

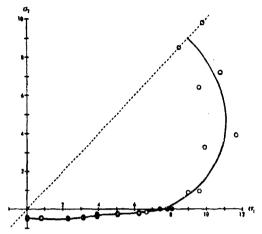


Fig. 8. Biaxial Failure Envelope.

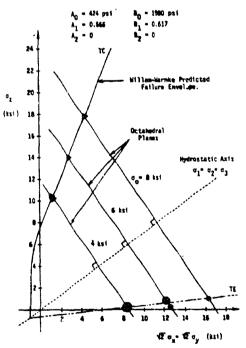


Fig. 7. Failure Data in Rendulic Plane

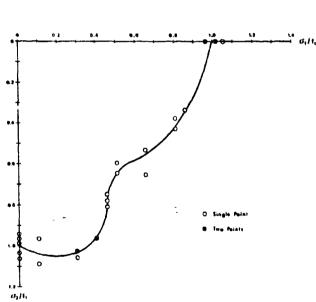


Fig. 9. Failure Data in Combined Tension-Compression



## P001720

### A SIMPLIFIED VISCOPLASTIC THEORY FOR FRICTIONAL MATERIALS

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### **ABSTRACT**

A viscoplasticity theory is described in terms of the mean pressure and a new third invariant which involves a shifted stress tensor. The flow rule is nonassociated with respect to the pressure. Illustrative results for limit states and stress paths are given for a variety of frictional materials.

### INTRODUCTION

The conventional theory of plasticity has a long history of successful use in applications involving metals. The theory is well-founded on a physical and a mathematical basis with numerous applications to engineering problems through the use of computer programs. This wealth of experience and familiarity has led to numerous attempts to apply the theory to frictional materials such as concrete, rock, soils, ice, and snow. Although there is no fundamental reason why the theory of plasticity should be appropriate for these materials, there are now several formulations that provide correct behavioral characteristics. Unfortunately many of these relations are so complicated that their use is limited to the simplest engineering applications. This presentation is the result of an attempt to formulate a model that captures essential response characteristics without recourse to a large number of parameters or special conditions. The introduction of a new third invariant leads to a plasticity theory that appears to be natural for frictional materials in the same sense that the von Mises formulation works so well for a wide class of metals.

### LIMIT SURFACES

Limit surfaces for frictional materials depend on the first invariant of stress, or mean pressure, and on a measure of shear which can be expressed through the second and third invariants of stress. The conventional approach has been to express a limit surface in terms of the mean pressure and the second invariant of the stress deviator

$$P = -\frac{1}{3} \operatorname{tr} g - J_2' = \frac{1}{2} \operatorname{tr} (g^d)^2$$
 (1)

with modifications provided by incorporating a third invariant as dictated by experimental observations. Lade and Duncan [1] and Lade [2] have shown if a particular form of the third invariant is used, the second invariant is not required in the expression for a limit surface for at least particular classes of soils and concrete. A modification of their approach is proposed to utilize this feature, which may hold for all frictional materials.

With the use of a shift in stress,  $\mathbf{g}_{s}$  , a convenient definition for a third invariant is

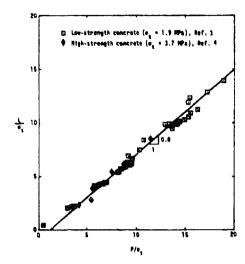
$$L = - [\det (g - g_s) + \det (g_s)]^{1/3}$$
 (2)

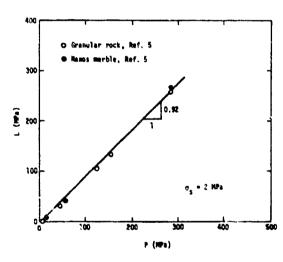
in which the second term in the brackets is included to make L equal to zero for a state of zero stress. Analogous to the square root that is often used with the second invariant, a cube root is introduced to provide the dimension of stress.

A limit point is the point on a prescribed stress or strain path at which the state of stress is stationary with respect to increments in strain. If such points for a variety of paths are plotted in stress space, the result of interpolating between the points is a limit surface (often called a failure surface). A fit to limit points for concrete, granite, marble, dense and loose sands, and clay is postulated to be the line

$$L = \lambda_{L}P - \sigma_{S} \tag{3}$$

described with two parameters consisting of a limit slope,  $\gamma_L$ , and the intercept on the L-axis represented by the shift stress,  $\sigma_S$ , with the assumption  $g_c = \sigma_c L$ . The fits, which are shown in Figure 1, are remarkably good considering the elementary formulation.





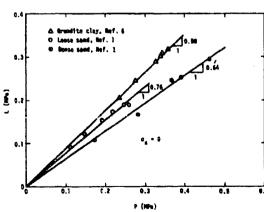


Figure 1. Limit curves for frictional materials.

### FLOW SURFACES AND FLOW RULES

For the development of a plasticity relation, the initial flow surface can be developed from the point of deviation from linearity on stress-strain curves. Then this yield surface can be assumed to evolve out to a limit surface to represent the strain hardening phase of deformation. Strain softening can be obtained by letting the flow surface collapse in a controlled manner.

Since the limit surface is conveniently represented by a line in a space involving the third invariant, a flow surface of a similar nature can be postulated as follows:

$$\phi = \gamma P - L - \sigma_S \tag{4}$$

in which  $\gamma$  is a strain-hardening function with the restriction  $\gamma > \gamma$ . A surface  $\phi = 0$  defines the flow state. For stress states above this line,  $\phi < 0$ , which represents an elastic state, and  $\phi > 0$  is not permitted.

A general hardening description is obtained by allowing the flow surface to rotate toward the limit line, i.e., to let y descrease with some measure of inelastic strain to the value y. Then with further deformation, the flow surface rotates back and this represents strain softening. The representation of such behavior together with typical loading paths in the P-L plane is shown in Figure 2.

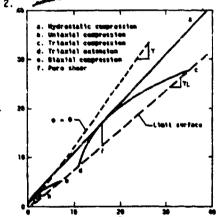


Figure 2. Stress paths and flow surfaces in the P-L plane. To control the amount of dilatation a nonassociated flow rule is adopted with the nonassociativity related only to the mean pressure. This is accomplished by using a potential function similar to the flow function but with the parameter  $\gamma$  replaced by another one,  $\gamma^{\pm}$ , where

$$\gamma^{+} = \gamma + \gamma_{a}$$
  
in which  $\gamma_{a}$  is a material constant. (5)

Deformation results have been compared with experimental data [7] for two materials with vastly different properties. One is a high-strength concrete that displays shear enhanced compaction and considerable dilatation. The other is a porous foundry core that simulates cemented sand. Volumetric compaction up to 30 percent is exhibited under uniaxial strain and the shear enhancement is considerable. All of these characteristic features are displayed by the constitutive model and the quantitative comparison with experiments is good for several stress paths.

### VISCOPLASTIC FORMULATION

Most frictional materials show a rate dependence although specific experimental data are rare and difficult to obtain [8]. Since these data were obtained for a single path, there are essentially no guide lines to assist in developing a three-dimensional theory. It is assumed that a reasonable representation can be obtained by allowing the parameter y to vary with inelastic strain rate in addition to inelastic strain. Furthermore, the relation is taken to be separable in strain and strain rate with the following form adopted for illustrative purposes:

$$Y_r = Y \left( 1 - A \tanh \frac{\dot{\epsilon}}{\dot{\epsilon}_0} \right) \tag{6}$$

in which  $\gamma_{\Gamma}$  denotes the parameter used for rate effects,  $\gamma$  is the rate independent value, A is an amplification factor,  $\bar{v}$  denotes a measure of inealstic strain rate, and  $\bar{v}_0$  is a reference strain rate. The result is a theory that is robust from a numerical point of view and that provides a smooth dependence on two additional material parameters, A and  $\bar{v}_0$ .

Representative response curves have been obtained numerically for loose sand and are shown in Figure 3 to illustrate the effects of these parameters. These preliminary results indicate that fits to existing data should be a relatively easy matter which is desirable for analysts who use large general purpose computer codes.

### **ACKNOWLEDGEMENT**

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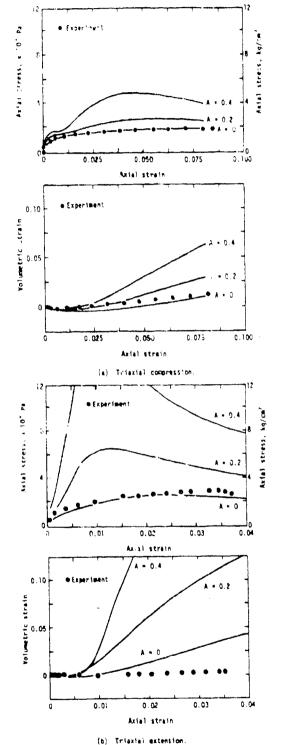


Figure 3. Theoretical predictions for a range of rate effects and static experiments! results (Mef. 1) for losse sand.

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## CONSTITUTIVE RELATIONS OF CONCRETE SUBJECTED TO A VARYING STRAIN RATE

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### ABSTRACT

Experiments conducted on concrete subjected to impact loading in uniaxial tension, unlaxial compression and in flexure, indicate that (1) the strain effects in concrete are not isotropic, (2) the stress-strain curves becomes less non-linear with increasing strein rate and (3) the rate of growth of internal microcracking decreases with increasing strein rate. A continuous damage model is proposed to establish the constitutive relationship of concrete. To include the effect of strain rate on internal damage, an inertial term is introduced in the damage evalution equation. The damage is expressed as a tensor quantity. The damage is expressed as a tensor quantity. Hersiholtz free energy function is expressed in terms of both the invariants of strain tensors and damage tensors. Equations predicted by the model are compared with the experimental results.

### 1. INTRODUCTION

It is widely accepted that the failure of concrete is brought about by the nucleation and growth of a number of microcracks. A review of the dynamic test results available for concrete also indicate that the strain-rate effects observed for concrete can be, to a large extent, attributed to the rate dependence of this microcracking process [1, 2]. It appears, therefore, that the continuous damage theory is a rational choice for predicting the mechanical behavior of concrete under both quasistatic and dynamic loading.

### 2 FORMULATION OF A CONSTITUTIVE MODEL

A vectorial representation is adopted for the damage which is motivated by the planar nature of the microcracks in concrete. The damage vector is chosen to be normal to the plane of the crack field and having a magnitude equal to the area density of the cracks. A vectorial damage variable, in contrast to a scalar damage variable, is also capable of modeling the crack induced anisotropy observed in concrete. Damage is treated as an internal state variable which influences the free energy of the material. For the present formulation the Helmholtz free energy function (a) is defined in terms of the coupled inveriants of damage and strain as.

$$+ \lambda^{2} (m_{\alpha}^{4} m_{\beta}^{4})_{-p^{2}} (m_{\alpha}^{6} e^{k\bar{x}} e^{k\bar{x}} m_{\alpha}^{8})$$

$$+ \lambda^{5} (m_{\alpha}^{4} m_{\alpha}^{4})_{-p^{2}} (m_{\alpha}^{6} e^{k\bar{x}} m_{\alpha}^{8})$$

$$+ \lambda^{1} (m_{\alpha}^{4} m_{\beta}^{4})_{-p^{2}} (m_{\alpha}^{6} e^{k\bar{x}} m_{\alpha}^{8})$$

$$+ \lambda^{2} (m_{\alpha}^{4} m_{\beta}^{4})_{-p^{2}} (m_{\alpha}^{6} e^{k\bar{x}} m_{\alpha}^{8})$$

$$(1)$$

where  $\lambda_i$  u are the lamb parameters,  $\omega_i$  is the damage vector,  $\varepsilon_{i,j}$  is the stress tensor and  $\rho$  the density of the material. The three parameters  $\gamma_i$  which define the influence of the microcracks on the state of the material, are considered to be constants in the present formulation. The superscript  $\alpha_i$  indicates the possibility of the occurrence of more than one independent damage field.

This particular form of the free energy function differed from the form chosen by Dawison, L. and Stevens, A. L. [3] by virtue of the power n associated with the fourth term. This term can thus be of a different order in atrain and damage. This provided for the obtainment of an equilibrium damage configuration from the free energy function.

A consistent thermodynamic approach yields the constitutive equation,

$$\sigma_{ij} = \rho \frac{\partial \psi}{\partial c_{ij}}$$
 (2)

and the damage evolution equation,

$$\rho k \widetilde{\omega}_{i} = g_{i}^{0} \left( \epsilon_{ij}, \omega_{i}, \omega_{i} \right) - \rho \frac{3\phi}{3\omega_{i}}$$
 (3)

where  $a_{ij}$  is the stress tensor and k is the ininertia associated with the microcrack growth [4].

 $g_{\frac{1}{4}}^{D}$  should satisfy the entropy production inequality resulting from the thermodynamic formalism and is chosen as,

$$g_{1}^{D} = -\gamma_{4} \left(\omega_{0} - \dot{\omega}_{0}\right)^{1/m} - \frac{\dot{\omega}_{1}}{\omega_{0}}$$
 (4)

where  $\mathbf{w}_0$  is the magnitude of  $\mathbf{w}_1$  and  $\mathbf{y}_4$  and  $\mathbf{m}$  are constants.

Eqs. 1-4 can be combined to yield the stressstrain relations for a particular state of the material. Due to the assumption of the planar nature of the microcracks however, the theory appears to yield reliable results only for planar problems where cleavage strains are small enough to keep the crack openings small. Also, since friction is not yet considered, it is not possible to simulate blazial compression and strain softening.

### 3. COMPARISON WITH EXPERIMENTAL RESULTS

Instrumented impact tests on flexurel beams have been conducted by the authors [1, 5, 6]. To obtain reliable mechanical properties with instrumented tests with brittle material such as concrete, it is necessary to reduce internal effects [5]. Results of this continuing experimental investigation were compared with the theory.

The analytical and experimental moment vs. strain curves at two strain rates are given in Figure 1. It can be noticed that increasing the strain-rate has no significant effect on the intial tangent modulus but results in decreasing the nonlinearity of the curves.

The analytical predictions for the strength increase in tension, flexure and compression are compared with results obtained by the authors and other available results in Figure 2. The constitutive model can be observed to be successful in predicting higher strain-rate sensitivity in the tensile mode as compared to the compression mode.

Figure 3 gives the variation of the apparent Poisson's ratio (calculated at a strain corresponding to the peak stress (under quasi static loading) with strain-rate. This value exhibits an increasing trend in tension and a decreasing trend in compression, as the strain-rate is increased. Such trends conform with the available experimental results [2].

### 4. CONCLUSIONS

A constitutive model was developed for the quasistatic and dynamic benevior of concrete, based on the continuous damage approach. The constitutive equations as well as the damage evolution equations were derived consistently from thermodynamic consideration. The model was calibrated by the use of flexural and compression test results over a range of strein-rates. The model was also found to be capable in predicting certain other phenomena of the dynamic response of concrete.

### ACKNOWLEDGMENT

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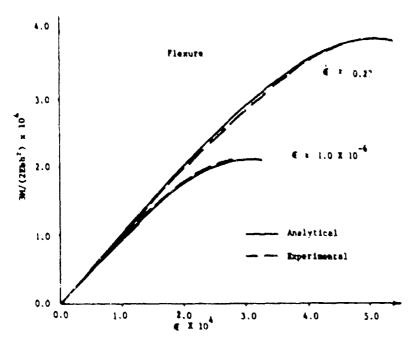


Fig. 1 Analytical and Experimental Moment vs. Strain Curves in Flexure

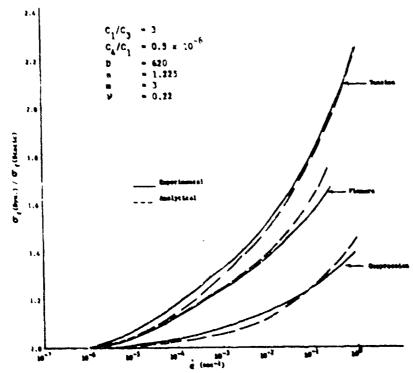


Fig. 2 Analytical and Experimental Curves for the Effect of Strain-Rate on the Ultimate Strength

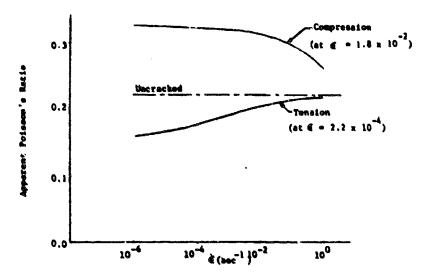


Fig. ) The Effect of Strain-Rate on the Apparent Poisson's Ratio

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### ROCK/ELASTOMER COMPOSITES AS IMPACT RESISTANT MATERIALS

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### AMETRACT

Composites cast from polymers, rock aggregates and send have been examined to determine their resistance to penetration by 7.62mm dismeter high velocity projectiles. The effects of using different polymer and rock aggregate types have been investigated, and the resultant composites optimized in terms of cost effectiveness and penetration resistance.

Optimization was carried out using response surface theory and variables considered were mix proportions, rock aggregate particle size and polymer hardness. Penetration tests were carried out on optimised desposites to determine the thickness required for a given confidence level of projectile containment.

### DITRODUCTION

An interest in the protection of buildings and other structures against small ares fire led Gibbs and Prescott (1) to undertake a limited experimental study into the behaviour of dry gravel armour which had been used in wire mesh boxes to protect wehicles against infantry fire during World Wax II. Their tests showed that a theoretical approach to find the optimum gravel perticle size, using "billiard ball" theory, was not valid because of the high degree of comminution of the gravel pirticles. The effectiveness of the armour, however, was proven.

A major problem in using grawel is containment of the material. A flexible binder is desirable because of the extensive fracture which occurs in brittle material on impact. Hence the idea axuse of using a cold curing rubbery polymer as the binder, and a study has been carried out to test the effectiveness of this type of rock/elastomer exaptsite and to optimize the material in terms of its impact resistance.

At an early stage it was realised that a two phase mixture of elastomer and work particles would be very expensive because of the large percentage wolds which had to be filled with high cost blastomer. Bence send was included in the mix to act as a filler. The resulting composites were unusual because of the relatively low elastic modulus of the matrix marerials. Mo published information on the penetration resistance of this type of composite material could be found, although there was considerable information about penetration into homogeneous and layered materials (2. 1. 4.)

Descriptions of pasetration suchanics have used the following approaches (i) espirical, (ii) assumed force law, (iii) enalytical and (iv) numerical (using computer codes). In the first two categories the parameters must be determined from pasetration superiments, and application of the resultant formulae is (m) valid in any other context. This is because the parameters are not defined explicitly in terms of the constitutive properties of the medium and projectile characteristics. However, such methods usually show good results within these bounds.

In the analytical approach, constitutive and continuum equations are used to describe the evant, and, ideally, are solved in a closel form to produce predictions of dmpth of penetration, projectile decleration, etc. However, this type of solution has not been achieved without a high degree of simplification.

Humerical approaches are expensive in time and money. However, for situations using materials with well defined properties offering a high degree of reproduceability, their value is apparent

The latter two methods have only been developed to the stage where they can cope with homogeneous materials, possibly in layers. Beterogeneous materials such as concrete have been considered, but have been treated as homogeneous. Generally, the projectile sizes used have been orders of magnitude larger than the concrete aggregate size. In the case of the composites in this study, the aggregate size was similar or about one order of magnitude larger in terms of mass than the projectile. This meant that the situation could not realistically be simplified as homogenous or layered. Because of these difficulties an experimental, rather than analytical, approach was adopted.

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### TEST MATERIALS

The composites were produced by mixing various proportions of sand filler, rock aggregate and electomer.

### Sand Filler

The mand filler reduced the amount of elastomer required to fill the void spaces between the rock aggregate particles. The effect of the mand particle size on penetration resistance was considered insignificant, so Sone II or Rone III ....! as defined by British Standard 882 : Part ? (5) was used in all composites.

### Rock aggregate

An advantage of the composites being exemined is that they are fairly economical because locally available aggregates may be used. To examine the influence of aggregate type on the penetration resistance of the composite, the main series of tests were carried out using three different aggregates: crushed limestone, crushed asalt, and river gravel.

The crushed limestone was a fine grained sedimentary rock, mid grey in colour and angular in shape with a significant amount of dust present. The crushed baselt was a fine grained clivine baselt, dark greyish green in colour and angular in shape with a significant amount of dust present. Must of the dust in these crushed rock aggregates was removed by sleving prior to mixing with the sand filter and elastomer.

The river gravel was predominately quartite and quarts, with small proportions of other rock types. The particles of the predominant rock types were rounded or irregular, but the minority rock type particles were of all shapes. Very little dust was present, because of the aggregate's mode of deposition from moving water which carried away the fines.

The properties of these rock aggregates as defined in British Standard 812 (6) are listed in Table 1. Also included in this Table are the percentage words for 27.5 - 37.5mm aggregate found using 300mm dis. x 300mm high cylindrical moulds as recommended in the British Standard, and using 152mm cube moulds similar to those used for composite specimen preparation.

### Elestomer

To achieve a relatively inexpensive composite which could be produced without special curing facilities and have a satisfactory penetration resistance within, at most, twenty four hours, it was essential to find an eleatomar which satisfied a number of criteria. The eleatomar had to be commercially available in large quantities at relatively low cost. For ease of mixing and casting it had to have a low viscosity and a gel time sufficiently long for casting. Thereafter it had to cure quickly at ambient temperature.

	Crushed Limestone	Crushed Basalt	Ri wr Gravel
Owen dry apecific gravity	2.67	2.75	2.57
Aggregate crushing value, %	23	17	-
Aggregate impact value, %	23	17	16
10% fines load (NN)	160	250	377
% voids - compacted B.S. cylinder test	430	43.0%	354
% voids - uncompacted B.S. cylinder test	49.3%	49.4%	39.41
% voids - uncompacted 152m; cube mould	52.16	49.49	43.71
% voids - compacted 152mm cube mould	140	451	39.14

Table 1 Rock aggregate properties

To act as a flexible binder at impact and during penetration the elastomer had to be elastic at high rates of strain. It also had to give a composite with adequate sechanical properties for large panels to be produced as cladding material or to form free standing units to a reasonable height.

Initially a "ide range of cold cure thermosetting polymers including epoxy resins, natural and synthetic rubbers and polyurethenes were examined. None of the sixteen polymers tested initially estisfied all of the criteria listed for the ideal elastomer. Polyurethenes were found to satisfy most of the criteria and two polyurethenes, a polyester polyurethene (Polymer A) and a blend of two polyether polyurethenes (Polymer B) were chosen for the main investigation. By varying the proportions of the polymer constituents different hardnesses of cured elastomer could be achieved.

### SPECIMEN PREPARATION

Single size rock aggregate wis used in all specimens and after sieving, the aggregate and sand filler were own dried. Mixing was cerried out using a mechanical boul mixer. The elastomer constituents were mixed for about 30 seconds to ensure complete bleading and then the rock aggregate and sand filler were added to the resin and the mixing continued for a further minute. The composite was cast in layers in 152mm concrete cube moulds, each layer being tamped in a consistent manner. Polymer A composites could be demoulded 1% hours after casting and Polymer 8 composites 1 hour after casting.

### TEST HE THOO

Test specimens with 152mm square face and varying thicknesses were fixed in a target holder which provided support round the tear perimeter of the specimen but with minimal lateral restraint.

Project.'ns were either 7.62mm NATO wall ammunition (mess 9.3g with lead elloy core) or 7.62mm NATO Armour Piercing ammunition (mess 9.6-9.9g with hardened steel core). Initially both types of ammunition were used, but indications were that armour piercing projectiles penetrated further than bell projectiles. Armour piercing project'les were therefore used in the main test series and after the composites had been optimised a subsidiary series of tests using bell ammunition was carried out on an optimised composite to confirm the lower penetrations.

The projectiles were remotely fired from a fixed pressure housing, bolt and barrel arrangement 20s from the target. A photodiode type velocity measuring rig was mounted 1.5m in front of the target and this allowed the projectile velocity to be checked. Nean measured velocity for ball ammunition was 794 m/s and for armour piercing ammunitum 507 m/s.

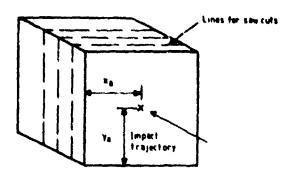
After testing target spacemens were sectioned as shown in Figure 1(a). This enabled the penetration depth of the projectile to be determined and the penetration path length could be calculated by taking coordinates as shown in Figure 1(b).

### OPTIMIZATION OF THE CONTROSITES

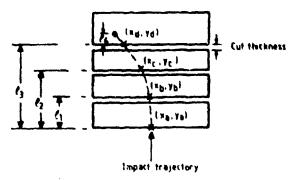
The fundamental aim of the project was to minimise the target thickness necessary to resist perforation, whilst keeping the cure time and the impact damage to the composite to an acceptable level. Thus the normal penetration depth, D, or penetration path length, D', were considered as alternatives for the design criterion. Initially the forms, was used but preliminary impact tests on composites showed that the penetration path rarely remained straight and normal to the impact face. The penetration path length was thun of more significance in assessing registance than the penetration Orpth, and was therefore used as the design criterion in the main series of tests.

In attempting to optimize the composites in terms of their penetration resistance of ere was a large number of independent variable which had to be considered for each rock aggregale/lastomer combination. These variables are instead in Table 2. It was decided to concentrate the main test programme on the four primary quantitative (x) variables at the top of Table 2, and to keep the other secondary variables or matant.

Morally the optimization procedure for four variables would be carried out by keeping three variables constant and varying the fourth. This would be repeated for each of the primary variables in turn. Thus sets of fitted equations



(a) ISOMETRIC ELEVATION ON IMPACT FACE



(b) PLAN ON SECTIONED SPECIMEN

Fig. 1 Target sectioning

Variable	Values in optimization programme
• polymer by weight in mix.x1	variable (7%-17%)
% rock aggregate by weight, x2	variable (44%-64%)
a sang filler by weight in mix	variable (194-494)
rock aggregate,x3 mm	variable (9.5-37.5)
polymer hardness, x4 Shore A0	variable (60-85)
specimen cure temperature, CC	ambient
specimen test temperature, oc	ambient
age of specimen, days	l day
specimen thickness, mm	152mm
bullet velocity, s/s	approx. 800 m/s

Table 2 Quantitative independent variables

\_ 1

would be obtained, each in only one x variable. From this stage, optimization can only be achieved by examining general trends and carrying out experiments on a trial and error basis. This method may require a very large number of tests and the inter-dependence of the variables may not be appreciated.

These difficulties were overcome by using a statistical method known as response surface theory, the general principles of which have been described by Cochran and Cox (7). Details of the application of this theory to the optimization of rock/elastomer composites are given by Anderson et al (8), and the mixes obtained from the optimization procedures are given in Table 3.

### THICKNESS TESTS

During the optimization test series targets which were expected to be sufficiently thick (152mm) to prevent perforation were used. Very occasionally perforation occurred when the worst combination of primary variables was used, but no perforations were recorded with optimum mixes. When each of the optimum mixes had been identified it was necessary to determine the specimen thickness,  $t_{\rm m}$ , which would contain the projectile with a given degree of confidence.

Two confidence levels were examined for the protective capability of the composite. The first, 80-70% containment, was thought to be applicable where the composite was to be used for protecting an existing reasonably strong structure, e.g. brickwork. Most of the projectiles would be contained, but those that were not would have their kinetic energy greatly decreased. The second confidence level, 97.5-99%, was considered sufficient where the composite was to be used alone, or over a weak structure.

Using specimens of verying thickness of optimized composites it was possible to estimate a thickness for each composite at which 80-90% containment would be achieved. Series of 20 tests on identical optimized specimens of this thickness were then carried out to check the 80-90% confidence level and to predict thickness for 97.5%-9% confidence. These tests showed that some adjustment of the mixes obtained from the main optimization test series was required for the Polymer B/basalt and Polymer B/limestone composites. Details of these tests and the various mix adjustmenets have been described by Anderson et al (8), and the results of thickness tests on all the final mixes are summarised in Table 4.

Polymer type	Rock type	* polymer by weight *1	% rock aggregate by weight *2	Rock size (mm) (nominal)	Polymer hardness (Shore A <sup>O</sup> )
А	River gravel	9	60	26.5 - 37.5	75
В	River gravel	9.8	59	26.5 - 37.5	80
В	Basalt	7	56	26.5 - 37.5	8C
В	Limestone	7	64	26.5 - 37.5	80

Table 3 Mixes obtained from optimization procedure

Polymer type	Rock type	* Polymer by weight *1	<pre>% rock aggregate by weight %2</pre>	Rock size (mm)	Polymer hardness (Shore A <sup>O</sup> )	t <sub>m</sub> for 80-90% confidence limits (mm)	tm for 97,5-99% confidence limits (mm)
A	River gravel	9	60	26.5 to 37.5	75	90	115
В	River gravel	9.8	59	26.5 to 37.5	80	75	100
3	Basalt	9	58	26.5 to 37.5	90	110	140
В	Limestone	11	59	26.5 to 37.5	80	100	130

Table 4 Summary of results from thickness tests

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### SUPPLEMENTARY TESTS

### Target Temperature Effects

In practical use the composite may be subjected to extremes of temperature and because the elastomer is very temperature sensitive, it was felt prudent to examine the protective capabilities of one of the optimized combinations (river graves/Polymer B) at temperatures other than ambient. Three series of twenty tests each were carried out three days after casting on identical specimens 80mm thick (80-90% confidence level). In the first series specimens, after curing, had been cooled in a freezer and the average specimen temperature at testing was -7°C. In the second series specimens were heated in an oven after curing and tested at a mean temperature of +34°C. The third series of tests was carried out on specimens cast, cured and tested at ambient temperature (+15°C). The results of the tests showed that higher than ambient temperatures had little effect on penetration resistance, but a low temperature increased the resistance. This increase in resistance was accompanied by increased brittleness of the target with much greater damage around the impact zone.

### Contact Explosive Tests

A limited series of tests was carried out to examine the resiscance of rock/elastomer composites to small explosive charges. Slabs 610mm x 610mm x 80mm of optimum mix of the best composite (river gravel/Polymer B) were cast and cured. Similar slabs of concrete were cast with the same proportions and size of river gravel and sand as in the composite slabs.

The slabs were placed on a steel sheet on the ground and a hemispherical charge of plastic explosive was detonated centrally in contact with the slabs. By trial and error the minimum charge required to defeat the slabs, i.e. cause dimintegration, was determined.

The results showed clearly the superior performance of the composite over concrete. A 50g charge caused only cratering of the composite slab with no cracking, indicating a high tensile resistance in the composite. A similar charge detonated on a concrete slab caused complete disintegration of the slab. Concrete was defeated by a 12.5g charge whereas the Linimum charge necessary to defeat the composite was 150g.

### COMMENTS

The tests showed that composites formed by binding rock aggregate together with an elastomeric matrix were effective in stopping small arms fire. The effectiveness of the composite depends on the constituents and the best performances were found with composites containing Polymer B. With all composites the optimized material contained the largest size gravel (26.5-37.5mm) which could easily be mixed with the resin and sand filler.

The aggregate type affects the penetration resistance. In particular, the harder the rock (as described by aggregate impact value) and the denser the rock particle packing (described by percentage voids), the greater will be the composite resistance. A guide to the necessary thickness of composite for any rock aggregate and for any particular confidence level is given in Table 5. It is suggested that the mix should contain 10% by weight of Polymer B (hardness 80 Shote A<sup>C</sup>), 60% rock aggregate of the largest available (up to 40mm maximum) and 30% sand. Rocks with aggregate impact values greater than 25 should not be used.

Confidence level	Aggregate impact value between 25 and 15	Aggregate impact value less than 15
801.	110 <del>cm</del>	95mm
901	120mm	105mm
951	1 3Omn	115mm
97.50	140mm	120mm
991	150mm	130mm

Table 5 Suggested thickness of composite containing untested rock aggregate

A major advantage of these composites is their early resistance to penetration. The material has sufficient cohesion for moulds to be removed after 1 - 15 hours. Static compression, bending and creep tests indicated full strength was achieved about eight hours after casting. These static tests also showed that the composite was strong enough for 80mm thick panels up 10 3m square to be handled, or for the material to be free standing to a height of 10 metres.

The limited meries of explosive tests showed promising results and this aspect of material behaviour should be further investigated.

### ACKNUMLEDGEMENTS

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BEHAVIOUR OF FIBER REINFORCED CONCRETE SLABS UNDER IMPACT LOADING

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### ABSTRACT

The behaviour of steel fiber reinforced concrete slabs under impact loads has been investigated. The results obtained show that fracturing and spallation effects are reduced to a large extend due to high energy absorption and the increased yield strength of this material. Crater depths are comparable to those obtained using normal concrete targets. Systematic tests using different fiber types and dimensions show that the terminal ballistic behaviour is strongly dependent on these parameters.

### INTRODUCTION

Concrete, as a wide spread and cheap building material is also preferably used for military shelter constructions. For this application its low yield strength and its brittle behaviour are of great disadvantage. These material properties lead to harmful spallation processes especially at the interior of building constructions. Considerable damage might be caused, even if the ballistic limit thickness is not yet over-come. An essential improvement of the protection properties of concrete can be expected, if a more plastic behaviour and an increased yield strength could be achieved. An appropriate means can be the mixing in of steel fibers. Many investigations concerning the behaviour of such fiber reinforced concrete under static loads have been performed. They show, that the application of steel fibers leads to a moderate increase of the yield strength, and to a considerable improvement of the plasticity. Though this material seems to be very promising also under dynamic loads, only few studies of its dynamic behaviour have been performed up to now. Therefore an extensive experimental program has been initiated at Ernst-Mach-Institut with the objective to study the behaviour of fiber reinforced concrete under dynamic loads and to optimize its composition.

### EXPERIMENTS AND RESULTS

For preliminary tests plain, normally reinforced and fiber reinforced concrete slabs have been produced. They have been impacted with steel dylinders (mass 50 g) in the velocity range between about 400 700 m/s. A comparison of the damage phenomena (Fig. 1) shows, that plates com-pletely brake and show rear side spallation effects already at impact velocities of about 400 m/s (Fig. 1, left). The normally reinforced plates not even brake at impact velocities of more than 700 m/s due to the high yield strength in the direction of the plate plane, however, rear side spallation is not suppressed by means of the reinforcement (Fig. 1, center). Up to more than 600 m/s the fiber reinforcement prevents fracture and spallation processes (Fig. 1, right). In addition it has been found that the fibers are of only minor influence on the crater depths. These tests show, that fiber reinforcement well suppresses damage due to shock wave propagation. By using several different types of fibers it became evident, that the fiber geometry is of great influence on the ballistic behaviour of this material.

Based on these results, an experimental program for the optimization of steel fiber reinforcement has been performed. In these experiments the dependence of the damage phenomena on fiber parameters was investigated. For this, planar impacts resulting in planar shock-wave loads have been performed. The projectiles were cylinders, made of fiber reinforced concrete, with diameters of 9 cm and thicknesses of 25 to 30 mm. Fiber parameters have been varied in the following manner:

### 1) Variation of the fiber content

The increase of energy absorption of concrete due to the fibers should be proportional to the fiber content. The influence of the fiber content on the

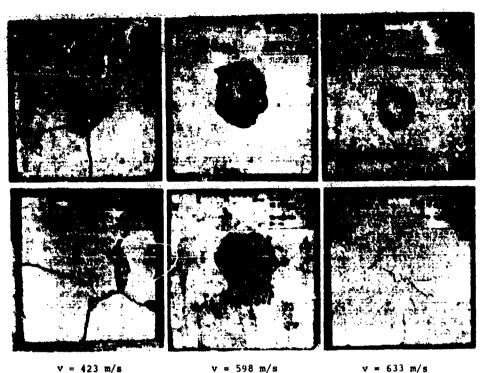


Fig. 1 Comparison of different concrete types

v = 633 m/s

reduction of braking and spallation proesses can only be clarified experimentally. Therefore a fiber type (0.4 x 25 mm) was used, which was easy to mix in. The degree of reinforcement was varied between O and 10 % by weight in steps of 2 %.

2) Variation of the fiber length at a constant fiber diameter

The energy, which is needed to pull out a fiber from the cement matrix is increasing with increasing fiber length. The force needed to pull out a fiber as well as the extension length are both increasing linearly with increasing fiber length. That means, the work needed for a complete disconnection is proportional to the square of the fiber length

- 3) Variation of fiber length and diameter at a constant L/D-ratio

It is not easy to predict the influence of the variation of these parameters, since opposite effects have to be taken in-

a) An increase of the fiber length and diameter leads to a decrease of the total surface for a constant fiber content and thereby the energy absorption is reduced.

b) See consideration to No. 2.

Concerning the variation of the fiber contents, it was found, that already a weak degree of reinforcement of only 2 % by weight leads to an effective suppression of braking and spallation. Only a gradual improvement is achieved, if the fiber content is increased up to 10 %. A quantitative charaterization of the damage phenomena at the rear side of the plates cannot be given due to extensive scattering of fracture data. Therefore, the plates have been sectioned. A distinct conical fragmentation zone can be observed within the slabs, the volume of which can be measured easily. This volume of highly fragmented target material can serve as an integral quantification of the target damage.

In Fig. 2 the volume of this fragmentation zone is plotted versus the projectile energy for different degrees of reinforcement. The relation is roughly linear, e.g. an approximately constant portion of the kinetic projectile energy is converted into fracture energy. The fragmentation zone is getting smaller with increasing fiber contents.

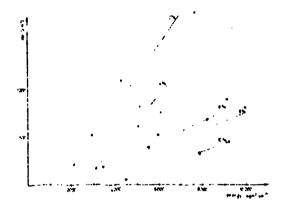


Fig. 2 Volume of fragmentation zone versus impact energy for different degrees of reinforcement

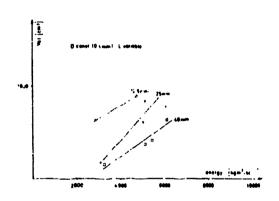


Fig. 3 Volume of fragmentation some versus impact energy for different fiber lengths and constant D

The variation of the fiber length at constant diameter shows, that a length increase leads to a reduction of the fragmentation zone, too (see Fig. 3). The results obtained by varying fiber length and diameter at a constant L/D ratio are shown in Fig. 4. The fiber of medium dimensions yields best results. The effectiveness of the small fiber is reduced due to a small stiffness and a bad adhesive strength. For the long fiber the mixing within the concrete is not sufficiently homogeneous and a predominant orientation parallel to the slab surface occurs. Considering all tests, the fiber with L = 25 mm and D = 0.4 mm was found to yield best results under ballistic loads. It can easily be mixed in up to relatively high degrees of reinforcement.

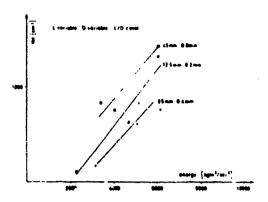


Fig. 4 Volume of fragmentation zone versus impact energy for different L and D and constant L/D

### SHOCK WAVE MEASUREMENT

Additional ballistic experiments have been performed in order to measure the shock pressure profile within the target. The experimental set up is shown in Fig.5.

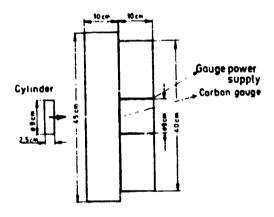


Fig. 5 Set-up for pressure measurement

A piezoresistive carbon gauge is mounted between two concrete slabs of 10 cm thickness each, which have been glued together. The gap between the plates where the carbon gauge is located, is only some tenth of a mm wide, that means the full pressure peak occurs at the gauge position. Fig. 6 shows a typical pressure signal for an impact velocity of 150 m/s. Since the electronic detection system was triggered at the time of projectile-target contact, the oscillogram also reveals the propagation time of the shock wave until it reaches the gauge. It was 25 µs and is

in good accordance with a wave propagation velocity close to the velocity of sound. Within 2 or 3  $\mu s$  the pressure rises to an amplitude of 9.5 10  $^{\prime}$  Pascal. The winth of the pressure maximum (12  $\mu s$ ) corresponds to the duration of the pressure phase at the projectile-target interface.



Fig. 6 Pressure signal

### CONCLUSION

Fiber reinforced concrete has very good properties with respect to dynamic loads due to its high energy absorption and a suppression of the rear side spallation.

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### EXPERIMENTAL MODELING OF STRENGTH AND DEFORMATION BEHAVIOR OF CONCRETE IN DIRECT SHEAR

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### ABSTRACT

Direct shear experiments on large prismatic specimens of plain concrete were conducted in a large capacity servo-controlled and structurally stiff test apparatus in order to assess the predictive capabilities of nonlinear computational analysis techniques. The objective in these expe-Timents was not to obtain material properties but rather to investigate load-deformation response behavior and attempth characteristics of a ministructure subjected to the complex states of nonproportional loading imposed by the direct shear test. The specimens were loaded to failure under displacement control and constant normal load. The complete spectrum of structure as well as material responses were observed including prepeak elastic-hardening plastic, post-peak strength strain-softening, and localisation of deformation into a shear band and continued shear gliding at a residual atrength level,

### INTRODUCTION

The direct shear translation test has in the past often been used rather frivolously to evaluate basic strength properties as well as shear stress-shear displacement response behavior of concrete and geomaterials. It has generally been assumed that the normal and shear stresses were uniformly distributed on the imposed shear plane. However, it is well established that both strain and stress distributions within initially homogeneousselid test samples are highly nonuniform during the experiment. The magnitude of the principal stresses varies nonproprtionally in the specimen and the principal stress directions rotate with respect to the material fabric to unknown extents during the shearing process, which in turn result in pronounced stress or deformation induced anisotropy. The overall sample response behavior therefore constitutes a combined response of a material that undergoes brittle and ductile fracture in tension and shear gliding. Proper material characterization for the purpose of obtaining basic engineering properties require homogeneous strain and stress states in the test specimen, and these do not exist in the direct shear test. This test is also highly sensitive to boundary conditions and the manner with which a centric or non-centric

tangential shear load is applied with respect to the shear plane. Several authors have discussed the merits of the direct shear test [1-4]. The shear test has been found to be a valuable tool for investigating residual strength characteristics of materials where shear bands or fracture zones already exist. It has also seen successful use for studying interface behavior between soils and structural materials such as steel and concrete. This aspect has been reviewed by 'essi [5].

In view of these considerations it was decided to adopt the direct shear test, not as a test for engineering properties, but as a miniature structure test where the boundary conditions can be carefully controlled and where complex states of tensile cracking and shear fracture can be studied. The direct shear structure test constitutes a controlled environment where the entire spectrum of the structure's and its material's responses can be followed through the elastic, hardening plantic, fracture, post-peak, strain-anftening, and residual atrength states. Investigations of brittle and ductile fracture transitions, progressive damage accumulation and localization of deformation in narrow shear bands in conjunction with degrading stressstarin or load-displacement relationships require A Very stable test system.

The general objective in this research effort has been to compare the measured response behavior to the computations; analysis predictions and to evaluate the capability of the so-called smeared fracture approach for describing progressive damage and frictional sliding along narrow shear bands. If this is achieved in the complex environment of the direct shear test, it is asserted that the computational analysis algorithm can model almost any three-dimensional boundary value problem involving brittle and ductile materials. The present paper covers apparatus description and the experimental technique used in the project. The computational aspects of this investigation are described in the companion paper by Willam [6].

### EXPERIMENTAL APPARATUS

The experiments were conducted in the high precision direct shear device shown in Fig. 1. The apparatus consists of loading actustors, normal and shear load reaction frames, normal and lateral

loading fixtures shown in Fig. 2. The top and bottom shear box compartments shown in Fig. 3 receive 20.3 x 20.3 x 10.2 cm (8 x 8 x 4 in.) samples of prismatic shape. In some instances the specimen width has been as small as 10.2 cm rather than 20.3 cm. The notched and un-notched specimens were fused to the shear box compartments by means of structural apoxy and conventional sulphur capping compound. In order to minimize a reactive moment about the average shear plane the shear lox is positioned in the holding fixtures and apparatus support system so that the applied lateral shear load and restraining action ite in the plane of induced shear failure. The top shear box compartment and holding fix. we remain stationary in the horizontal direction during shearing, while they are allowed to trans-late vertically. This feeture facilitates obervation of dilatancy. The restraining action in the horizontal direction is provided by means of a very stiff horizontal load support frame, which in turn is connected to an extremely stiff atructural floor by means of heavy holts. The top holding fixture together with the top shear box compartment can also undergo small roll and pitch movements in addition to the vertical translation. At present only one average vertical displacement has been monitored by means of a Linear Variable Differential Transformer (LVDT). It is planned to use three LVDTs at a later stage in order to define the rotational movements of the top portion of the specimen during and after fracture. It is also possible to lock the top entirely against rotations as well as vertical translation. The latter can be achieved through displacement control of the vertical actuator. Servo-controlled hydraulic MTS-actuators having 735 kM (165 kip) capacity in the normal direction and 156 kN (35 kip) in the tangential direction were used. The bottom shear box compartment and holding fixture have shapes and stiffness properties that are similar to the top components. The bottom sheer holding fixture is supported by two rows of heavy roller bearings which allow translatory motion of several centimeters. The bottom holding fixture is connected to the tangential load actuator by means of a large and stiff load transfer block (Fig. 2). The MTS control system 'an operate the apparatus under very slow or high displacement rates. Dynamic tests of rock joints subjected to large normal stresses and large relative displace ments have been successfully conducted in this device at frequencies ranging from nearly 0 to 10 Hz. Figure 3 shows a schematic illustration of the MTS and apparatus control system. The MTS hydraulic actuators operate independently in serarate closed-loop control systems. The Series 204 MTS actuators are equipped with Series 252 servovalves; beries 661 fatigue-resistant load cells; internal LVPTs; and swivel heads and bases. The control console is equipped with the following components: 430 digital indicator, 436 control unit, 410 digital function generator, and two 406 controllers, which are operated independently. Prior to testing a selection of force or displacement control for each 406 controller must be made. Once the mode of operation has been decided, the proper feed-back signal provided by the internal

LVDT or load cell, is compared with the input signal, If the signals are not equivalent, action is taken by the servo-valve to equilibrate the two signals. This is the basic feature of the closedloop system.

A Hewlett Fackard 3054 A Automatic Data Acquisition/Control System controlled by a HP 9825 T desk top computer was used as the primary control and data acquisition system. The 3054 A system contains a HP 3437 A System high speed voltmeter and a HP 3497 A Data unit scanner. The data collected by the HP 3054 A system were transmitted to the HP 9825 T computer and stored on tape. Real-time observations of load-deformation and strength behavior was recorded by means of an Esterline Angus xyy' 540 plotter. The relative shear displacement was measured by means of two 500HR-DC Schaevitz LVDTs whose feeler rods were inserted into the sample as depicted in Fig. 4. T' LVDTs were connected in series.

### EXPERIMENTAL TECHNIQUE AND RESULTS

Notched and un-notched plain concrete prismatic specimens having unconfined compressive strengths (f') ranging from 26.2 MPa to 28 MPa and unconfined tensile strength (f') of 4.1 MPa were initially subjected to nominal normal stress states that varied between 0.69 MPa and 6.9 MPa (100-1000 pai) prior to shearing. The lateral load was increased in displacement control at a constant rate of 0.05 mm/s.

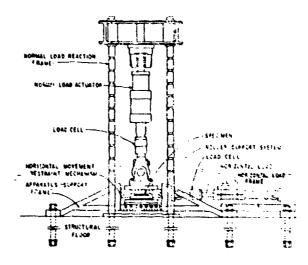


Fig. 1 large capacity direct shear apparatus

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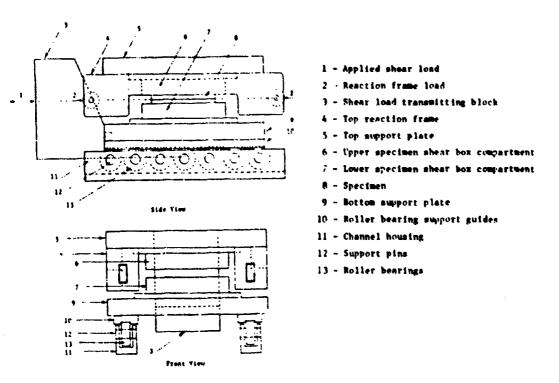


Fig. 2 Specimen holding fixtures and shear box compartments

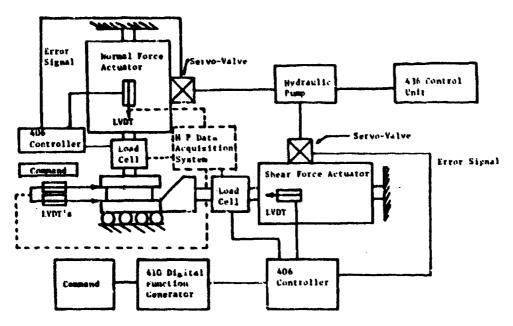


Fig. 3 Schematic diagram of apparatus and load control system

The notched and un-notched specimens' widths varied between 10.2 cm and 20.4 cm (4-8 in.), whereas lengths and heights were maintained constant at 20.4 cm and 10.2 cm in all tests. All specimens were savout to final size from over-size castings. The exterior side faces of the specimens were exposed for visual and photographic observation. Shear displacement measurements were obtained by LYPTs mounted on control rods embedded in the specimen through ports in the top and bottom shear box compartments. The spacing between the parallel rods varied between 3.8 cm and 10.2 cm in the tests. On one occasion the rods penetrated into the tensile fracture zone. Figures 4 a and b show the notched and un-notched specimens within the shear box compartments. The feeler-rods are shown in Fig. 4a. The specimen was notched at two opposite faces with 90° and 1.27 cm (0.5 in.) deep grooves in order to induce high stress concentrations near the ends. Figure 4s also shows the finite element mesh idealization used in modeling the notched grecimen test.

Specimen failure initiated due to tensile cracking rather than shear alip in both the notched and un-notched tests. This happened before any shear band formation. Crack openings were visible before shear failure took place in the center regime. Cracking also took place outside the notches, and fracture propagation from the notch surfaces only took place after significant crack development. Pronounced inclined cleavage cracks later developed across the notched section. In both specimen categories the tensile stress state was responsible for ultimate failure, although the nominal compressive stress on the shear surface was much higher in the un-notched case. Tensile cracking occurred under very small relative displacements, while shear fracture and subsequent gliding took place under relatively large displacements. The shear fracture propagation was rather slow in comparison with the tensile cracking events. Figure 5 shows photographs of the notched specimen prior to and after failure and the exposed bottom of the failed specimen after test disassembly.

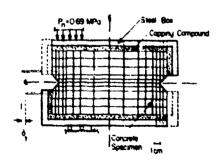
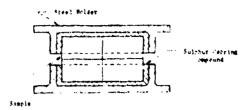
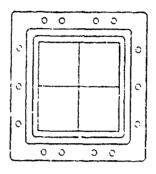


Fig. 4a Direct shear box compartment for notched specimen and LVDT gage rods

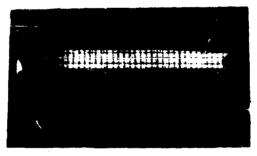


(side view)



(top view)

Fig. 4b Direct shear box compartment for unnotched specimen



(specimen before failure)



(specimen after failure)

Fig. 5 Failure behavior of notched concrete apecimen

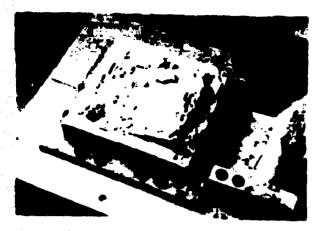


Fig. 5 [continued] Failure behavior of notched concrete specimen

No debonding was observed between apecimens and shear box compartments after the tests. Both specimen categories exhibited nearly linear elastic behavior before reaching peak strength. The nonlinear shear stress-displacement response is most pronounced in the un-notched specimen. Upon continued shearing the lateral force decreased in both specimens until a residual strength level was reached. The rate of softening and the residual strength levels are quite different due to the applied normal loads which were 143 kN in the un-notched case, which resulted in a nominal normal stress of 6.9 MFa (1000 psi), and 24.9 AN in the notched case, which resulted in a nominal normal stress of 0.69 MPa (100 psi). The residual friction angle (6) in both cases was found to be 35°. The stick-slip pattern on the shear stressshear displacement response curves shown in Figs. 6 and 7 indicates that shearing and crushing of clasts are far more pronounced for the high confinement un-notched specimen than for the low confinement notched specimen. The un-notched specimen was subjected to a small unloading-reloading cycle at approx. 70% of peak strength and sign!ficant permanent inelastic deformation was observed. It should also be noted that the relative displacements were recorded by having the LVDT measurement rods 3.3 cm apart in the notched specimen test and 10.2 cm apart in the un-notched specimen test.

The apparatus and test specimen configuration was essentially stable throughout the shearing process, although energy teleases in the post-peak strain-softening branch of the stress-displacement response diagrams indicate rate increases. Real-time xyy' plots of the events also gave this impression. Nevertheless, it is maintained that the atrain-softening branches in Figs. 6 and 7 represent true behavior of the concrete miniature structure subjected to defined boundary conditions.

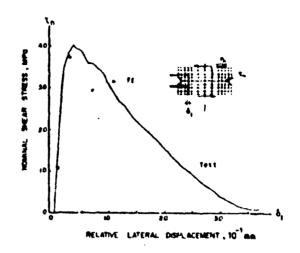


Fig. 6 Shear stress-relative displacement response behavior for notched specimen (nominal normal stress 690 kPa)

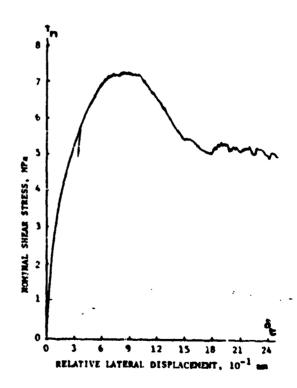


Fig. 7 Shear stress-relative displacement response behavior for un-notched specimen (nominal normal stress 6.9 MPa)

### CONCLUSIONS

It has been demonstrated that the direct shear test may constitute a favorable environment for evaluating load-displacement as well as nominal shear stress-relative displacement response behavior of small prismatic or other regularly shaped miniature structures of concrete or geometrials for the purpose of calibrating computational analysis procedures as well as constitutive models. The prismatic direct shear specimen is subjected to complex stress states that vary throughout the experiment. Issues related to tensile cracking and shear gliding as well as their interactions can be investigated in this test. The computational considerations associated with these experiments are described by Willam [6].

### ACKNOWLEDGEMENT

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### FINITE ELEMENT ANALYSIS OF CONCRETE FAILURE IN SHCAR

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### ABSTRACT

The main purpose of this study is to assess the current computational methods for predicting the failure behavior of concrete and geomaterials in the form of tensile cracking and frictional slip. The paper concentrates on the peak and post-peak response of plain concrete in shear which is modeled by the "smeared" finite element approach in which localized failure zones are distributed over a finite material region with softening material properties. The computational results are compared with experimental observations of plain concrete specimens which are tested in the large capacity servo-controlled direct shear apparatus described by S. Sture in the companion paper.

### /INTRODUCTORY REMARKS

In view of the importance of ductility to structural safety a comprehensive research project was recently initiated at UC, Boulder to examine different forms of local material failure and their effect on the response of the overall structure. The main purpose of this work is to scrutimize the value of the current computational strategies to predict progressive material instabilities withir the structure up to collapse of the entire configuration. Considerable criticism was voiced in the past whether the so-called "smeared approach" was capable to provide reliable predictions of structural failure. This computational strategy is normally adopted because the complex fracture process can be readily accompdated within traditional procedures for nonlinear material behavior in the form of an equivalent strain softening model. In this way progressive material damage may be accounted for in a conventional finite element program in the form of an averaging technique for highly localized deformations, discrete cracks and shear bands within the

Clearly local material failure implies in reality a change in the topology of the structure. Therefore, the alternative discrete fracture approach incorporates these discontinuities right from the beginning within the structural idealization. However, in three-dimensional components, the discrete fracture analysis involves definition of an initial fracture surface and rubsequent propagation with continuous changes of

the structural topology which simply overtaxes current computational facilities. Moreover, the specification of the underlying criteria for fracture initation and propagation as well as the definition of prevalent interface conditions introduce additional constitutive difficulties similar to the softening formulation in the smeared approach.

As a result of these controversial issues it is mandatory to scrutinize the shortcomings and limitations of the smeared and discrete failure models in the light of experimental evidence. To this end plain concrete specimens were tested in the large capacity direct shear apparatus which was developed by S. Sture at the University of Colorado, Boulder [1] and which covers the full spectrum of tensile cracking and frictional slip modes of failure. The direct shear specimen forms in reality a structural configuration rather than a material sample because of the non-uniform state of stress resulting from the complex boundary conditions as well as localized material failure. In fact the servo-controlled test set-up reproduces the stress transfer of highly indeterminate structures and covers the entire response regime including the post-peak behavior down to the residual strength response.

### RELATED RESEARCH

Due to rapidly increasing demands in computational mechanics and the electronic revolution in testing extensive research efforts are currently devoted to investigate failure in three areas:

- (i) Micromechanics of the underlying ductile fracture process
- (ii) Constitutive modeling of the material behavior for smeared and discrete failure studies
- (iii) Analysis of structural failure within the smeared strength of materials and the discrete fracture mechanics approach

For brevity only those contributions are cited here which are of immediate concern. The direct shear test is probably the oldest and most controversial experiment ever since it was adopted by Coulomb to study shear in soils. The under-

lying morphology and mechanics of discontinuities in the failure zone were examined among others by Morgenstern and Tchalenko [2] in overconsolidated clays. In a recent paper Vallejo [3] recognized that the development of shear bands is the result of different crack discontinuities rather than uniform frictional slip. In fact he claims that the formation of crack discontinuities precludes application of the Coulomb failure theory or alternative continuum models. Based on linear elastic finise element analysis of the direct shear test Kutter [4] noticed previously that tensile stresses remain insignificant for ratios of normal to tangential loading N/T >1. Moreover, he observed for the field of rock mechanics that the direct shear experiment on solid test samples is really not meaningful since the direction of initial slip surfaces does not coincide with the enforced direction of failure. As a result the direct shear test is certainly not the simple material test originally intended and thus requires a full stress analysis of the specimen similar to realistic structural components.

Palmer and Rice [5] adopted a discrete fracture mechanics approach for modeling the behavior of concentrated shear bands in order to interprete strong size effects. On the computational front Cleary and Dong presented recently a discrete interface model for failure in geological materials [6] combining finite elements with a surface integral technique considering the effect of a stationary shear band along a predetermined zone of weakness.

A fundamentally different approach was pursued by Rice et al [7,8] who studied the localization of deformation into a shear band in the form of constitutive instabilities in homogeneous deformations. Following the mathematical theory of bifurcation and uniqueness due to Hill they established conditions for material stability and found a high sensitivity with regard to "normality" and rate effects. Along similar lines Vardoulakis [9], Vermeer [10] and Darve [11] determined very recertly the critical orientation of shear bands in simple test configurations. In analogy to the linearized buckling analysis of structures these material stability studies yield the incipient failure mode for a homogeneous deformation state. However, in this form they provide no insight into the redistribution capacity and reserve strength of realistic structures with slow contained propagation of material instabilities within complex structural configurations.

On the computational front it is intriguing that the first finite element studies of reinforced concrete structures followed the discrete crack approach, see e.g. the state-of-the-art report in ref. [12]. Recently, this methodology has been newly interpreted in terms of the underlying fracture mechanics concepts by Hillerborg et al [13]. Ingraffea et al [14] developed on thic basis a discrete fracture analysis program for two-dimensional applications with sophisticated interactive remeshing capabilities. However, the bulk of

computational studies relied on the alternative smeared failure approach. The essential shortcoming of this strategy was retrofitted only recently by Bazant et al [15, 16] who adopted the fracture energy concept in order to account for size and gradient effects. The strain softening branch for tensile cracking depends in this case on the mesh size in order to insure mesh-independent release of fracture energy as failure propagates. For frictional slip and the mixed modes of failure a rational concept for simultaneous softening of the cohesive and tensile strength values is still missing and is therefore an immediate objective of the current investigation.

### COMPUTATIONAL STUDY

Preliminary results of the current research were presented in ref [17] which contained a detailed substructure analysis of the entire shear box. The purpose was to define appropriate boundary conditions for the actual test specimen which was sheared under displacement control in order to capture the softening regime (relative tangential displacements between the upper and lower halves of the shear box). Fig. 1 shows a typical finite element idealization of the entire shear box which includes the notched concrete specimen, the capping compound, the steel box and the loading frame.

In the main portion of ref [17] experimental data of the direct shear test were compared with the finite element solution using the smeared approach. One principal outcome of this study was that the direct shear test of concrete was in reality a tension test for the ratio of normal to tangential loading N/T = 1/6 at failure. Moreover, the shear test specimen behaved like a structural component with considerable redistribution capacity because of contained material instabilities due to the confinement of the shear box. The Mohr-Coulomb model with tension cut-off in Fig. 2 [18] reproduced fairly well the overall response behavior shown in Fig. 3 with material parameters which were obtained from separate material tests. As a result, the direct shear test could be utilized to verify the computational strategy for predicting structural response behavior in the pre- and post- peak regime. Clearly, the smeared approach did not model the localization of deformation into the discontinuous failure band shown in [17]. however, it was able to capture the stress redistribution and the propagation of material failure in the form of tensile cracking and frictional slip within the structure, see Figs. 4 and 5. Although the fracture energy concept for tensile cracking furnished a rational concept for strain softening as function of mesh size it did not resolve the fundamental short-comings with regard to localization. Moreover, a comprehensive theory for different fracture modes is still lacking, in particular for mode #2 type shear failure which is of primary interest in this context.

To this end a series of direct shear tests are currently on the way which are described in

the companion paper [1]. For different N/T loading ratios the catine failure spectrum is covered from predominantly tensile cracking to frictional slip.

The study below shows computational results for the second test series. The particular case is examined in which the shear box is preloaded with a constant vertical pressure of  $p_n=1$  ksi which corresponds to a load ratio of N/T=1 at failure. The idealization of the shear box is shown in Fig. 6 with 129 plane strain elements interconnected by 1105 degrees of freedom. before [17] the shear specimen as well as the shear box are included in the idealization in order to ensure centric application of the tangential force in the prevailing shearing plane.
initial test set-up was slightly modified to accommodate test specimens of different width. The actual size of the hexahedral specimen is in this case L\*H\*W = 8.0 x 4.5 x 3.0 in. The concrete specimen is fastened to the steel box with an epoxy layer which assures full bond even on the tensile side walls. The material properties were determined with a series of independent uniaxial and triaxial concrete tests yielding the following values

Elastic Stiffness: E = 3000 ksi

v = 0.20

Strength Values:

 $f_{c}^{t} = 4.7$  ksi  $f_{t}^{t} = 0.55$  ksi

c = 1.0 ksi and  $\phi = 40^{\circ}$ 

In the post-peak regime different softening models are currently examined along the fracture energy concept, whereby brittle collapse and plastic yielding of the tensile, cohesive and frictional strength values are limiting cases. The resulting shear behavior of the brittle strategy is reproduced in Fig. 7 in terms of the nominal shear stress on the prevailing shearing plane and the relative tangential motion of the lower steel box against the upper one. In this case the residual strength values for tension and cohesion are instantaneously reduced to zero when the stress path penetrates the failure surface while the residual friction angle is reduced to  $\phi_T=34^\circ$ . The response curve clearly illustrates the effects of local material instabilities in the form of oscillations before the overall degradation of strength takes place down to the residual strength level due to internal friction.

Fig. 8 shows the deformed mesh for the load point in the peak regime where  $\delta_{\pm} \approx 20.9 \times 10^{-3}$  in. Together with the plots of displacement vectors and principal stresses in Figs. 9 and 10 this problem illustrates clearly the stress redistribution into axial thrust action between the compressive side walls during progressive shearing and the extent of localized deformations in the specimen. In contrast to the usual notion of a horizontal shear band in yeomaterials the failure planes are in this case inclined parallel

to the direction of minor principal stress and a horizontal mode of frictional slip develops only in the final state of shearing. As a result this example demonstrates some of the limitations and capabilities of the smeared approach.

### CONCLUDING REMARKS

The computational study clearly illustrates the complex failure mechanisms of plain concrete subjected to shear. As a result the direct shear test is not a simple experiment for determining the stiffness and strength characteristics of a material, it is rather a structural configuration in which considerable stress redistributions take piace in the pre- and post-peak regime. Within limits the smeared approach models fairly well the propagation of local material instabilities due to tensile cracking and frictional slip within the structural configuration. However, it does not reproduce the localization of discontinuities failure zones except for a continuous band of failed elements with similar orientation of the individual fracture planes.

### **ACKNOWLEDGEMENT**

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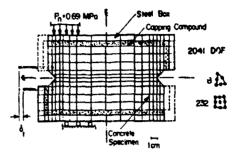
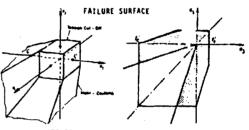


FIG. 1 IDEALIZATION OF DIRECT SHEAR BOX



TENSION AND COMESTVE SOFTENING

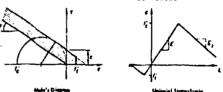


FIG. 2 SOFTENING MOHR-COULOMB MODEL
WITH TENSION CUT-OFF

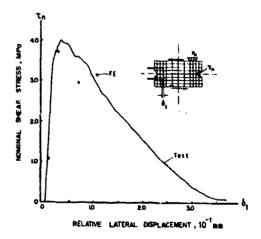
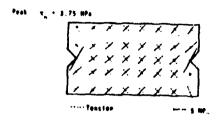
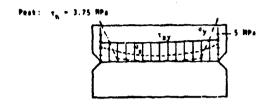
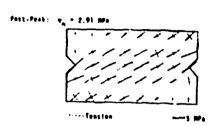


FIG. 3 SHEAR RESPONSE FOR LOAD RATIO N/T = 1/6







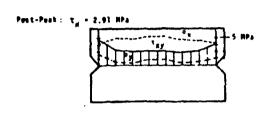


FIG. 4 REDISTRIBUTION OF PRINCIPAL STRESSES

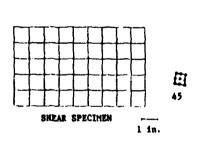
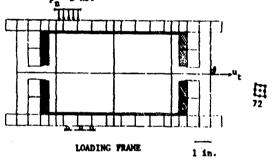
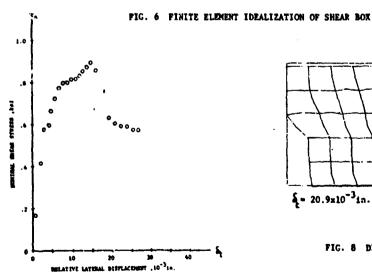


FIG. 5 STRESS DISTRIBUTION ON MOTCHED SECTION





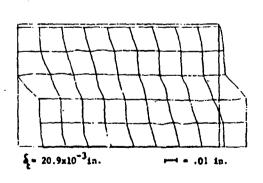


FIG. 7 SHEAR RESPONSE FOR LOAD RATIO N/T = 1/1

FIG. 8 DEFORMED MESH LAYOUT

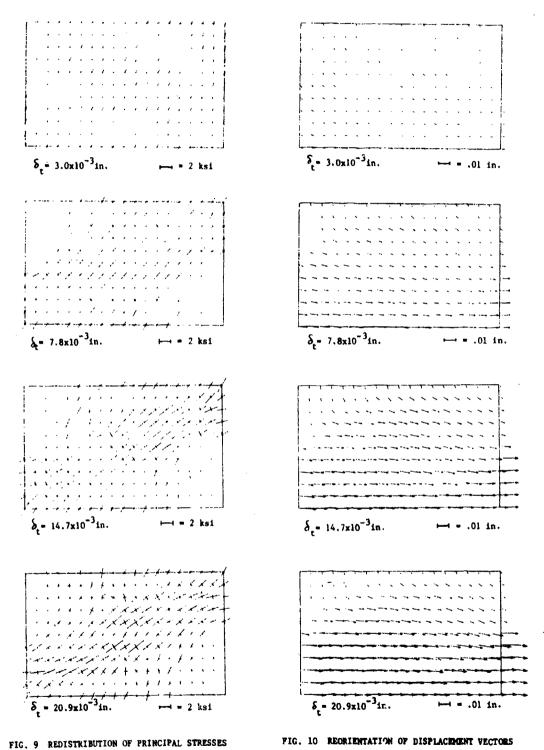


FIG. 10 REORIENTATION OF DISPLACEMENT VECTORS

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SHAKING TABLE TESIS TO EVALUATE THE LIQUEFACTION POTENTIAL OF NEAR SURFACE SATURATED SAND DEPOSITS

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### ABSTRACT

The design and implementation of largescale testing equipment for liquefaction studies of near surface saturated sands is reported. The test results can be used to determine material properties required for the development of constitutive relationships capable of describing the behavior of saturated sands during dynamic loading.

Specimens of saturated Ottawa sand 16.5 cm by 15 cm by 122 cm were tested and measurements of sample pore water pressure and accelerations taken during shaking. Results of the liquefaction tests have shown that, although qualitative agreement is achieved between the results of this program and those obtained in earlier investigations, the onset of liquefaction as measured in this study takes place at much higher stress levels than previously reported.

### INTRODUCTION

The cyclic behavior of soils has attracted considerable attention and extensive research over the last two decades, due mainly to the extensive damage observed in the Alaska and Hiigata earthquakes in 1964 (1), and to the more recent findings on the detrimental effects of blast-induced liquefaction (2). Liquefaction, as the term is used in this report, describes the complete loss of shearing strength of sands re-sulting from an increase in pore water pressure. This increase in pore water pressure is produced by vibratory loading under undrained conditions. Cyclic shear stresses induce saturated sands to compact, but compaction cannot occur under undrained conditions, and this leads to a transfer of part of the stress from the sand grains to the interstitial pore water. Continued cycling can lead to increasing pore water pressure up to the level of the initial confining pressure. The resistance to liquefaction for sands has been related to many factors but has been found to be primarily a function of the relative density of the sand, the initial effective confining pressure and the intensity of vibration.

A complete investigation of the behavior of saturated sands under dynamic loading would ultimately take the form of an analytical model based on fundamental stress-strain relationship for

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sand. The formulation of such an analytical model requires a basic understanding of the liquefaction phenomenon, with a clear definition of all factors involved, and an accurate representation of the important soil characteristics. However, since there is relatively little field data available on liquefaction, the material constants and coefficients which are needed are determined from laboratory tests. Therefore the accuracy and applicability of any analytical method can only be determined by evaluating how accurately the laboratory tests used to obtain the important soil properties actually simulate field conditions.

in the early stages of laboratory research work on soil liquefaction, the standard triaxial test apparatus was adapted for cyclic testing since it was and still remains the most widely used laboratory device for measuring strength, While such tests are relatively easy to perform, there are several features of the cyclic triaxial test which restrict the applicability of results obtained from tests using the device. These features include: stress concentrations introduced by the sample cap and base, redistribution of water content within samples, necking of samples on the upward stroke, variation of the intermediate principal stress, and rotation through a full 90° of the major principal stress direction during loading. An improvement over the triaxial test is the cyclic simple shear test. In this device samples are horizontally sheared in alternating directions by applying a shear stress to the top and bottom faces of the sample. The simple shear device clearly provides stress conditions in the laboratory closer to stress conditions in the field. However, it also exhibits certain undesirable features including: stress concentrations around the central zone of samples, complimentary shears not being developed along vertical faces of samples, and re-orientacion of principal stress directions causing patches of high and low stress along the top and base of samples.

Since the small-scale laboratory tests for determining liquefaction potential share the problem of close-in boundaries adversely affecting sample behavior, the use of larger samples would seem to be the best way of modeling "free field" conditions in a streable volume of sand. Thus large-scale tusting devices were introduced which could be mounted on a shaking table, and thus provide an excellent means of applying the required cyclic shear stresses to samples. Another advantage with large-scale tests is that small trans-

ducers can be placed inside samples to record the pore pressures, etc. without noticeably affecting the sample behavior. Several investigations have hern performed using large samples mounted on shaking table; including programs at the University of California (3) and at the University of British Columbia (4). In the tests performed at the University of California, Seed et al. subjected samples to time varying motions on a shaking table. Samples measured 90 inches long by 42 inches wide 4 inches high, and had sloped sides to avoid contact with rigid boundaries. A steel-shot ballast was placed over the sample to add mass and simulate a further 6 inches of sand, thus achieving shear stress levels sufficient to liquefy the samples. However this bailest was enclosed in a rigio boundary on four sides, was separated from the sample by a membrane, and contained a material of much higher density than the sand. The authors believe that this ballast did not effectively simulate a thicker layer of sand, but rather acted as a "dead weight," inducing faster buildup of pore water pressures.

Thus the main aim of the work reported herein was to design a testing system which could operate without the use of a ballast, and could apply either isotropic or geostatic  $(k_0)$  confinement to samples.

### TEST APPARATUS

The basic criterion followed in designing the apparatus used in the testing program described below was to make an assessment of the merits of previously used large-scale equipment, attempting to improve upon their ability to simulate fire field conditions, and to incorporate newly developed miniaturized transducers. The test chamber or "box" designed by the authors is illustrated in Figure 1 below.

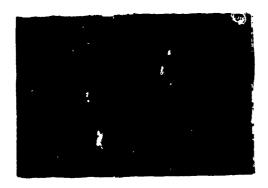


Figure 1: Test Chamber mounted on Shaking Table with iid removed.

Test specimens measured 112 cm (48 inches) long by 15 cm (6 inches) wide by 16.5 cm (6.5 inches) high, giving a length-to-height ratio in the order of 10:1 as proposed by Arango and Seed (5) for minimization of end effects. All parts of the test chamber were made of aluminum to minimize the

total weight. Samples were built while supported by retractable inner side walls, which after applying the confining pressure to the sample could be drawn back, enabling the specimens to deform free-ly under shaking in plane strain conditions. Several holes were drilled through these inner walls allowing transmittal of confining fluid to the sample (see Figure 1). Iwo separate fiber reinforced rubber membranes were used to seal the specimen, one flat sheet to seal the top of the sample from the lid and a long open rectangular bag-shaped membrane to seal the base and sides of the sample. Sealing the top of the sample separately from the sides enable anisotropic confinment to be applied if required. The confining fluid (water) was supplied through inlet ports in the outer side walls and lid of the chamber, and bleed lines were provided at the top of the side walls and lid to let out any trapped air. A drainage line was installed in the base of the chamber to allow consolidation of the sample under the static confining pressure. This drainage port was sealed from the confining fluid by screwing down the membrane into the chamber base using a washer. Fixing the washer around the drainage port then sealed the drainage hole in the membrane. A thin mat of highly permeable plastic material was glued to the lower membrane along the chamber base to ensure uniform sample drainage.

In order to record the behavior of the sample before and during liquefaction, instrumentation was designed to measure sample pore water pressure, sample accelerations, table accelerations, and sample displacement relative to the chamber. The table accelerations, pre-programmed using an MTS electro-hydraulic controller-actuator, were recorded by an accelerometer which was permanently mounted to the shaking table. All measurements of sample pore water pressures, displacements and accelerations were made in the middle third of the sample length, as shown in Figure 2 below.

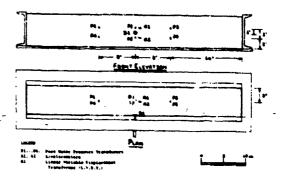


Figure 2: Relative Positioning of Instruments in Specimen

Accolerations of specimens were measured by two miniature accelerometers placed at the one and two third points of the sample height. This positioning would indicate any variation in sample acceler-

ation as a function of depth as pore pressures increased and liquefaction initiated. A linear variable displacement transformer (L.V.D.T.) was mounted on the side of the chamber to measure the displacement of the sample at mid-height relative to the chamber.

Based upon the assumption that the measurement of pore water pressure in samples is the most important record for invicating the onset of liquefaction, a total of six transducers were used to monitor the dynamic pore pressures. The trans ducers were placed as shown in Figure 2. The pore pressure transducers were modified so that sample pore pressures could be measured without placing the transducers in the sample. This was achieved by sealing a flexible six inch needle in the pressure sensitive port of each transducers, and then feeding the needle through the chamber wall and membrane into the center of the sample. The needles were sealed at the chamber wall and membrane using a silicon rubber sealant. Thus pore water pressures were measured in the sample at the point of a needle and transmitted to the transducers outside the chamber. All the data measured by the instruments during tests was recorded and stored digitally for inalysis at a later time.

### TEST PROCEDURES

A uniform Ottima sand (Cu=1.18) was used for all tests carried out on the shaking table. The sand was saturated by boiling under a vacuum using de-aired water. The sand was then placed into the specimen chamber under water in layers at zero drop height. The miniature accelerometers were placed by hand and gently covered over with further layers, making sure not to displace the sensitive axis off the horizontal zero-reading jostition. Extra care had to be taken in keeping air out of the s nd when placing the final layers of sand as there was only about a kinch of water above the finished surface of the samples. A roller device which could be moved along the chamber walls was used to smooth off the sample surface at the correct height.

Having prepared the sample, the top membrane was placed over the sample surface as shown in Figure 3, and the 11d holted down to seal the samply and confining fluid. Refore running a test the sample saturation was measured by increasing the contining pressure applied to the sample in steps, taking measurements of the sample pore water pressure each stap. Unce the confining pressure was applied, the inner walls could be drawn back to leave the sample free standing. With "a desired total confidence. a desired total confining pressure applied to the sample, the required effective confining pressure was produced by allowing water to drain from the sample, reducing the sample back pressure. Total confinement in tests was limited to 5 p.s.i., with effective confining pressures ranging from 3/4 p.s.i. to about 2 p.s.i. All tests were run at a frequency of 10 Hz. with accelerations in the order of 1 g. Each sample was vibrated for seconds and all the necessary data recorded. Each sample was vibrated for 150 After each test the lid and top membrane were

removed to examine the liquefied samples.

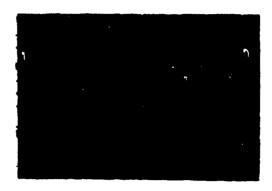


Figure 3: Sealing of top membrane over sample surface

### PRESENTATION OF RESULTS

The results of tests performed on three samples of saturated sand are presented. The data for each sample are given in Table 1.

Sample	0 <sub>r</sub>	8	ā ps 1	ä	1/c0	NL
1	56	1.0	2.0	1.20	0.274	1530
2	61	0.99	1.5	1.24	0.378	304
3	54	1.0	0.75	1.27	0.666	85

Table 1. Sample test data

Where: Dr is the relative density in percent; B is Skempton's pore pressure parameter; X is peak horizontal acceleration; g is acceleration due to gravity;  $\tau$  is shear stress on a horizontal plane;  $\sigma_0$  is initial effective confining pressure; N, is the number of applied stress cycles to reach liquefaction

Figure 4 presents results of the pore pressure response for Sample 2 at three different times during base excitation. It can be seen that when the pore pressure time history is superimposed on the on the sample acceleration time history, that both records are harmonic, and that accelerations are leading pore pressure. Peak pore pressures are reached at zero horizontal acceleration, i.e. when shear stresses in the sample are zero. The increase in the mean pore water pressure as a function of number of stress cycles is shown for Sample 2 in Figure 5. In this figure it can be seen that the rate of pore pressure increase is fairly uniform for the majority of the test. However, when the ratio of induced pore pressure to confining pressure reaches approximately 0.7, there is a sharp rise in the rate of pore pressure increase which leads to liquefaction in few additional cycles.

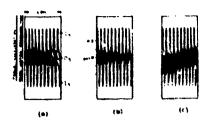


Figure 4: Samples of Pore water Pressure variation and table accelerations, Sample 42.

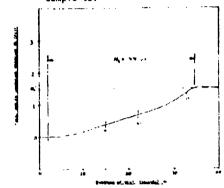


Figure 5: Porc water pressure response, Sample #2, Dr = 56%.

Neither the pore water pressure transducers nor the accelerometers located in the sample indicated any variation in the measured values as a function of location of the instrument during any of the tests conducted. The results of the program reported herein can best be compared with data obtained from other investigations by normalizing the cyclic shear stress with respect to the initial mean confining pressure. In Figure 6 are shown the results of this study compared with those presented by De Alba et. al (3).

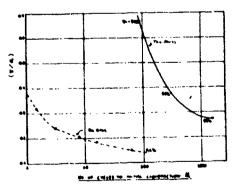


Figure 6: Comparison of Test Results with data from De Alba et. al (3).

### CONCLUSIONS

A new liquefaction device has been developed at The Ohio State University for Laboratory shaking table testing of sand samples. This equipment provides control over the main factors which affect the behavior of sand under dynamic loading. The test conditions created are thought to give a closer representation of actual field conditions than has some equipment used in previous investigations. The tests described herein have provided new information on liquefaction potential. While test results agree qualitatively with previous investigations, they do indicate a higher resistance to liquefaction than that indicated by other researchers.

It is felt that the primary reason for the difference in quantitative results presented in this paper and those of De Alba et. al. is the geometry of De Alba's testing device where boundary conditions might have caused a mure rapid increase in pore water pressure than would be expected under field conditions. Therefore current practice which consists of modifying the results of standard laboratory tests to make them consistent with the "more realistic" large sample shaking table tests may result in underestimating resistance to failure by liquefaction. A comparison should be made with the liquefaction behavior of sands predicted by analytical methods under similar conditions to assess the applicability of the results obtained in tests. Future tests should include more locations where pore pressures are measured in order to better determine whether or not pore pressure increase actu-ally is uniform throughout the sample as these tests indicate. It is further recommended that additional tests be performed on a variety of sample types under both isotropic and anisotropic stress conditions in order to substantiate the results of the initial tests presented herein.

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### SOIL CHARACTERIZATION FOR NON DESTRUCTIVE IN SITU TESTING

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AMALYSIS OF BURIED REINFORCED CONCRETE ARCH STRUCTURES UNDER DYNAMIC LOADS

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### **ABSTRACT**

A damped single degree—of-freedom model was developed to represent the gross dynamic behavior of shallow buried reinforced concrete arches subjected to specified nonuniform pressure distributions. Structural parameters were developed for a generic structure based upon available information in the literature and first principal calculations. Values of maximum crown deflection, calculated from numerical integration of the differential equation of motion, were compared with similar results from field experiments. Results utilizing structural narameters selected on this basis of the recommendations in this study provide the best agreement,

### INTRODUCTION

The objective of this study was to develop a single degree-of-freedom model capable of representing the gross dynamic behavior of shallow buried reinforcet concrete semi-circular arches subjected to specified input loadings resulting from the application of superseismic airblast loadings at the ground surface. Emphasis was placed on large deformation behavior approaching collapse. The soil was assumed to be dry and cohesionless.

### BASIC THEORY

In order to analyze a shallow buried structure, it is necessary to know the input load to the structure. The input load is not simply a function of the overpressure applied at the ground surface. It is also related to the flexibility of the structure, the characteristics of the soil type, and perhaps the depth of burial. Determination of the input load for an arbitrary loading function at the ground surface is beyond the scope of this study.

Crawford, et al. (1974) suggest that the general form of the nonuniform pressure distribution shown in Figure 1 is representative of a large majority of the actual loads encountered in the analysis of hardened buried cylinders. Their analysis for cylinders is directly applicable to fixed semi-circular arches.

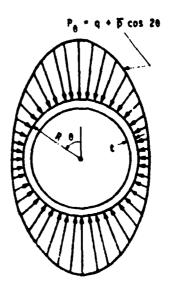


Figure 1. Circular Ring Subjected to Nonuniform External Pressure

They give the following results for the internal thrust (N), shear (V), and bending moment (M) resulting from the pressure distribution shown in Figure 1

$$N_{\bullet} = -qR + \frac{\overline{p}R}{3}\cos ?\bullet \tag{1}$$

$$V_{\Delta} = -\frac{2}{3} \vec{p} \sin 2\theta \tag{2}$$

$$M_0 = \frac{\overline{p}R^2}{3}\cos 2\theta \tag{3}$$

where q is the magnitude of the uniform component and  $\overline{p}$  is the maximum amplitude of the nonuniform component of applied external pressure. In this formulation the total nonuniform pressure distribution,  $P_{\theta}$ , is given by

$$P_{\mathbf{p}} = \mathbf{q} + \overline{\mathbf{p}} \cos 2\mathbf{\theta} \tag{4}$$

Crawford, et al. (1974) also indicate that the elastic deflection of a perfectly round ring subjected to the nonuniform pressure distribution of Figure 1 can be approximated by

$$\delta_{\Theta} = \frac{\overline{p}R^4}{9\Gamma\Gamma} \cos 2\Theta$$
 (5)

### SINGLE DEGREE-OF-FREEDOM MODEL

The maximum crown deflection relative to the support motion,  $\delta_{\rm C}$ , is chosen as the single parameter representative of the general arch response. The dynamic nonuniform, but symmetric, pressure distribution specified by Equation 4 is assumed to obtain and the first symmetric flexural mode shown in Figure 2 is assumed to govern.



Figure 2. Theoretical First Symmetric Flexural Mode

A viscously damped single degree—of-freed n system can be utilized to represent the secified conditions. The response of this system is defined by the following differential equation of motion:

$$M \stackrel{\circ}{\circ}_{C} + 2s \sqrt{kM} \stackrel{\circ}{\circ}_{C} + R(\stackrel{\circ}{\circ}_{C}) = \overline{p}(t)$$
 (6)

where M is the effective mass, B is the damping ratio or fraction of critical damping, k is the stiffness and  $R(\delta_C)$  is a generalized resistance function.

Solutions can be readily obtained for Equation 6 through the use of standard numerical integration techniques if the system parameters and the time varying maximum amplitude of the

nonuniform component of the applied external pressure are known. For the purposes of this study an assumed  $\overline{p}(t)$  will be utilized. This function can be obtained experimentally from interface pressure measurements in a dynamic structural test. Equation 4 indicates that  $P=q+\overline{p}$  at the crown and P=q at  $e=\pm45$  degrees. Thus, interface pressure measurements at these locations completely define the two parameters of the assumed nonuniform pressure distribution function.

### STRUCTURAL PARAMETERS

The structural parameters from Equation 6 which require specification are 8, M,  $R(s_c)$ , and k. These parameters are developed for a generic semi-circular reinforced concrete arch with the haunches rigidly connected to the floor. The assumed dimensions and material properties are as follows:

Radius, R = 47.2 in Haunch thi kness, t = 6.3 in Depth of over at the crown = 23.6 in Dense dry cohesionless soil Concrete strength,  $f_c' = 4500 \text{ lb/in}^2$  Reinforcement steel yield strength,  $f_y = 60,00 \text{ lb/in}^2$  Steel percentage, p = 1.45, each face Depth of steel cover = 1.165 in, each face sufficient shear reinforcement is provided to preclude shear failure.

Higgins, et al. (1981) presents results from extensive dynamic soil-structure interaction experiments on test structures resembling scale models of nuclear containment vessels. The reinforced concrete test structures were embedded in dry cohesionless soil from 25 to 200 percent of their height and were subjected to explosively induced ground motions which simulate the strong earthquake excitation of full-scale systems (structural accelerations in the 1 to 10 g range). They observed that damping was uniformly high, typically 10 to 20 percent of critical damping, at the high displacements corresponding to strong motion earthquake response. They further observed that damping typically increased with response level. Based upon this information, the large displacement interaction associated with shallow buried arches loaded close to failure should be highly dissipative with a damping ratio of 20 percent or more.

The effective mass of the shallow buried arch system can be developed utilizing energy considerations. Crawford, et al. (1974) indicate that a single load-mass transformation factor can be utilized to convert a distributed mass system into an undamped single degree-of-freedom model. They indicate that the value of the load-mass transformation factor ranges from 0.66 for a uniformly distributed load to 0.33 for a single concentrated midpoint load on a beam of uniform mass loaded plastically. The system under consideration consists of a uniform circular

team, with nonuniform depth of soil cover and spatially varying load. The amount of soil which should be included in the analysis is not known, but the full amount is commonly utilized for the analysis of shallow buried structures. A detailed analysis is not considered appropriate because of the large uncertainties associated with the formulation. A load-mass transformation factor of 0.5 is probably adequate for our purposes. Utilizing this value, an equivalent mass equal to 0.0045 lb-\$2/in³ is obtained for the combined mass of the reinforced concrete section and the average value of the soil cover for an assumed straight beam extending from a equal \* 45 degrees.

The resistance function can be derived from one of two possible approaches: evaluation of available experimental data or fundamental analysis of the reinforced concrete cross-section. Axial loads contribute significantly to the maximum resistance and beam-column theory is appropriate for calculating this value.

Meyer and flathau (1967) present experimental data for the response of unreinforced concrete fixed semi-circular arches buried in dry sand. Their data generally support the assumptions made in this study with regard to load distribution and general arch response. Figure 3 presents measured load versus crown deflection curves for static tests on arches with R/t values of 3, 6, and 12.

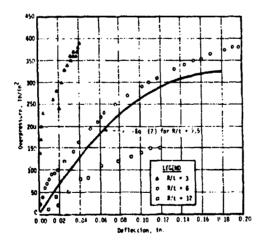


Figure 3. Static Surface Load Versus Crown
Deflection After Meyer and Flathau
(1967).

It should be noted that the load in this figure is the uniformly applied surface pressure rather than the maximum amplitude of the nonuniform component of the external pressure applied to the arch. It appears that the surface load versus crown deflection curves are generally parabolic in shape and that they are a linear function of R/t. The surface load versus crown deflection curve developed for R/t equals 7.5 (the value of the generic arch under consideration) is given by

$$F = -10,000 (s_c - 0.18)^2 + 324, lb/in^2$$
 for  $0 \le s_c \le 0.19$  in (7) .

Assuming that the uncracked moment of inertia is applicable because of the presence of the large axial thrust and that Equation 5 remains applicable at large deflections, \$\overline{p}\$ is found to be equal to 26 lb/in² for the generic section at a crown deflection of 0.18 in. This value corresponds to a surface overpressure of 324 lb/in². Because the response is well outside the elastic range the calculated value of \$\overline{p}\$ may be low by a factor of 2 or more.

Utilizing beam-column theory for reinforced concrete sections, see any standard text, the ultimate bending moment and thrust at the balance point for the generic section are found to be approximately 35,400 in 1b/in and 11,800 lb/in, respectively, when the static strengths of both the steel and concrete are increased by approximately 20 percent to account for the influence of dynamic loading. Assuming that the section will try to respond at the balance point and that Equations 1, 2, and 4 are applicable, values of P equal to 48 lb/in², n equal to 265 lb/in², and P equal to 313 lb/in² are obtained.

Anderson, et al. (1966) suggest that the crown deflection at ultimate load for a concrete failure strain of 0.003 can be calculated from

$$(a_c)_{u1t} = \frac{R(f_y/E_s)}{2\left\{1 - (\frac{87,000}{87,000 + f_y}) \cdot \frac{(3\frac{q}{p} - 1)}{(3\frac{q}{p} + 1)}\right\} }$$
 (8)

Utilizing the above results for  $\overline{\rho}$  and q, a value of 0.12 in is calculated from Equation 8 for the generic arch. The calculated values of  $(\delta_C)_{ult}$  and P are seen to be on the same order as the previously presented experimental data of 0.18 in and 324 lb/in², respectively. Utilization of an increased values of the concrete failure strain would further improve the agreement.

Park and Pauly (1975) recommend utilizing an idealized elastic-plastic approximation to the moment-curvature curve for a reinforced concrete section. Moment-curvature can be converted to load-deflection through the use of Equations 3 and 8. A proposed idealized elastic-plastic approximation to the load-deflection curve is shown in Figure 4.

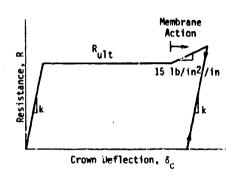


Figure 4. Idealized Elasto-Plastic Approximation to Resistance Function

 $R_{\rm u}$  )t and k can be arbitrarily defined. The slope of 15  $1b/\ln^2/in$  is included to represent membrane action which comes into play at very large displacements. The load-unload slope is arbitrarily defined to agree with the initial slope.

The following values of the structural parameters have been selected to best represent the generic structure under consideration:

s = 20 percent

 $M = 0.0045 \text{ lb-s}^2/\text{in}^3$ 

 $R_{ult} = 46 \text{ lb/in}^2$ 

 $k = 511 \text{ lb/in}^2$ 

### SEMSITIVITY STUDY

A sensitivity study was run for Equation 6 varying three of the four structural parameters, i.e.,  $\beta$ ,  $R_{0,1}$ , and M. Figure 5 presents a typical curve for the time variation of the maximum amplitude of the nonuniform component of external pressure,  $\overline{\rho}(t)$ .

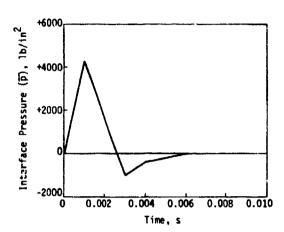


Figure 5. Typical  $\overline{p}(t)$  Curve

This loading function was utilized for all of the calculations in the sensitivity analysis. Haltiwanger and Hall (1979) have shown in a similar study of a shallow buried box structure that the solution of Equation 6 is most sensitive to the assumed loading function. Therefore, this study does not vary the most important, and possibly the least known, of the various parameters involved.

Table 1 presents the results of the sensitivity analysis calculations.

TABLE 1
SENSITIVITY STUDY RESULTS

Calculation	R <sub>ult</sub>	M	ß	k	<sup>δ</sup> c
Number	lb/in <sup>2</sup>	1b-s <sup>2</sup> /in <sup>3</sup>	%	1b/in <sup>2</sup>	in
1 2 3 4 5 6 7	46 46 46 46 46 46 92	0.0014 0.0014 0.0014 0.0014 0.0021 0.0045 0.0014 0.0021	0 10 20 30 20 20 20	511 511 511 511 511 511 511 511	26.8 13.3 8.7 6.4 6.9 4.6 8.1 6.4

These calculations indicate that the crown deflection is relatively insensitive to the value selected for  $R_{ult}$ . The response becomes less sensitive to the value of  $\mathfrak B$  in the 20 to 30 percent range and is most sensitive to the value selected for M.

Betz (1983) has calculated the crown deflections for several generic arches which were

subjected to a loading function similar to that shown in Figure 5. These results indicate that the relative crown deflections were on the order of 5 in or less. It is interesting to note that calculation number 6 utilizing the recommenced values of the structural parameters gives the best agreement with this result.

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### ACKNOWLEDGEMENTS

Support of this research by the Air Force Weapons Laboratory is gratefully acknowledged.



THE USE OF COMPENDIA, DESIGN MANUALS, AND REFERENCE TEXTS IN PREDICTION OF NONNUCLEAR WEAPONS EFFECTS

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### ABSTRACT

The literature on nonnuclear weapons effects dates from the 16th century, is extensive, is widely scattered, and includes many classified references. This diffusion presents problems to both neophytes and experts in this field — the neophyte can be overwhelmed by the volume of the literature, and unable to choose between conflicting references or prediction methods; while the "expert" may be expert in only a narrow specialty in weapons effects, and not truly conversant with other specialties. So, a limited library of broad references on the symposium topic can be very useful.

The broad references include compendia, design manuals and general reference texts. They give rather broad coverage, but the topics covered, depth of coverage, and accuracy and depth of reference to the literature vary considerably between the references. The paper will discuss the coverage of each cited general reference, will note the depth or lack of depth of literature reference, and will also give a brief evaluation of the reference.

### INTRODUCTION

Nonnuclear weapons effects include at least the effects on a wide variety of targets of: explosions and shock waves in air, water and the ground; impacts of penetrating projectiles and fragments; penetration by high-speed jets; incendiaries; smokes; and a variety of chemical agents. The spectrum of past, present and future weapons is very broad. The spectrum of "targets" is also very broad. Weaponry is an ancient discipline, and is also highly nationalistic. All of these factors combine to render the literature on the symposium topic voluminous, secretive and very diffuse.

If you are a neophyte to weapons effects, you can easily be overwhelmed by the extensive literature, and inconvenienced by the security classification of some of it. Even if you have been working in this field for many years, you may be rather unaware of some types of weapons effects, and are also inconvenienced by security restrictions.

We have found over the years that your work can be somewhat eased by using a <u>limited</u> basic library of unclassized references which contain useful technical discussions, data bases and/or analysis and prediction methods for a variety of weapons effects. Some of these broad references are obvious and well-known; others are not. We have found

some to be much more usefu" than others. Some have been quickly outdated, which there retain remarkable usefulness after many years.

This paper presents the author's suggestions for a limited library of broad references which can be useful in describing and evaluating nonnuclear weapons effects. Only unclassified references are included in the list. All were at one time easy for anyone to acquire, but some may now be quite difficult to get. We review in this paper only references in English.

The broad references are divided into three categories, i.e., compendia, design manuals and reference texts. They are discussed in that order. For each reference, we identify it, and then briefly discuss those contents relating to weapons effects. Depth of literature coverage is noted, as are strengths or shortcomings. Usually, the discussion is the author's, but in some instances, reviews by others are substituted. When this is done, the review is in quotes, and the name of the reviewer is included.

The paper includes a brief closure, which includes some discussion on availability of these references.

### DISCUSSION OF COMPENDIA

Because compendia usually consist of groups of papers or chapters by different authors, the adequacy of coverage of specific topics tends to vary considerably from chapter to chapter. But, there are some exceptions to this rule in our list, as noted.

White, M. T. (Editor) (1946), Effects of Impacto and Explosions, Summary Technical Report of Division 2, National Defense Research Council, Volume 1, Washington, D.C., AD 221-586. (Ref. 1)

Although this reference is rather old, it is a thorough review of U.S. research studies during World War II on explosions in air, water, and earth; ballistic impact effects on steel, concrete, and soil; gun muzzle blast; dynamic materials properties; protection against various weapons effects; and target analysis and weapon selection. Some of the Weapon Data Sheets included in the compendium, particularly those on penetration of projectiles into various media, are useful. The reference list is extensive.

The discussions and descriptions in this work are very clear and readable, and some of the compiled and scaled test data are still the most definitive available. Unlike many other compendia, treatment of <u>all</u> topics, by the various authors, is excellent and thorough. This is a <u>must</u> for your reference shelf.

Annals of the New York Academy of Sciences (1963), Volume 152, Article 1, "Prevention of and Protection Against Accidental Explosion of Munitions, Fuels and Other Hazardous Mixtures," October 28, 1968. (Ref. 2)

This is a very unusual source giving information on accidental explosion; and their effects, but this one volume of the Anzals contains a wealth of useful information in papers contributed by many researchers and safety engineer from the U.S. and Europe. The quality of the individual papers ranges from excellent to fair. Host of them reference the literature well, but a few omit a number of key references to prior work on the paper topic. The sections most applicable for predicting weapons effects are Part II. Personnel Sensitivity; Part III. Sensitivity of Explosive Materials, and Part IV. Explosive Effects.

Swisdak, M. M., Jr., "Explosion Effects and Properties: Part I - Explosion Effects in Air," NSWC/WCL/TR 75-116, Naval Swrface Weapons Center, White Cak, Silver Spring, Maryland, Cat 1975, AD A018 544. (Ref. 3)

This is an excellent compendium giving properties of air blast waves from nonnuclear weapons. The emphasis is on presentation of graphs and equations, and on example problems for their use. Included also are data on air blast from shallow underwater and underground explosions, and cratering for buried explosions. The compendium is based primarily on work in U.S. Navy laboratories, and this is well referenced. A weakness is that the extensive related work by U.S. Army, U.S. Air Force and foreign sources is largely ignored.

Swiedak, M. M., Jr., "Explosion Effects and Properties: Part II - Explosion Effects in Water," NSWC/WOL/IR 76-116, Naval Surface Weapons Center, White Oak, Silver Spring, Maryland, Feb 1378, AD A056694. (bef. 4)

This is the counterpart to the preceding compendium, but for underwater explosion effects. The type of coverage is similar, with coverage of similitude relations, underwater shock wave parameters for shallow and deep explosions, bubble pulse characteristics, underwater shock from line charges, and related topics. This compendium should be considered as a supplement to Cole's book, Underwater Explosions, which will be discussed later. The literature is well referenced.

"Behavior and Utilization of Explosives in Engineering Design and Biochemical Principles Applied to Chemical Medicine," <u>Proceedings of the 12th Annual Symposism American Society of Mechanical Engineers</u>, Acu Exrico Section, March 1972. (Ref. 5)

The first part of this compendium includes a number of well-written papers on detonation of explosives and their utilization. Its value lies in good descriptions of explosive processes, how explosives accelerate materials, and how materials respond to intense explosive loading. Most of the papers are excellent, and well-referenced.

Doering, W. and Burkhardt, G., "Contributions to the Theory of Detonation," Translation from the German as Technical Report No. F-TX-1287-IA (GDAM A9-T-4G), Headquartors, Air Material Cornent, Wright-Patterson AFE, Chio, May 1949, AD 17863. (Ref. 6)

Much of the German work during World War II on detonation of explosives, and shock transmission through air, water, and at interfaces between media is included. The treatment is very lucid, even in translation. Reference is, of course, almost exclusively to German work. One of its most useful aspects is the presentation of equations for predicting shock strengths on reflection from or transmission between different media.

### DISCUSSION OF DESIGN MANUALS

There are available a number of man als for prediction of explosion and impact loads on structures, and design of structures to resist such loads. Most are intended for use by structural engineers, and they concentrate heavily on presentation of design equations and graphs. A number of weapons effects can be predicted from information in most of the manuals.

U. S. Army Material Command, Engineering Design Handbook: Principles of Explosive Behavior, AMC Furphlet AMCP 706-180, 1970. (Ref. 7)

This is one in an extensive series of Army design manuals. It includes very thorough, well-written, and well-referenced material on the detonation physics of explosives. It will not allow you to numerically predict many weapons effects, but it should give you a good understanding of the physical processes occurring when explosives detonate.

"Fundamentals of Protection Design (Non-Nuclear)." Department of the Army Technical Manual, TM 5-855-1, Department of the Army, July 1965. (Ref. 8)

This was one of the first design manuals for protective structures. It was based on work by MIT and University of Illinois structural engineers, and includes some information useful in estimating weapons effects. Like some other manuals, a weakness is inclusion of only a bibliography, and rot specific references. It has now been superceded by later manuals.

The Army Engineering Handbook Series includes several other esquals which are very useful in predicting wespons effects, but they are classified and so do not qualify for our list.

## **BEST AVAILABLE COPY**

"Suppressive Shields Structural Design and Analysis Euclideck," U.S. Army Corps of Engineers, Huntsville Division, ENDM-1110-1-2, 1977. (Ref. 9)

Suppressive shields are structures (usually vented) designed to arrest fragments and attenuate blast and fireball effects for accidental explosions in munitions plants. This manual includes a number of topics which can be quite useful in estimating weapons effects, including prediction methods and data for free-field blast waves, blast loading of structures, internal explosion blast and gas pressure loads, and fragment impact on structures. Fresentation is clear, and sources are well referenced.

Crumford, Robert E., Higgins, Cornelius, C., Bultrunn, H., "The Air Force Manual for Design and Analysis of Hardened Structures," Report No. AFWL-TR-74-102, Contract No. F29801-74-C-9018, Civil Ruelear Systems Corporation, Albuquerque, New Mexico, October 1974, Second Printing October 1976. (Ref. 10)

This manual is intended for design to resist nuclear weapons effects, but it still contains material useful in estimating some nonnuclear effects. The useful parts are those on air blast phenomena, and ground shock and cratering. The treatment of structural response and damage largely repeats that in Ref. 9 and 20. Referencing is extensive and good.

Structures to Resist the Effects of Accidental Explosions, Department of the Army Technical Manual TM 5-1800, Department of the Navy Publication NAVFAC P-397, Department of the Air Force Manual AFM 89-20, Department of the Army, the Navy, and the Air Force, June 1869. (Ref. 11)

This design manual is the "Bible" for most structural engineers involved in blast-resistant design in reinforced concrete. Its strengths are in presentation of detailed procedures for estimating blast loading for internal explosions, failure modes for reinforced concrete, structural elements, and design of reinforcing. Basic structural design procedures are identical to those presented earlier by MIT authors.

There are data and prediction methods for estimating free-field blast wave properties, internal and external blast loads on structure, fragment impact effects on structures, and blast effects on humans. Descriptions of blast loading and its effects are quite good. A weakness is complete lack of referencing, although there is a reasonably complete bibliography.

This manual is now being revised and updated. Unfortunately, the weaknesses in lack of referencing will <u>not</u> be corrected.

Baker, W. E., Westine, P. S., Kuless, C. C., Wilbeck, J. S., and cox, P. A., "A Manual for the Prediction of Blast and Fragment Loading on Structures," (1980), DOE/TIC-11268, U.S. Dept. of Energy, Amarillo, TX, Nov 1980. (Ref. 12) This voluminous work is directed toward structural engineers who design blast-resistant structures for accidental explosions involving high explosives. Many graphs and equations, and many example problems are included. Topics covered are air blast from single and multiple high explosive sources, both bare and encased; blast loading of structures for internal and external explosions; cratering and ground shock for explosions in earth-covered structures; and a very detailed treatment of fragmentation and impact effects of fragments. General information is given on dynamic properties of constructural design. Referencing is thorough, and an extensive bibliography is also included.

### DISCUSSION OF REFERENCE TEXTS

There are a number of reference texts which provide very useful information relating to nonnuclear weapons effects. But, very few give direct prediction methods for such effects. It is suggested that the reader study them primarily to try to understand the physics of the complex processes occurring, for information on computational and experimental methods, and as general background reading.

Zel'dovich, Ya. B., and Razier, Yu. P., Physics of Shook Waves and High-Temperature Hydrodynamic Phenomena, Vol. I, Academic Fress, N.Y., 1966. (Ref. 23)

Zel'dovich, Ya. R., and Ranier, Yu. P., Physics of Shock Waves and High-Temperature Rydrodya 45 Phenomena, Vol. II, Academic Press, N.Y., 1967. (Ref. 14)

This two-volume work is a translation from the Russian. If you want to make a detailed study of the title topic, it is must reading. The treatment is very thorough, but also very readable. Reference to related work world-wide is thorough.

Johansson, C. H. and Persson, P. A., <u>Detonics of</u> <u>High Explosives</u>, Academic Press, London and New York, 1970. (Ref. 15)

"This is a thorough treatment of almost everything that is known about liquid and solid explosives. It should be the first source for anything you want to know. It also contains many excellent modern references." (W. C. Davis, in Ref. 5)

Cook, M. A., The Science of High Explosives, Reinhold, NY, 1958. (Ref. 16)

"Here we have many useful data, lots of phenomenology, and interesting pictures. Unfortunately, there is also a great deal of interpretation which is not accepted by other workers in the field, and a newcomer to the business has a hard time deciding what to believe and what to reject. My advice is to use it as a very valuable source of data, but to be careful about accepting the discussion and conclusions." (W. C. Davis, in Ref. 5)

Kinney, G. F. (1962), Explosive Shocks in Air, MacMillan, New York, New York. (Ref. 17)

For the pears, this was one of the few readily available references on air blast waves. It evolved from a course taught by its author of the U.S. Naval Postgraduate School. But, the material is relatively superficial and does not at all reflect the breadth of experimental and analytical work which had been done before it was published. Literature citations are very limited. It has been supplanted by later and more comprehensive works.

Ruker, W. E. (1973), Explosions in Air, University of Taxas Press, Austin, Texas. (Ref. 18)

"Although this book will not satisfy all the requirements of either the casual, neophyte, or experienced investigator, it provides by far the most comprehensive treatment of the subject available in a single volume, and as such it offers something worthwhile to all. A good by lance between theoretical and experimental approaches is maintained throughout the book with adequate mention of theoretical—experimental relationships and their importance to the understanding of the blast phenomena or solving practical explosion problems."

"Baker does a good job of describing many types of instrumentation in current use for laboratory or field applications. Mechanical, electromechanical, and piezoelectric gages are discussed. Mechanical, CRO, magnetic tape, and photographic systems and techniques for recording transducer output or blast phenomena directly are given adequate treatment."

"In light of the rapid changes in instrumentation available for researchers' use, it would have been well to devote a page or two to the requirements of a blast-measuring system. A curve showing frequency response requirements versus charge weight (or energy, the term Baker is prone to use) would have been quite helpful."

"The relatively large bibliography is a fine feature; the serious investigator is given guidance to sources in greater depth."

"All in all, Baker's Explosions in Air is a welcomed and noteworthy addition to a sparsely documented field." (J. F. Petes, book review)

Honoych, J. (1979), "The Dynamics of Emplosion and Its Use," Amsterdam, Elsevier Scientific Publishing. (Ref. 19)

This book is a very useful reference work, but flawed. In some respects, it is encyclopedic, with coverage of many aspects of explosions of chemical high explosives and the effects of such explosions in air, water, and earth. Some treatment of nuclear explosions is also included. But, like an encyclopedia, coverage of some topics is shallow and does not reflect the depth of material available on these topics.

Topics which are well covered include the stress wave theory, detonations and close-in effects of explosions in high explosives, explosions in soils, underground blasting and cratering,

and response of elastic and elastoplastic structural elements to blast loading. Coverage of elastic vibrations of structures is particularly exhaustive. Topics covered in a more superficial manner include explosions in air, explosions in water, use of explosives in demolition and seismic effects of explosions. Scaling laws for explosions in air or water, which are essential to these topics, are barely mentioned.

As is probably natural for a book written in Czechoslovakin, references to work in eastern Europe and Russia are extensive, and the inclusion of such references is very valuable for western readers. But, many readily available references from the United States and other western world sources are lacking, and many of the references which are listed are now dated and superceded by later work. In general, there are too few references to work more recent than 1969.

The writing is clear and the exposition easy to follow, but in some instances, too much mathematical detail is included. We would have preferred to see less mathematical development and more experimental data verifying some of the theory.

In nummary, this is a voluminous book containing much useful information on detonative explosions of chemical explosives, effects of these explosions, and a number of peripheral topics. But the reader is cautioned that the coverage is quite incomplete on some topics, and perhaps too detailed on other topics. References to good recent works in this field are also omitted.

Normis, C. H., Hansen, R. J., Holley, M. J., Eigas, J. M., Namyet, S. and Minami, J. V., Structure! Design for Punamic Loads, NaGraw-Hill Book Co., NY, 1988. (Ref. 20)

This book first appeared as a set of course notes for a short course taught by MIT staff. Procedures carry over directly from an earlier U. S. Army Corps of Engineers manual. As with the Army manual, these methods reappear in many later manuals. It is an excellent introductory text for response of dynamically-loaded structures.

Bigge, J. M. (1964), Introduction to Structural Lynamics, McGrew-Hill Sook Company, New York, New York, (Ref. 21)

This is an excellent introductory text for any engineer engaged in dynamic structural design. Biggs is one of the authors of the earlier Army Corps of Engineers manual, and Norris, et al. (Ref. 20). This book draws heavily on the earlier work, but adds considerable material. Presentation is very clear and understandable.

Baker, W. E., Cox, F. A., Messine, P. S., Kuless, J. J., and Strehlou, R. A., Explosion Kneards and Englantian, Elsevier Scientific Publishing Co., Amsterdam, 1983. (Ref. 22)

This new book discusses a variety of types of explosion sources, and presents methods for estimating air blast loads on and within structures,

some classes of fragment formation and impact effects, simplified and more complex methods of predicting structural response and damage from blast loading, and thermal radiation effects from nonnuclear explosions. Referencing is thorough, and there is an extensive bibliography. A number of example problems illustrate the prediction methods.

Collemith, W., Impact, the Theory and Behavior of collising Solids, Flanci Arnold, Iti, London, 1960. (Ref. 23)

This text gives very thorough coverage of the title topic, both theory and experiment. If you have any interest in the elastic and plastic processes invoived when solids collide, you should have this book on your shelf (or desk). The references to the literature are as complete as you could hope to find. [In fact, the earliest reference starts, "Galilei, G.... (1638)." It seems unlikely that Professor Goldsmith missed any significant references to this topic between 1638 and 1960!]

Zukas, J. A., Nicholas, T., Swift, H. F., Jreszczuk, L. B., and Jurran, D. R., <u>Impact Dynamics</u>, John Wiley & Jons, New York, 1982. (Ref. 24)

In recent years, the power of new computers has allowed numerical solutions to the complex sets of differential equations, describing the impact, and resulting deformation and penetration processes occurring in high-speed impacts. Experimental methods have also advanced to allow some observation of the dynamics of these very fast processes. This book covers both of these aspects of high-speed impact quite well. If you are interested in modern technology in this field, you should get this book. Presentation is graphic and clear, and all at trees are well referenced.

Kiekman, M. E., Tellminil Ballistics, NWC II 8.83, Naval Meapons Center, Chini Like, CA, Feb 1976. (Ref. 25)

This book is in reality a report, but it is included because of its direct applicability to nonnuclear weapons effects. It is a primer in ballistics, and as such does not go deeply into any topic. It should make good initial reading for the necephyte, but it should be quickly supplemented by more detailed references. The reference list in the report is quite limited.

Cole, R. H., Underwater Explosions, Princeton University Press, Princeton, NJ, 1948 (Reprinted by Dover Publications, 1965). (Ref. 26)

This is an example of a reference which is truly unique in a field. Cole's book covered U.S. and British research, both analytic and experimental, on underwater explosions during World War II. There is no other comparable reference on this topic, and much of the material in it is an useful now as in 1948. Swisdak's compendium (Ref. 4) adds some never work, but also relies very heavily on Cole's book. If you are interested in underwater explosions, you must get a copy of this book.

Baker, W. E., Westine, P. S. and Podge, F. T., Similarity Methods in Engineering Pynamics, Hayden Book Co., New Rochelle, NJ, 1978. (Ref. 27)

The predecessor to this book was a set of notes for a short course on scale modeling of weapons effects. The book is expanded considerably beyond that scope, but it contains chapters on scaling of air blast waves and impact forces, scaling of dynamic elastic and plastic response of structures, scale modeling of penetration mechanics, modeling of rigid-body dynamics of structures, and scaling of cratering from buried explosions. The reference list is thorough.

There are a number of example problems, keyed to individual chapters.  $% \left( \frac{1}{2}\right) =\frac{1}{2}\left( \frac{1}{2}\right) +\frac{1}{2}\left( \frac{1}{2}\right) +\frac{1}{$ 

### CLOSUKE

The limited list of broad references reviewed in this paper have, for the most part, proved very useful to staff members at Southwest Research Institute in prediction and evaluation of a number of conventional weapons effects, even though only a few of them were intended for that purpose. We have found that having a reference shelf with general, unclassified references of this kind is often far more valuable than having many file cabinets full of classified references.

Let us comment on the availability of the 27 general references on our list. Those which have an accession number for National Technical Information Services (NTIS) are readily available at a nominal cost, and we have given those numbers which we know. Procedures for obtaining the design manuals are often more difficult. You must usually contact the sponsor for the manual preparation and beg for a copy. Obtaining the never reference texts in our list is not difficult, provided you are willing to pay the (sometimes outlandish) purchase price. Any published more than 10 years ago are probably out of print, and thus obtaining a copy can be quite difficult. Unfortunately, for a few very useful references such as Refs. 2 and 5, extra copies are now almost impossible to obtain, and you must rely on friendship with someone who happens to have access to a few spare copies.

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X

## ANALYSIS OF CONTAINMENT RINGS FOR FLYWHEEL BURST PROTECTION

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### ABSTRACT

This paper is concerned with the analysis of Hertzian impact of a band-supported, thick-rim Alveheel against an elastic containment ring. The following topics are addressed: consideration of probable failure mode of the flycheel, estimation of impact velocity, prediction of maximum conditions at contact, prediction of the maximum bending stress in the impulsively loaded containment ring, and sample calculation for a proposed containment ring.

### INTRODUCTION

The functions of a centainment shield for an automotive energy-storage flywheel system are:

- 1. Vacuum preservation
- 2. Protection against flywheel failure
- 3. Protection against external impact

Designing for the vacuum containment function involves a relatively simple static external-pressure vessel analysis. Furthermore, this function is independent of type, mass, and rotational speed of the flywheel. Thus, it will not be discussed further here.

Designing for protection against flywheel failure has certain similarities to rotor-burstprotection shields for turbine engines. The latter problem has been telatively extensively investigated; see, for instance (1-3). In comparison, almost no attention has been directed toward flywheel concainment [4], except for [5] which appeared subsequent to completion of the work described herein. Thus, in this work, attention is concentrated on this problem, with particular reference to the benign failure characteristics encountered in spin tests on band-supported, graphite-epoxy rim flywheels [6]. The present work can be considered to be a correction and extension of preliminary work reported in Section 4 of [7].

Protection against external impact is undoubtedly important in automotive applications, in connection with a head-on collision, for instance. However, the extent of the collision which must be borne by the automobile's chassis and that which must be taken by the flywheel containment depends considerably upon the detail design of the specific vehicle concerned. Thus, consideration of this aspect of containment will not be discussed further.

### METHODOLOGY OF ANALYSIS

The philosophy upon which this analysis is based is analogous to that used by Timoshenko for impact on straight beams [8] and by Yang [9] for impact on plates and shallow spherical shells. The analysis consists of the following steps:

- 1. Consideration of probable failure modes
- Estimation of worst-case initial conditions (impact velocity) from elementary whirling theory and other considerations
- Prediction of maximum impact force, contact stress, and contact time from Hertzian contact theory
- Prediction of maximum bending stress from impulsively-loaded ring theory
- Selection of suitable material and thickness for containment rings (sample calculation)

### PROBABLE FAILURE MODES

In all of the spin tests previously mentioned, the flywheel rim remained intact. This is in contrast to turbine disks and other metallic rotating disks, which generally fair in three large pieshaped fragments. It is not definitively known at this time whether this difference is due primarily to the differences in naterial (filamentary composite vs. monolithic), stress state (essentially uniaxial in a ring versus highly biaxial in a disk), or both.

The types of failure encountered in the tests of Ref. [6] were either shaft failure at the necked-down breakaway portion of the shaft or band failures. The former failure is merely a testfacility protective device and probably would not be desirable or even feasible in vehicular applications. Thus, primary concern here is with band failure, which may be due to either excessive tension or compressive buckling. In either case the failure may be quite sudden. However, there is a question as to how many bands would fail. If the rim was in an out-of-plane tilting mode at the

time of failure, it might be expected that only bands on either the top or the bottom would fall. This would induce a tilting type action which would not be the worst case to contain, since the impact with the containment shield would be oblique rather than normal (radial). However, preliminary calculations reported in [10] indicated that buckling. say in the top bands, and tensile failure in the bottom ones would occur at almost the same tilt angle. Thus, it is plausible that even under tilting action both top and bottom bands could tail. Of course, in the case of an in-plane translational whirling, the top and bottom bands would be exposed to identical conditions and thus would be expected to fail simultaneously and result in normal (radial) impact.

When a band fails, in say tension, on one side of the hub, depending upon the hub design, it may or may not carry through to its continuation on the opposite side of the hub. In one of the flywheel designs, this depends upon the frictional or mechanical splaying restraint at the hub. In the other design, if one band fails, the remainder may or may not remain effective.

### ESTIMATION OF IMPACT VELOCITY

To estimate the maximum distance from the center of the rim to the center of the hub, the following approximate equation of motion for forced synchronous whirling of a single-degree-of-freedom system is used:

$$m_{r}r + (b/..)r + Kr = m_{ei.} \cos ...t$$
 (1)

Here, m, mass of rim, r radial displacement of rim center, b material damping factor for the band material, K in-plane mpring constant of the entire band subsystem, e initial eccentricity of rim, rotational speed, t time, and a dot denotes differentiation with respect to time.

The amplitude of the general solution of equation (1) is given by

$$\tilde{r} = n_{\mu} e^{i t \tau} / \left[ \left( K - n_{\mu} t \tau \right)^{2} + b^{2} \right]^{\frac{1}{2}}$$
(2)

The maximum amplitude at resonance  $(\mathbb{R}^2 = K/n_{_{\rm I\! I}})$  is

$$r_{\text{max}} = (K/b)e$$
 (3)

However, for K = 1.239 x 10° 1b/in. and  $m_{\chi}$  = 0.043 1b-sec'/in., this is predicted to occur at a speed of  $(60/2^{\circ})(1.239 \times 10^{\circ}/0.043)^{\circ} = \lambda_1,250$  rpm, which is well beyond the design maximum operating speed of 32,000 rpm. At 32,000 rpm (i = 3,351 rad/sec), b/K = 0.0172, and e = 0.010 in., equation (2) yields  $\bar{r}$  = 0.064 in. However, for more realistic design, based on the results of [11], a dynamic magnification factor of 1.0 will be used, i.e.,  $\bar{r}$  = 0.010 in.

Under these conditions the peripheral velocity and raifal acceleration of the mass center of the rim would be

$$v_{can} = .\bar{r} = (3,351)(0.010 = 33.5 in./sec or 2.79 ft/sec$$

It is conservatively assumed that upon failure the hands offer no radial restraint and that there is a 0.028-in. radial clearance between the rimperiphery and the inside of the containment housing. Thus, the radial velocity at impact, for a total travel  $s=0.028\sim0.010=0.018$  in., would be

$$v_r = (2 a_r s)^{\frac{1}{2}} = 63.5 \text{ in./sec}$$

Thus, the resultant impact velocity would have a magnitude of

$$v_0 = (v_T^1 + v_{tan}^1)^{\frac{1}{4}} = 63.6 \text{ in./sec or 5.30 ft/sec}$$

### PREDICTION OF CONTACT CONDITIONS

To predict the contact displacement, force, and compressive (bearing) stress in the containment, the perfectly elastic Hertzian impart theory as developed by Goldsmith [12] is used. Inc containment parameters are denoted by subscript 1 and the rim ones by subscript 2. The inside surface of the containment is assumed to be perfectly cylindrical with an inside radius of 10.028 in. Thus, in the sign convention of Hertzian contact theory,  $1/R_1 = 0$  and  $1/\overline{R}_1 = -1/10.028$  in.

The flywheel rim is toroidally curved with these curvatures:  $1/R_2$  = 1/0.9474 in.\* and  $1/R_3$  = 1/10.000 in.

Since it is assumed that the principal axes of the rim and containment shield are aligned, Goldsmith's angle  $\beta=0$ . Then the Hertzian geometric parameters A and B can be calculated simply

A = 
$$(1/2)\{(1/\overline{R}_1) + (1/\overline{R}_2)\}$$
  
B =  $(1/2)\{(1/R_1) + (1/R_2)\}$  (4)

Here, A = 0.00140 in. -1 and B = 0.428 in. -1. Thus, A/B = 0.00265 and by interpolating Goldsmith's [12] Table 5, page 87, one obtains factors q<sub>1</sub> = 14.7 and q<sub>2</sub> = 0.370. To obtain q<sub>3</sub> = 1.85, it was necessary to extrapolate Goldsmith's values by plotting on log-log paper.

The contact force F is related to the contact displacement a as follows:

The radius R<sub>2</sub> is calculated from the respective axial and radial semi-axes of the elliptical cross section of the rim (1.5 and 2.375 in., respectively; see Fig. Al in [10]) as (1.5)-/2.375 = 0.9474 in.

$$F = k_2^{-1/2} = F_m \sin(1.068 \text{ v}_0 t/v_m^3)$$
 (5)

where  $v_{\alpha}$  is the relative velocity at initial contact, t is time, and  $v_{m}$  and  $F_{m}$  are the saximum values of the displacement and force, respectively:

$$r_{\rm m} = (5 \text{ v}_{\rm o}/4k_{\rm j}k_{\rm j})^{2/5}$$
 (6)

$$F_n = k_2 a_n^{-3/2} + 1.143 k_2^{-2/5} v_0^{-6/5} / k_1^{-3/5}$$
 (7)

Here, the following additional parameters are defined as

$$k_1 = (1/\pi_1) + (1/\pi_2)$$
 (8)

$$k_{2} = \frac{(4/3)q_{k}}{(\frac{1}{4} + \frac{1}{2})(A + B)^{\frac{1}{2}}}$$
 (9)

$$r_1 = (1 - \frac{1}{2}) / \tau E_1 + \frac{1}{2} = (1 - \frac{1}{2}) \tau E_2$$
 (10)

where E is Young's modulus and is Poisson's tatio.

The total time of contact : is given by

$$t = 2.9432 \frac{1}{10} / v_0$$
 (11)

The contact area is an ell.pse with semi-axes a and b:

$$a = q_a [(3F_m/4)(\gamma_1 + \gamma_2)/(A + B)]^{1/3}$$
(72)

 $b = (q_b/q_a)_a$ 

the peak compressive stress developed is given by

$$r_{\rm op} = (3/2)(F_{\rm p}/ab)$$
 (13)

### DYNAMIC STRESS ANALYSIS OF CONTAINMENT RING

To determine the peak dynamic bending moment in the containment ring, the analysis by Mittal [13] is used. Mittal showed that for a circular ring subjected to a concentrated loading that is a half-sine pulse in time, i.e., equation (5), the maximum bending moment occurs at some value of time t, 0 × t × :. For this time interval, the bending moment is given by

$$E = (F_m/2) (E_1 I/\rho_1 A_T)^{1/4} (\tau/\tau)^{1/2} \{f(x)\}$$

 $= (1/2) \cos (ht/t) + (1/2) \sin (rt/t)$ 

+ 
$$(F_m t/2\pi^2)(E_1 1/o_1 A_p)(2.9303/R^3)$$

$$*[t - (1/r) \sin (rt/1)]$$
 (14)

where x : 2t/: and

$$f(x) = \frac{1 + 0.926x}{2 + 1.792x + 3.106x}$$
 (15)

Here, Ar cross-sectional area of containment ring, l rectangular area of moment of inertia of ring cross section about the appropriate centroidal axis, R mean radius of containment ring. It is noted that equations (14) and (15) both differ elightly from those given by Mittal, since his paper had some obvious typographical errors.

### SAMPLE CALCULATION

 $n_1 = 2^{-(10.528)(3.06)(1.00)(0.050/386)}$ 

= 0.0257 lb-sec /in.

Using equations (10), one obtains  $\delta_1$  = 2.36 x  $10^{-8}$  in.  $^2$ /lb and  $\delta_2$  = 1.64 x  $10^{-7}$  in.  $^2$ /lb. Then equations (8) and (9) yield  $k_1$  = 62.17 in. /1b-wec² and  $k_2$  = 89.62 x  $10^6$  1b/(in.)  $^{5/2}$ . From equations (6), (7), and (11), one gets  $\alpha_{\rm H}$  = 0.00383 in.,  $\Gamma_{\rm H}$  = 21,200 lb, and  $\tau$  = 177 x  $10^{-6}$  sec.

Application of equations (12) yields a = 1.703 in. and b = 0.0429 in. Using these values in equation (13), one obtains  $\sigma_{\rm cm} = 139,000$  psi, which is an acceptable value for the Hertzian contact compressive stress in this material.

By examination of the numerical results given by Mittal [13] and some further calculations, it can be shown that the peak bending moment always occurs when t/t = 0.72. Then, application of equations (15) and (14) yield i(x) = 0.2449 and a peak moment  $|H_{\rm ms}| = 21,600$  lb-in., respectively.

Finally, the maximum bending stress is given by

This is a very reasonable tensile stress for aramidepoxy, which has an ultimate tensile strength of 200,000 psi. However, it may be marginal on the compressive side of the bend.

It is noted that the calculated weight of the 1.0-in, thick aramid-epoxy containment ring is only 9.92 lb. It should be emphasized that this weight is equal to that of an aluminum containment ring 0.50 in, thick or a steel containment ring 0.177 in, thick.

### DISCUSSION

in this section are discussed the implications of the numerous engineering approximations which have been made in the foregoing analysis in order to obtain relatively simple closed-form solutions.

The present analysis has been based upon Hertzian elastic contact theory, which in itself has some engineering approximations. However, relatively recent dynamic-contact experiments by several different investigators [14,15] have corroborated this theory. This was true even in the experiments of [14] which used impact condition that were chosen to maximize the effects of streamwave energy dissipation. The question of the effects of material damping and localized yielding in the vicinity of contact were investigated by Chou and Flis [16] for the case of dynamic contact loading of straight beams. They concluded that these effects reduced the peak stresses only slightly. Thus, Hertzian theory should be slightly conservative, which, of course, is usually desirable for design purposes.

Perhaps the most questionable assumption used here is the use of isotropic-material contact stress theory. The theory could be improved, as the cost of considerable complexity, by combining anisoropic elasticity results for the point-loaded half-space from Lekhnitskii [17] in a manner analogous to Goldsmith's development of Hertzian dynamic contact for isotropic med(a [12].

There may be some question regarding the validity of using Mittal's thin-ring theory for a ring which has a 0.10 ratio of radial depth to inside ring radius. Although more accurate ring theory including transverse shear deformation and rotatory inertia is now available [18], the Morley theory used by Mittal has been shown to be adequate for thickness-to-radius ratios as high as 0.5 [19].

It should also be mentioned that the additional restraint provided by the end plates, located above and below the flywheel and recessary for vacuum preservation, has been neglected in the present analysis. Again, this is another factor which would provide additional structural integrity beyond that computed here.

Finally, it should be kept in mind that the present analysis has not addressed the problem of frictional hearing due to the abrasive rubbing of the flywheel perip ery against the inside of the containment ing.

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A RATIONAL APPROACH TO THE ANALYSIS OF STRUCTURES SUBJECTED TO UNDERGROUND BLASTS

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### ABSTRACT

The two major data bases connected with underground blast effects on structures are utilized to obtain rational procedures for solving - approximately - the two fundamental engineering problems. The data bases are, 1) accelerogram records at points in the field affected by the blast and 2) isoseismal contour maps for the entire field affected by the blast. These then lead to analytic expressions and charts for the engineering problems, namely 1) damage assessment and 2) structural design/analysis.

### INTRODUCTION

The theory and procedures to be described were developed during the course of earthquake engineering research. However, all the results obtained, suitably scaled, apply as well to the underground blast phenomenon. As is well known the earthquake mechanism has been likened, physically, to the equivalent of an underground explosion of enormous initial energy.

Thus, the presentation will utilize equations and charts that were obtained in studies related to earthquakes. But all the procedures, all the equations, all the charts apply as well for the underground blasts which are the topic of this symposium. The numerical values of the different terms will very likely vary from those obtained for earthquakes and used in this report. But the fundamental techniques are the same. In fact, underground blast phenomena afford an excellent means for checking the more comprehensive predictions which follow from the application of the theory to the earthquake event.

### BASIC ASSUMPTIONS

This research is founded on three fundamental (and related) premises:

 Underground blast engineering (hereafter designated as UBE) is a unique discipline in the overall field of applied mechanics, just as for example, elasticity and heat flow are separate and different. Therefore, UBE has its own particular invariants, parameters, equations, variables and similar quantities - and furthermore these should be very different from the other well-known terms and relations in applied mechanics.

- 2) The sources or fountain heads for all the quantities mentioned above (the invariants, parameters etc.) will be the two major observation banks (or experimental data or field data) of UBE, these being
- a) The accelerogram which, physically, must be related in some fashion to the variation with <u>time</u> of ground surface energy at a <u>point</u> in the blast field.
- b) The isoseismal contour map which, physically, must be related in some fashion to the variation with <u>distance</u> of the ground surface energy over the <u>entire area</u> affected by the blast.
- Note, therefore, that proceeding from 1) to 2) above we are led directly to
- 3) namely, energy is the key element, the basic ingredient in the entire underground blast event, starting from its initiation (the explosion) and proceeding timewise and spacewise until its completion with the accompanying effect upon and response of structures.

The research - which will be reported elsewhere in its entirety (Ref. 1) covers every facet of the blast from its initiation (a blast mechanism) up to and including its effect on and the response of structures. New parameters, invariants, equations and similar relations are introduced and a complete unified, rational approximate theory of UBE is developed.

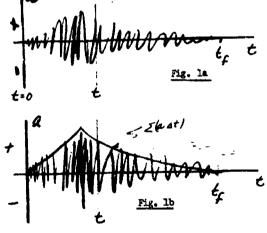
The theory is based upon reasonable mathematical, physical and technological assumptions, is dimensionally sound and represents logical, integrated over-all approaches to all facets of the blast event.

As in all engineering design applications, certain experimental (field) data must be obtained in order to establish "allowables" or equivalent terms. At this time only a limited fund of such quantities is available and the applications are limited in this respect. However, the entire development is "self-correcting" in the sense that as more and more data is collected and utilized, corrections and modifications to the working data can be made without difficulty until finally, the design relations, curves and charts will be established with sufficient accuracy so that ordinary engineering design offices can use them with a level of confidence suitable for engineering purposes. The author suggests that even at this time, there probably is sufficient data available (possibly in the classified files) to permit its use – at the appropriate approximate level.

In this report only that portion of the study dealing with damage to structures will be dealt with in detail and because of space limitations, only the results will be presented. The details are described elsewhere - as are the applications to the structural design and analysis phases of the problem.

### THE ACCELEROGRAM INVARIANT AND PARAMETERS

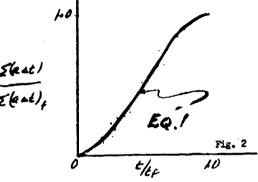
A typical earthquake accelerogram is shown below, Fig. la. We assume that except possibly for scale, the underground blast accelerogram is similar. Hence the discussion which follows applies to UBE.



An analysis and study of a number of accelerograms, as well as physical considerations, suggest that  $\mathbf{t}_{\Sigma 0}^{\Sigma}$  (a $\Delta t$ ) and t are the important variables in this phenomenan, and in particular  $\Sigma$  (a $\Delta t$ ) and  $\mathbf{t}_f$  are the fundamental parameters, Fig. 1b.

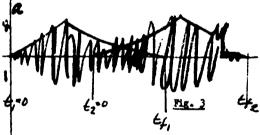
A mathemarical derivation leads to an invariant expression (the "acceleration index") which holds for "canonical" accelerograms, this being

$$\frac{2(a + t)}{2(a + t)_{f}} \cdot \frac{0.12 \left[1 - \left(\frac{t}{a}\right)^{1.5}\right]}{(1)}$$
which plots as shown in Fig. 2.



The numerical values obtained in Eq. 1 apply to earthquakes. They probably differ for underground blasts. In any case, these values can be established without difficulty.

For those accelerograms that are not "canonical", typically as in Fig. 3, we



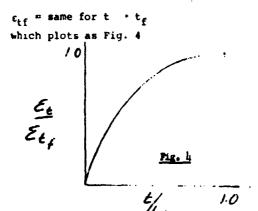
can generally superpose 2 or more canonical accelerograms.

By utilizing an alternate, but equivalent postulated mathematical forumlation, equating equal terms, and integrating we obtain an equation for the <u>timewise</u> variation of horizontal ground energy at the point where the canonical accelerogram was obtained, Eq. 2.

$$\frac{\mathcal{E}_{t}}{\mathcal{E}_{t_{F}}} : \frac{\left[\left(\frac{t_{F}}{t}\right)^{l.8} - \left(\frac{t_{F}}{t_{L}}\right)^{l.8}\right]}{\left|-\left(\frac{t_{F}}{t_{L}}\right)^{l.8}\right|}$$
(2)

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 $\varepsilon_{\rm t}$  = surface horizontal energy per unit effective area between the times  ${\rm t_i}$  and t at the accelerogram location.



In Eq. 2 also the numbers may be different for underground blasts.

For 2 or more superposed canonical records (Fig. 3) we superpose the energy expressions, Eq. 2, Fig. 4.

### THE GEOLOGY AND MEASURES OF DAMAGE

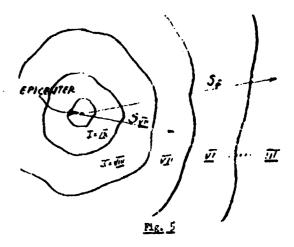
Physically, we must assume that the "geology" of a region affects the ground behavior and structural response due to underground blasts. We assume, at this time, three different "geologies", designated as R1, R2, and R3, to be defined following further study of this variable. It is conceivable that a smaller (or larger) number of separate geologies is required to account for all possible situations. In a general way, frequency of the acceleration is accounted for in this classification. These geological designations are used in the mathematical, physical and technical formulations throughout the research, as we shall see typically, in the present damage assessment portion of the study.

We assume "damage" is defined by an "Intersity Number," I, as given in a (possibly modified) Mercalli type Scale, on an "isoseismal contour map". Fig. 5 shows such a map for an earthquake. Its form will be similar but the values may differ for an underground blast.

### THE ISOSEISMAL INVARIANT AND PARAMETERS

An analysis and study of 28 earthquakes during the past 500 years, occuring all over the earth, as well as physical considerations, suggest that I (IS) and S are =0

the important variables in this phenomenon and in particular that  $\mathbf E$  (IS), and  $\mathbf S_{\mathbf F}$  are

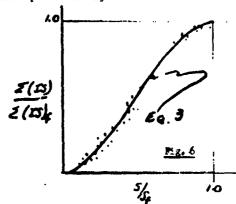


the fundamental parameters.

A mathematical derivation leads to an invariant expression (the "isoseismal in-dex") which holds for all 28 earthquakes, this being Eq. 3,

$$\sum_{z=(zs)_{c}}^{z}(zs) = e^{-(zs)^{3}}$$
(3)

which plots as Fig. 6



The author suggests that a similar equation and curve will hold for underground blasts - suitably modified, if necessary, for "geology".

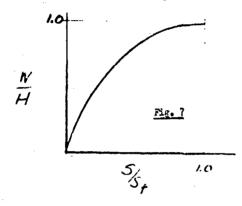
By utilizing an alternate but equivalent postulated mathematical formulation, equating equal terms and integrating, we obtain an equation for the spacewise variation of horizontal ground energy over the

entire field affected by the earthquake,  $\overline{Eq. 4}$ , which plots as Fig. 7.

$$\frac{W}{H} = \frac{\left(\frac{S_F}{S_F}\right)^3 - \left(\frac{S_F}{S_F}\right)^3}{\left(\frac{S_F}{S_F}\right)^3 - 1}$$
(4)

W = total surface horizontal energy between the small radius S; and the radius S.

 $H = same as 2bove for S \rightarrow S_f$ 



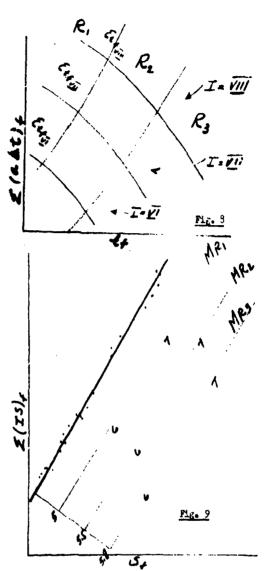
THE DAMAGE ASSESSMENT CURVES

In this theory,  $\Sigma(a\Delta t)_f$  and  $t_f$  and  $\Sigma(IS)_f$  and  $S_f$  are the key parameters in the rational underground blast analysis and must be included in all theoretical developments connected with the blast phenomena. Thus

A) Physically,  $\Sigma$  (aat)  $_f$  and  $_f$  must be connected with the damage of structures. A study of a limited number of earthquake accelerograms (corrected for direction) that had isoseismal maps for the same eventuleads to a preliminary damage (intensity) map as follows, Fig. 8, for earthquakes. A similar, suitably modified chart, should apply to underground blasts.

If we have a superposed accelerogram as in Fig. 3, the author suggests at this time that the separate  $\mathbb{S}(a\Delta t)_f$  and  $t_f$  values for each separate canonical envelope be added. Then use these sums in Fig. 8

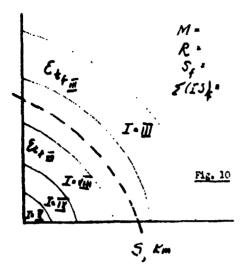
B) Physically,  $\Sigma(IS)_f$  and  $S_f$  must be related to the magnitude, M, and hence the energy, of the underground blast. For example, by using the 28 earthquakes we find Fig. 9, (and a similar representation will apply for the underground blasts) so that



C) using the equation given above and Fig. 9, for a given M and R we can determine  $\Sigma$  (IS) f and Sf and the corresponding isoseismal map may be computed and plotted, Fig. 10, from which the damage may be assessed.

### THE STRUCTURAL DESIGN PROCESS

Very briefly (because of space limitations) - the structural design and/or analysis phase of the study utilizes the energy concept in conjunction with the accelerogram and isoseismal invariants and parameters previously described. The details are described in Ref le and 1f.



In applying the method, symmetry and anti-symmetry are the basic tools used. A free-free form of vibration is assumed which requires the estimation of an "equivalent" length, i. The energy tobeabsorbed by the structure requires the determination of an "effective area, ae". Symmetrical and anti-symmetrical energy and vibrational configurations are utilized and the entire process leads to an approximate analysis that includes all of the variables that should enter into an underground blast analysis in a form that can by used by ordinary engineering design offices.

### CONCLUSION

The design process, as in all engineering design, starts with specified or code or judgement design decisions. These could be, typically,

 a) A specified canonical accelerogram or cluster of canonical accelerograms with given separate Σ(aΛt)<sub>f</sub> and t<sub>f</sub> values and geology.

or

b) A given blast magnitude, efficiency and geology from which I(IS) and Sf are obtained.

or other similar data.

From these, using the equations and charts derived from this theory, we can determine all of the necessary UBE parameters required for the rational, analytical assessment of damage and for the structural design.

There is no doubt whatever, that every underground blast is different, in detail,

from every other underground blast that majever occurred, wherever it occurred.

But, by the same token, because the blast is a natural phenomenon, it must also be true that, overall, in the large, there are certain relationships or equations or parameters that are approximately common to all underground blasts.

These relationships or equations or parameters are here called the <u>invariants</u> of the blast phenomenon and the writer suggests that any attempt to obtain a rational, quantitative, scientific theory for UBE must start with a consideration of these basic building blocks — the invariants.

To uncover these the research was guided strongly by physical-engineering-mathematical considerations founded on available earthquake tests and experiments which, initially, surfaced in the form of hypotheses. By extension the hypotheses permitted the derivations of new mathematical expressions which include those physical-engineering terms that must occur in UBE theory. These new expressions predict new phenomena which are capable of experimental check.

Should the new relations check out - with accuracy consistent with the observed data and sufficiently precise for engineering applications then one may with some confidence assume they represent an acceptable theory for the UBE event.

Closely related to the above is the fact that in all fields of applied engineering, an essential requirement for the engineer is the collection and tabulation of basic design information. This design data is generally subject to continuous adjustment and revision as additional experience or special conditions require. Instructural angineering for example, we need data on (to name just a few items), wind loads, pile capacities, earth pressures, allowable steel stresses etc - data which to this day are being adjusted and revised as required by ongoing research. This data almost always can be determined only by performing laboratory or field tests and furthermore varies in form or content depending upon the appliced engineering field considered.

As these experimental (i.e. field) data are collected, they become part of the inventory in the storehouse of design data and as they accumulate, the need for additional experimental values frequently diminishes and the applications (in design and/or analyses) can generally be made with greater accuracy and confidence.

In this new UBE theory, the necessary experimental refinements can be obtained by

analyzing experiments currently being routinely performed (i.e. the accelerogram and the isoseismal map) and/or by developing and performing other relatively simple exercises utilizing man-made blasts. In this way, the following terms will be evaluated more precisely, thereby permitting greater and greater accuracy as the accumulation of data continues:

- a) The efficiency, n, of the blast.
- b) The role of the "geology"
- c) The acceleration index invariant expression and the derived relations for pointwise - temporal variation of blast energy.
- d) The isoseismal index invariant expression and the derived relations for spacewise variation of blast energy.
- e) The effective length, (
- f) The effective area,  $a_e$

The design engineer, architect, specification or code writer, damage or safety engineer and other professionals who are concerned with rational scientific UBE analyses can use the new theory at the present time based upon available data and reasonable assumptions. Because of the limited available amount of the required accumulated experimental data (which is a common occurrence in any newly developed theoretical application in applied engineering) the amount of approximation involved and other possible limitations are uncertain. In order to increase the accuracy, the author recommends further continuing study, testing and refinement of the quantitative values for the uniquely UBE terms mentioned above in a) through f).

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# EXTREME DIWARLC LOADING EFFECTS ON STREE AND CONCRETE SHELL STRUCTURES

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### ARSTRACT

Using the modern computerized analysis, the special purpose computer program SLOOPSAN can be successfully applied for the evaluation of thin structure strength limits in presence of extreme dynamic loading phenomena. This program correctly solves wave-propagation-type of problems involving short transient (very rapid loading-time sequence) and including shock-wave response from impulsive loading (explosion or blast wave) and impact loading (missile impact). SLOOPSAN program is based on a finite element shell formulation using the Semiloof element and has been developed for transient dynamic non-linear analysis applying an efficient explicit direct time integration technique.

SLOOFSAN 3-D capabilities in the fields of structural safety assessment and anti-missile design are illustrated in the paper.

### TPLICIT DINANIC ANALYSIS USING SHICLLOP

The present formulation for the solution of complex shell problems in transient non-linear analysis is based on the construction of a very performing mechanical model with the use of advanced numerical techniques. The explicit solution strategy is preferred to a modal superposition procedure or an implicit direct time integration technique for the following reasons:

- the equations of motion are decoupled thanks to a mass-lumping process and are simply expressed interms mertia, damping, internal and external mere ectors;
- the nod:1 accelerations, velocities and displacements are directly computed using central difference formulas;
- the internal force vector represents the keystone of the mathematical model because it solely contai. I the information related to the struct it stiffness and the non-linear material behaviour through the stress vector;
- the constitutive equations are easily implemented, in particular total stress-strain formulations of the explicit type. See e.g. Ref.(I).

- the geometrical non-linearities, due to large rotations, are trivially implemented using the convective coordinate technique;
- -the program architecture is much more simple: no bandwidth problems, less computer storage, no assemblage nor inversion of any matrix, ease of programming;
- this attrategy is more competitive for advanced vector processing, thanks to a complete vectorial formulation.

This technique of explicit time integration, in connection with numerically tested mass-lusping procedures, has been implemented in previous works of the author (2,3,8), for the more complex isoparametric shell element Semiloof developed by Irons (6).

The Semiloo? dynamic model for steel and concrete thin shells has nodal masses and inertia moments obtained by lumping techniques, explained in Ref. (2), and can be represented as a system of discrete nodal masses interconnected by means of springs representing the internal forces and moments. Any spring stirfness may var from high values to very small ones when plasticity and any other material disintegration process take place in the finite element.

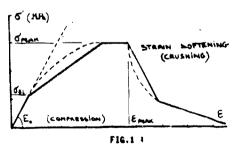
The modelling of reinforcement is obtained by adding layers of steel bars at the upper and lower shell surfaces. These steel membranes undergo the same total strains as concrete until the reinforcement bars buckle when concrete locally crushes. Concrete thickness and steel reinforcement percentage may vary from an element to another and the reinforcement may be different at the upper and lower surfaces within one element.

Prestressing may be included in the concrete by giving an initial prestrain in the reinforcement. The static stresses due to prestressing or dead weight may be carried out using the transient program SLOOPSAN in a kind of dynamic relaxating mode, as illustrated for example in Ref. (3). The material non-linearities, dealt with in this paper, include a plasticity model for ductile materials like steel, based on:

- experimentally observed monoaxial yield stress we plastic s'rain relationship;
- the concepts of Von sissis stress, Drucker's postulate, isotropic hardening and plastic energy dissipation.

For reinforced concrete, the following inelastic behaviours are included:

- cracking of concrete in tensile regime. The model is based on the concept of sero tensile strength, or small tensile strength, before the appearance of the iarst crack. A stress redistribution takes place when a crack strain is defined perpendicular to the new crack, in agreement with Mohr's circle. See e.g. Ref.(3):
- elasto-plastic formulation for concrete in compression. Based on the well-catablished theory of plasticity, the ascending and descending parts of the stress-strain curve are quite simulated, as shown for example in Fig. I. Crushing of concrete is defined by the postpeak strain softening behaviour;
- a new explicit biar'al stress-strain relationship for concrete in compression has also been incorporated in SLOOFSAN because it reproduces outte well the inelastic dilatancy of concrete near failure (4). This general constitutive ecuation, developed by Cedolin et al (I), is obtained by expressing the secant bulk and shear moduli of elasticity as non-linear functions of the first two invariants of the strain tensor only:
- concerning the steel reinforcement, plasticity is encountered in tension as well as in compression. Foreover, local steel buckling in compressive regime, when concrete crushes, is similated by deleting the compressive contribution of the reinforcement to the internal force vector.



STRESS-STRAIN CONSTITUTIVE LAW FOR CONCRETE

The proposed mechanical andel permits to follow very accurately the progressive plastification of steel shells or the cracking propagation of concrete thin structures within each finite element in the mid-surface and across the thickness.

As a consequence, the complete disintegration of reinforced concrete shells is created by concrete cracking, concrete crushing, steel planticity, local steel buckling, which represent the major four factors computed directly through the internal force vector.

The present material models for concrete do not yet take into account of the sensitivity of concrete to some parameters like stress history or strain rate. Experimental research into concrete behaviour under dynamic load is urgently needed in order to use the results from computer program with more confidence.

#### EXPLOSION / STRUCTURE INTERACTION

The advanced computer program SLOOFSIN permits to illustrate some extreme dynamic loading condition acting on thin metal structures. A cylindrical steel panel is submitted to impulsive loading (initial velocity) which is supplied by an explosive sheet in contact with the metal. Pig. 2 shows I/4 model of the panel using only 20 Semiloof elements. High membrane and bending wave propagation effects occur in the cylinder together with a rapid plasticity extension.

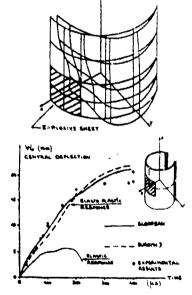


FIG. 8 - CYLINGRICAL PART, UNDER INPULSIVE LOADING (EXPLICITOR)

The deformed whape of the cylindrical namel shows how the impulsive motion involves very large displacements and rotations. The highly non-linear response of the central defliction versus time is quite different from the clastic linear response. Excellent agreement with numerical and experimental results, given in Ref. (5), is obtained.

#### SOPP-MISSILS / STWICTURE INTERACTION

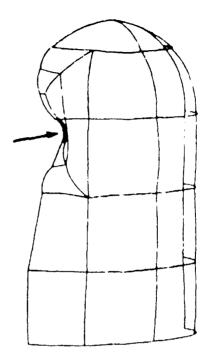
The described numerical technique based on explicit dynamic analysis using a shell formulation is particularly suited to handle highly non linear problems of soft-missile impact on large concrete structures. Using the Semiloof element. relative coarse meshes are defined for the nuclear reactor containment building impacted by an aircraft. The computer program SLOOFSAN permits an accurate determination of the nartial da mage of the local impacted area as well as the overall behaviour of the remaining structure under the induced vibrations. The impact of a civil aircraft (Boeing 707-320) on the dome and the lateral wall of the reactor containment has been already presented in a previous paper by the author (3).

For the complete 3-D problem of the reactor building loaded laterally, the effects of incorporating the dead weight or a little tensile strength for concrete on the dynamic structural response are shown in Fig. ). The values for the maximum horisontal displacement obtained in linear and non-linear analysis are very close to the response values published by Rebora et al (7) where a more complex concrete model and solid brick elements have been utilised. In Fig. 4, the deformed shape and the crack pattern during the siroraft impact are illustrated. Concerning the crack propagation, radial cracks appear first during loading at the interior surface around the impacted area. Than, radial and oircumferential cracks appear at the exterior surface as well as

REACTOR BUILDING ANALYSIS	SLOOFSAH (CR)	REBORA (CR)
LINEAR ELASTIC (8)	4.03/4.00	3.32
HUH-LIHEAR (CRACKING) des.8 Mg. (.)	4.47	4.29
HOM-LINEAR (CRACKING) 3-0.0 (.) + DEAD WEIGHT	7.21	-
HOM-LINEAR (CRACKING)	9.13	-

(1) I CONCRETE TENSILE STRENGTH LOT

FIG.3 : MOKIZONTAL BISPLACEMENT BUE TO AIRCRAFT CRASH (AT POINT 1)



DEFORMED MESH

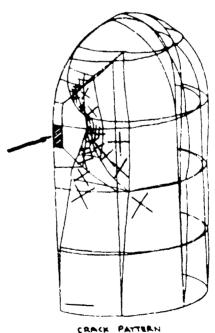


FIG.4 : HUCLEAR REACTOR SUILBING LINGER SOFT-HISSILE (AIRCRAFT) IMPACT

through cracks in the impact none. A tangential crack appear also at the cortainment base after the impact. SLOUPSAN analysis is fulfilled with the complete knowledge of the principal stresses in every place of the structure is both the concrete and the steel reinforcement. In this caloulation, only multiaxial cracking appears without any concrete crushing nor steel yielding.

#### CHIMNEY COLLAPSE CAUSED BY AURCRAPT COLLISION

The dynamic response of a tall chimney impacted by different aircrafts (military and ciwil) is studied using the present 3-D shell sodel. The score of using the shell formulation is to examine the effects of all the non-linearities incorporated in SLOOPSAN and to understand the dynamic failure modes obtained by an explicit time integration approach. The aircraft loading functions for the military aircraft (Phantom F-4E) and the civil aircraft (Boeing 707-120) are defined in Fig.5.

A preliminary linear elastic analysis for the Boeing crash shows a well-known deflection mode with a maximum horizontal deflection at the top H of 5 m. , as shown in Fig. 6.m .

A complete different deflection shape is obtained, in Fig. 6.b , for the non-linear impact of the same civil aircraft. Due to this fast transient phenomena, only the impacted area is completely damaged with local bending failure mode at the top but without any loss of bending rigidity at the chimney base, large rotations and horisonts' displacements are observed at the top (H greater than 45 m.)

For the faster military aircraft collision, a more severe disintegration of reinforced concrete with a more pronounced shear failure mode is obtained, as shown in Fig. 6.c . The deflection at the top H exceeds the 40 m.

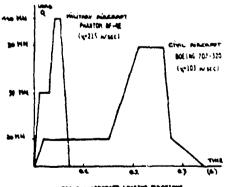


FIG.S I AMERICA LONGING PURCTIONS

These highly non-linear analyses do not terminate when the finite elements start to be distorted, as shown in Mr. 6, but the analysis can be carried on until the internal resisting force vector vanishes completely in the temacted area. in presence of a total material disintegration . For the present structural behaviour simulation, all the disintegration factors ( concrete cracking, concrete orushing, steel yielding, local steel buckling ) have been encountered.

Unfortunately, no particular post-processor was available to correctly visualise the real local chimney collapse. Because, with the use of the present explicit non-linear dynamic analysis, the modal points with their mass and velocity but without resisting forces ( or springs connecting all of them together), are moving away and down (gravity field) like in the reality.

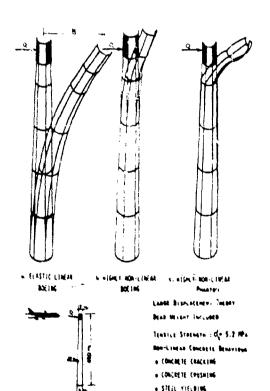
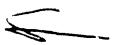


FIG.6 : CHIMEY COLLAPSE CAMES BY AIRCRAFT IMPRIGERENT

. STEEL BUCKLING

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FRACTURE DIAGNOSIS IN STRUCTURES USING CIRCUIT ANALOGY

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#### **ABSTRACT**

The paper uses the Kirchhoff's equations for the T- and M-circuits to analogously simulate the beam vibration. Structures formed by straight beam segments can then be simulated by electrical meshes formed by T- or M-circuits. In the paper the analogous circuits are also developed for the cracked beams. The natural frequencies of the circuits thus yields the natural frequencies of the structures with or without crack. In the inverse application, the change in frequencies leads to the location and assessment of the fracture damage of the structure.

The paper developed, specifically for the a-circuit, a formalization of establishing the activate, a formalization of establishing the characteristic matrices. The standardized format makes it possible for adaptation to computer programming. An estimate of the algorithm is included for comparison of its advantage in the speed of computation.

#### 1.0 Introduction

The diagnosis of fracture damage in structures may involve two steps: The first is the detection of the presence of damage, and the second is the determination of the location and intensity of the fracture [1]. The first step requires monitoring of some variables associated with the structure. The second is related to a quantitative interpretation of the first. In this paper the variables to be monitored are the first few modal frequencies of the structure. The data on Changes of frequencies are used for the estimation of the location and the intensity of the fracture damage. The classical modal shape of beam oscillation is employed to discretized the mathematical model, which is analogous to the circuit equations describing the T- or M-circuits.

Keropyan and Chegolin [2] surveyed the work done on electrical analogies for solving problems

in statics and dynamics of elastic structures. Their approach to frameworks with sidesway involves either an iterative or a three-step procedure in solving the horizontal displacement of girders and is analogue-computer-oriented. In this paper, a modified and improved approach is develuped, that is readily formalized and adaptable to digital programming. When the method is applied digital programming. When the method is applied to free vibration of multi-story multi-span frame structures with or without cracks, natural frequencies of the analog circuit, hence modal frequencies of the frame with or without crack, can be determined by exciting the circuit with a variable frequency excitation, and by establishing the excitation frequencies at which response is maxi-Analytically this corresponds to finding zeros of a determinant. Multi-cell structures and structures with crack will be illustrated in the application.

#### 2.0 Circuit Analogies

The classical modal shape  $y(\xi)$  of a single section of a straight beam is:

$$y(\xi) = A \cosh \theta \xi + B \sinh \theta \xi + C \cosh \xi + D \sinh \theta \xi (1)^6$$

where  $a^{h} = \rho w^{2}L^{h}/EI$ ,  $\rho$  the lineal density, w the modal frequency, L the beam element length, (EI) the beam stiffness and t the dimensionless length such that the two end points are  $\xi_1$  = 0 and  $\xi_2$  = 1. The set of slopes  $(y_1,\ y_2)$  and shears  $(V_1,\ V_2)$  can be expressed in terms of the set of resisting moments  $(N_1, N_2)$  and deflections  $(y_1, y_2)$  as fol-

$$\begin{cases} y_{1}^{i} \\ y_{2}^{i} \\ v_{1} \\ v_{2} \\ \end{cases} = \begin{bmatrix} -\frac{L\overline{S}}{ET} & -\frac{L\overline{T}}{ET} & -\frac{\overline{S}}{L} & \overline{T}^{i} \\ \frac{L\overline{T}}{ET} & \frac{L\overline{S}}{ET} & -\frac{\overline{T}}{L} & \overline{S}^{i} \\ \frac{\overline{S}^{i}}{L} & -\frac{\overline{T}^{i}}{L} & \overline{PS} & \overline{PT} \\ \overline{T}^{i} & -\frac{\overline{S}^{i}}{L} & -\overline{PT} & -\overline{PS} \\ \end{bmatrix} \begin{cases} M_{1} \\ M_{2} \\ y_{2} \\ \end{cases} (2)$$

5Numbers in brackets denote the references.

<sup>&</sup>lt;sup>6</sup>Numbers in parentheses denote the equations in this paper.

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Research Assistant, Mechanical Engineering Dept. Professor, Mechanical Engineering Dept.
Assoc. Professor, Civil Engineering Dept.

where  $P = EI B^3/L^3$ , S = (coth B - cot B)/2B, T = (csc B - csch B)/2B,  $S^3 = B(coth B + cot B)/2$ ,  $T^3 = B(csc B + csch B)/2$ . The first two equations in (2) can be written as

$$y_{1}^{2} + (z + z_{0}) H_{1} - z_{0}H_{2} + \varepsilon_{1}$$

$$y_{2}^{2} + z_{0}H_{1} - (z + z_{0}) H_{2} + \varepsilon_{2}$$
(3)

where  $Z = -(\overline{S} + \overline{T})L/EI$ ,  $Z_0 = L\overline{T}/EI$ ,  $E_1 = (\overline{T})y_2 = \overline{T}$  $S(y_1)L$  and  $E_2 = (S(y_2 - T(y_1)/L)$ . Equations (3) are the Kirchhoff's equation for the active through terminal network shown in Figure 1. In this electermechanical anglogy, moment and slope (M, y') are analogous to the electrical current and voltage, respectively. The coefficients, Z and E, are respectively the impedance and the potential source. The negative impedance shall pose no difficulty in the theoretical development. The natu ral frequencies, hence the modal frequencies of the analog frame, can be determined by exciting the circuit with a variable frequency excitation, and by establishing the excitation frequency at which response is maximum. With reference to Figure 1, a simple cantilever beam problem can be illustrated. The left part of the T-circuit is shorted, resulting in yi = 0, corresponding to the built-in end. The potentials  $E_1$  and  $E_2$  are computed based on  $y_1=0$  and  $V_2=0$  the last equation of (2). At modal frequency when a constant amplitude voltage of  $y_2$  is input,  $M_2$  diverges. The analysis becomes one to compute the zeros of the network impedance function  $l_{22} = y_2/M_2$ .

Modeling the cracked section in a beam shall follow the method of fracture hinge [1]. The crack is mechanically represented by a torsional spring of spring constant  $\kappa$ . Slope is thus discontinuous at the cracked section (ay' =  $M_c/\kappa$ ). Such discontinuity in the circuit analogy is represented by a voltage source of magnitude  $M_c/\kappa$ . The two parts of the beam, divided by the cracked section are each represented by a T-circuit as shown in Figure 2. The other continuity conditions are satisfied.

When the first two equations in (2) are inversed, we have this:

$$\begin{cases} M_{1} \\ M_{2} \\ v_{1} \\ v_{2} \end{cases} = \frac{E I - \theta^{2}}{L^{2}} \begin{bmatrix} \frac{L}{8} S & \frac{L}{8} T & S' & -T' & S' \\ \frac{L}{8} T & -\frac{L}{8} S & -T' & S' \\ S' & T' & \frac{B}{L} P & -\frac{B}{L} P' \\ Y' & S' & \frac{B}{L} P' & -\frac{B}{L} P \end{bmatrix} \begin{bmatrix} y_{1}' \\ y_{2}' \\ y_{1} \\ y_{2} \end{bmatrix} \tag{4}$$

where  $S = (\cosh \beta \sin \beta - \sinh \beta \cos \beta)/\alpha$ ,  $T = (\sinh \beta - \sin \beta)/\alpha$ ,  $P = (\cosh \beta \sin \beta + \sinh \beta \cos \beta)/\alpha$ ,  $S' = \sinh \beta \sin \beta/\alpha$ ,  $T' = (\cosh \beta - \cos \beta)/\alpha$ ,  $P' = (\sinh \beta + \sin \beta)/\alpha$ ,  $\alpha = \cosh \beta \cos \beta - 1$ . The first two equations in (4) can be rewritten as

where 6 = (S + T) El g/L,  $G_0$  = -TEl g/L,  $I_1$  = (S' $y_1$  - T' $y_2$ ) El  $g^2/L^2$ , and  $I_2$  = (S' $y_2$  - T' $y_1$ ) El  $g^2/L^2$ . Equations (5) are the Kirchhoff's current equations for the active three terminal network shown in Figure 3. In this electromechanical analogy, moment and slope (M, y') are analogous to the electric current and voltage, respectively. Given the electric current admittances and the current sources, respectively. The negative admittance poses no difficulty in the theoretical development.

A single cantilever beam problem can be illustrated with reference to Figures 3 and 4. The left port of the N-circuit is shorted, resulting in  $y_1=0$ , corresponding to the built-in end. This yields the circuit in Figure 4. The current source  $I_2$  is expressed in terms of the node voltage  $y_2$ , based on  $y_1=0$  and  $V_2=0$ . The node equation produces  $S=S^{*2}/P=0$  which is the characteristic equation for the cantilever beam. In must be noted that this analysis does not hold for the clamped-clamped beam since a defined above is itself the characteristic equation for the clamped-clamped beam.

Similar to the T-circuit analogy, slope is discontinuous at the cracked section (ay' =  $M_c/\kappa$ ), giving rise to two more unknown slopes. Such discontinuity is represented in the analog circuit by an admittance of magnitude - $\kappa$ . The two parts of the beam, divided by the cracked section, are each represented by a  $\pi$ -circuit as shown in Figure 5. The other continuity conditions are satisfied.

#### 3.0 General Two-Dimensional Frame Structure

In a generic model of a two-dimensional multi-storied frame, for which there are n-stories and m-spans (thus m+1 anchors), the analogous circuit network contains n(2m+1) interconnecting T-circuits. If there is a crack on any girder or any column, the number of T-circuits will increase by one. The magnitude of computation for modal frequencies involves principally the inversion of two matrices of orders (3nm - n+1) and (n) respectively.

In representing beam-frame structures, Il-circuits corresponding to individual columns and girders joining at right angles are interconnected such that boundary conditions at the analog-frame joints are observed. Kirchhoff's current law is written in terms of the node voltages which correspond to the angles of rotation at the frame joints. Under free vibration the coefficient matrix must be singular, and zeros of its determinant yield modal frequencies of the frame structure. Order of the matrix is equal to the number of frame joints. For each crack introduced in one of the beam elements, order increases by two.

\_:1

Order of the matrix involved for an n-story, m-span frame is thus n(m+1); n(m+1)+2 if there is a crack on any girder or column. The node equation can be established as  $(y - x^T)$ of order  $n \in X$  is n by n(m + 1), and Z is of order  $n \in X$  is n by n(m + 1), and of order  $n \in X$  is n by n(m + 1), and of order  $n \in X$  respectively in the presence of a crack). The coefficient matrix  $(U - X^T Z^{-1} X)$  is symmetric. A step-by-step schematic procedure will now be described to compute the entries of the individual matrices without drawing any equivalent cir-cuit. Reference will be made to Figure 6 which illustrates a two-dimensional frame with and with-out crack. For simplicity m = 1, n = 2, and uni-form properties are assumed. With reference to Figure 6, each beam element is identified by a number. The numbering order begins at the left lowest column, proceeds up through the columns on the same line in n stories, returns back to the second anchor, proceeds up vertically, and in that Once the columns are finished, girders on each floor are numbered progressively from left to right starting with the first floor and continuing or with the upper floors. Quantities related to a beam element such as S, T, S', etc. are subscripted by the number of the element. The node is numbered by the column under the node. If there is a crack on a column (girder), the original number of the element refers to the upper, (right) side of the column (girder) which is now represented by two beam elements. The lower (left) side is numbered following the largest number in the scheme. Due to discontinuity of slope at a crack, two new nodes are created on each side of the crack. In Figure 6b, cracks are represented by conductances  $-1/\beta\theta_k$ , where  $\theta_k$  = EI/L $\kappa_k$ is the sensitivity parameter [1] based on characteristic length L. The following steps will be presented in two parts:

### 3.1 Frame Without Crack (Figure 6a)

As a guidance y' and y vertors are arranged as  $y' = \{y_1 \ y_2 \ y_3 \ y_4\}^T$ ,  $y = \{y_1 \ y_2\}^T$  where  $y_1$  and  $y_2$  are the horizontal displacements of nodes 1 and 3, and 2 and 4, respectively.

#### 1) To establish U:

- a) diagonal entries  $u_{\hat{1}\hat{1}}$  corresponding to  $y_1'$  will be the sum of S values of the elements adjoining at the node i.
- b) off-diagonal entries  $u_{ij}$  will be  $T_k$  if ith and jth nodes are adjacent and kth beam element links them. Otherwise,  $u_{ij}$  = 0. Due to symmetry,  $u_{ij}$  =  $u_{ji}$ .

#### 2) To establish Z:

a). diagonal entries  $z_{1j}$  will be the sum of  $\beta_k$  value: of all the girder elements in the ith floor plus the sum of P values of all the columns adjoining at the ith floor, where  $\beta_k$  can be expressed in terms of  $\beta$  of the reference element as,  $\beta_k$  =  $e_k\beta$ .

b) off-diagonal entries  $z_{i,j+1}$  will be negative of the sum of P' values of all the culumns joining ith and i+1st floors.  $z_{ij}=0$  for j>i+2 and  $z_{ij}=z_{ji}$ . Z is hence a tridiagonal symmetric matrix.

#### 3) To establish X:

 $\chi$  is partitioned into m + 1 square submatrices of order n each. Namely,

$$x = [x^1 | x^2] \dots | x^{m+1}].$$

- a) diagonal entries  $x_{ij}^k = S_{n(k-1)+j}^* S_{n(k-1)+j+1}^*$ ,  $i=1,\ldots n-1$  and  $x_{nn}^k = S_{nk}^*$ . Referring to Figure 6a,  $x_{ij}^k$  for the kth "wall", wall denoting the union of all the columns on the same line, is equal to S' value of the column under the node n(k-1)+i mirus S' value of the column above the same node.
- b) off-diagonal entries  $x_{i,j+1}^k = -T_{(i-1)n+i+1}^k$  for  $i=1,2,\ldots,n-1$ .  $x_{i,j}^k = 0$  for  $j \geq 2$  and  $x_{i,j}^k = -x_{j,i}^k$  for  $i \neq j$ .  $x_{i,j+1}^k$  are thus tridiagonal matrices. Referring to Figure 6a,  $x_{i,j+1}^k$  is equal to the negative of the T' value for the column above node n(k-1)+i.

$$\overset{\chi^{T}}{Z}^{-1} \overset{\chi}{X} \text{ is thus in the form}$$

$$\overset{\chi^{T}}{Z}^{-1} \overset{\chi}{X} = \begin{bmatrix}
\overset{U}{U}_{11} & \overset{U}{U}_{12} & \cdots & \overset{U}{U}_{1,m+1} \\
\overset{U}{U}_{12}^{T} & \overset{U}{U}_{22} \\
\vdots & & \ddots & \vdots \\
\overset{U}{U}_{1,m+1}^{T} & \overset{U}{U}_{m+1,m+1}
\end{bmatrix}$$
(6)

where  $\mathbf{U}_{ij} = (\mathbf{X}^i)^\mathsf{T} \ \mathbf{Z}^{-1} \ \mathbf{X}^j$  are symmetric matrices of order n.

Based on the above procedure, the following matrices are obtained for the frame in Figure 6a:

$$\underline{U} = \begin{bmatrix}
S_1 + S_2 + S_5 & T_2 & T_5 & 0 \\
T_2 & S_2 + S_6 & 0 & T_6 \\
T_5 & 0 & S_3 + S_4 + S_5 & T_4 \\
0 & T_6 & T_4 & S_4 + S_6
\end{bmatrix}$$
(7)

$$\widetilde{Z} = \begin{bmatrix}
\beta_5 + P_1 + P_2 + P_3 + P_4 & -P_2' - P_4' \\
-P_2' - P_4' & \beta_6 + P_2 + P_4
\end{bmatrix} (8)$$

$$\chi = \begin{bmatrix} S_1' - S_2' & -T_2' & & S_3' - S_4' & -T' \\ & & & & & \\ T_2' & S_2' & & T_4' & S_4' \end{bmatrix}$$
(9)

#### 3.2 Frame With Cracks (Figure 6h)

y' and y vectors are now given as  $y' = \{y_1', y_2', y_3', y_7', y_8', y_8'\}^T$ ,  $y = \{y_1, y_2, y_7, y_8'\}^T$  where  $y_7$  and  $y_8$  are the deflections at the two cracks. Node equations corresponding to nodes which are not adjacent to a cracked element will remain the same relative to the previous case. The new matrices will be of the form

$$\underline{U}_{C} = \begin{bmatrix} \overline{\underline{U}} & \underline{\underline{A}} \\ \underline{\underline{A}^{T}} & \underline{\underline{B}} \end{bmatrix}, \underline{\underline{J}}_{C} = \begin{bmatrix} \overline{\underline{I}} & \underline{\underline{L}} \\ \underline{\underline{L}^{T}} & \underline{\underline{D}} \end{bmatrix}, \\
\underline{\underline{J}}_{C} = \begin{bmatrix} \underline{\underline{X}^{T}} & \cdots & \underline{\underline{I}}_{m+1} & \underline{\underline{L}}_{1} & \underline{\underline{L}}_{2} \\ \underline{\underline{L}}_{1} & \underline{\underline{L}}_{m+1} & \underline{\underline{L}}_{1} & \underline{\underline{L}}_{2} \end{bmatrix} (10)$$

where barred matrices are modified forms of Equations (7)-(9). ith row in  $\overline{y}$  is unchanged relative to y if the ithe node is not adjacent to a cracked element. ith row in  $\overline{\chi}$  remains the same if there is no crack on any column adjoining with the 1th floor.  $\overline{\chi}^k$  is the same as  $\chi^k$  if there is no crack on the kth wall.  $F_{x}=0$  if there is no crack on the kth wall and on any of the girders adjacent to the kth wall.

Following the procedure in Part 3.1, the submatrices for the frame in Figure 6b are obtained as  $% \left( \frac{1}{2}\right) =\frac{1}{2}\left( \frac{1}{2}\right) =$ 

$$\mathfrak{T} = \begin{bmatrix}
s_1 + s_2 + s_8 & \tau_2 & 0 & 0 \\
\tau_2 & s_2 + s_6 & 0 & \tau_6 \\
0 & 0 & s_3 + s_5 + s_7 & 0 \\
0 & \tau_6 & 0 & s_4 + s_6
\end{bmatrix}$$

$$\underline{B} = \begin{bmatrix}
S_7 - M_4 & M_4 & 0 & 0 \\
M_4 & S_4 - M_4 & 0 & 0 \\
0 & 0 & S_8 - M_5 & M_5 \\
0 & 0 & M_5 & S_5 - M_5
\end{bmatrix} (12)$$

where M<sub>k</sub> = 1/80<sub>k</sub>

$$\widetilde{Z} = \begin{bmatrix}
\beta_5 + \beta_8 + P_1 + P_2 + P_3 + P_7 & -P' \\
-P_2' & \beta_6 + P_2 + P_4
\end{bmatrix}, \quad \widetilde{C} = \begin{bmatrix}
-P_7' & 0 \\
-P_4' & 0
\end{bmatrix}$$
(13)

$$\underbrace{\mathbb{D}}_{0} = \begin{bmatrix} P_{4} + P_{7} & 0 \\ 0 & P_{5} + P_{8} \end{bmatrix}, \underbrace{\mathbb{X}}_{1} = \underbrace{\mathbb{X}}_{1}, \underbrace{\mathbb{X}}_{2} = \begin{bmatrix} S_{3}^{'} - S_{7}^{'} & 0 \\ 0 & S_{4}^{'} \end{bmatrix}$$
(14)

$$\underline{E}_{1} = \begin{bmatrix} 0 & 0 \\ \tau_{8}^{*} & 0 \end{bmatrix}, \underline{E}_{2} = \begin{bmatrix} \tau_{7}^{*} & -\tau_{4}^{*} \\ -\tau_{5}^{*} & 0 \end{bmatrix}, \underline{E}_{1} = \begin{bmatrix} -\tau_{7}^{*} & 0 \\ 0 & -\tau_{4}^{*} \end{bmatrix}$$
(15)

$$\underline{E}_{2} = 0, \underline{H}_{1} = \begin{bmatrix} S_{7}^{1} & -S_{4}^{1} \\ 0 & 0 \end{bmatrix}, \underline{H}_{2} = \begin{bmatrix} 0 & 0 \\ S_{8}^{1} & -S_{5}^{1} \end{bmatrix}$$
 (16)

The frequency analysis applied to a two-story single-span frame with six equal length elements and with data of relative changes of 0.010 and 0.015 in the first two frequencies respectively yields, under the assumption of presence of single crack, four possible damage pairs:  $(\theta_1, e_7) = (0.108, 0.906)$ ,  $(\theta_2, e_7) = (0.182, 0.816)$ , and due to symmetry,  $(\theta_3, e_7) = (0.108, 0.906)$ ,  $(\theta_6, e_7) = (0.182, 0.816)$ , where  $e_7$  indicates relative crack location measured from the lower end of each column. The crack is thus on one of the columns. In order to determire the actual damage pair within symmetry, relative change in the third frequency is required.  $(\theta_1, e_7)$  and  $(\theta_2, e_7)$  would produce relative changes of 0.0074 and 0.0155 respectively in the third natural frequency. It may be argued that if the relative change in the third frequency could not be measured, then it must be small and thus  $(\theta_1, e_7)$  or  $(\theta_1, e_7)$  is the likely damage pair.

#### 4.0 Conclusions

(11)

Use of circuit analogy in computing model frequencies of a two-dimensional multi-story frame with or without cracks on it has been developed into a formalized method. The method enables the study of effect of cracks on modal frequencies of frame structures, as well as determination of the

location and intensity of a crack, given sufficient number of modal frequency changes. Computation of modal frequencies of an natory maspin frame with k cracks on it requires finding zeros of a determinant of order n(m+1)+2k. In the finite element method, using generally required twenty elements per basic beam segment, there are 40 n(m+1) nodes each with two degrees of freedom. The size of computation savings is almost 40-fold. However, using circuit analogy in determining the location and intensity of a crack may involve n(2m+1) computations of zeros of a determinant of order n(m+1)+2.

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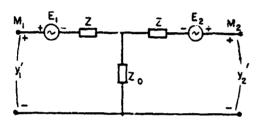


Figure 1. T-Circuit.

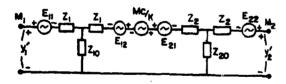


Figure 2. Fracture CKT.

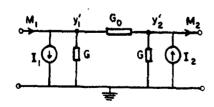


Figure 3. n-Circuit.

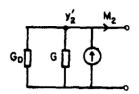


Figure 4. Analog circuit for a cantilever beam.

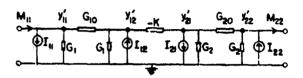


Figure 5. Fracture circuit.

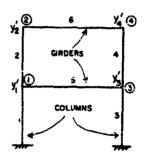


Figure 6a. Two-story, single-span frame without crack.

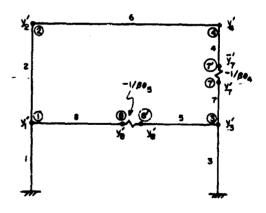
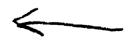


Figure 6b. Two-story, single-span frame with \*wo cracks.





DYNAMIC LOADING: MORE THAN JUST A DYNAMIC LOAD FACTOR

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#### ABSTRACT

The response of a simply supported beam to uniform blast loading is determined by using the normal-mode technique. Especially for short load durations the higher modes become important. The rotary inertia and shear force deformation have to be taken into account. At short load durations high peaks of shear force appear near the supports immediately after loading.

#### 1. INTRODUCTION

In literature such as TH 5-1300 [1] and Biggs [2] the starting points for the design of explosion resistant constructions are the static shapes of deflections of the construction parts and the static force distribution. For the dynamics usually a dynamic load factor is introduced. Experiments show clearly, however, that dynamics is more than just statics multiplied by a DLF. Plates that are simply supported at two opposite edges and would collapse in the middle in the event of static loading, appear to collapse close to the supports some times when exposed to a uniformly distributed explosion load, Apparently not only the amplitude, but also the shape of the deflection, shear force, and bending moment diagrams are influenced by the loading rate and the duration of the load. To get more fundamental insight in the dynamics of explosion loaded plates a theoretical study has been performed of the behaviour of an idealized simply supported elastic beam.
The beam will be subjected to an uniformly distributed blast load, i.e., the time variation in the load is the same at any point x. The blast load is simplified by a peak triangular pulse of variable duration.

#### 2. BERNOULLI-EULER BEAM

It is obvious to start with a simple primatic flexural beam that has uniform density  $\rho$  and has constant stiffness SI. The governing equation of motion during elastic response is the following well-known equation [3]:

$$EIW^{(n)}(x,t) + cA \ddot{W}(x,t) = q(x,t)$$
 (1)

This equation two.es into account transverse inertia and bending deformation. To solve this equation we use the normal-mode technique [3].

Express the transverse motion W(x,t) as the product of a time function G(t) and a displacement function F(x). For free transverse vibration (i.e., q(x,t)=0) each displacement function F(x) describing one of the normal modes of the beam gives a solution if G(t) is chosen as a periodic function with a period that corresponds to the mode under consideration.

Thus 
$$F_n(x) = \sin \frac{n\pi x}{1}$$
 and  $G_n(t) = A_n \sin \omega_n t +$ 

with 
$$\omega_n^2 = n^4 \pi^4 \frac{EI}{oAl^4}$$
 which gives for  $W(x,t)$ :

$$W(x,t) = \prod_{n=1}^{\infty} \sin \frac{n \pi x}{1} \left( A_n \operatorname{Sinw}_n^{t} + B_n \operatorname{Cosw}_n^{t} \right)$$
 (2)

A particular solution of eq. (1) can be found by splitting up the load function q(x,t) in function corresponding to the normal modes as well:

$$q(x,t) = \prod_{n=1}^{\infty} q_n(x,t) = \prod_{n=1}^{\infty} \sin \frac{n\pi x}{1} Q(t)$$
 (3)

The complete solution of eq.(1) can be found by combining the calculated responses for every a (x.t).

 $\mathbf{q}_n(\mathbf{x},t)$ . The constants  $\mathbf{A}_n$  and  $\mathbf{B}_n$  are established from the initial conditions. When the displacement  $\mathbf{W}(\mathbf{x},t)$  is known the bending moment  $\mathbf{H}(\mathbf{x},t)$  and shear force  $\mathbf{D}(\mathbf{x},t)$  can be calculated by the following equations

$$M(x,t) = - \Xi i W''(x,t)$$
 and  $D(x,t) = M'(x,t)$  (4)

Calculations have been made for several response durations [4]. Interesting responses are found for the extreme values of the triangular load, namely the step load and the impulse load.

Results of the step load are as follows:
As for the deflection, the bending moment and the shear forces, the maximum values are dominated by the lat mode response. Immediately after loading the influence of the higher normal modes are perceptible, but the corresponding response values are small kesults of the impulse load are as follows:
The deflections can be calculated and have the shapes as illustrated in Fig. 3. The bending moment calculations yield quite whimsical results, which cannot be clarified. The influence of the higher modes is very apparent.

For the impulse load it appears not to be possible to calculate the shear force. The series for the shear force does not converge. As a result of the calculations it can be said that for long load duration the first normal mode dominates the beam response i.e., for response calculations methods as given in [1] and [2] are useful. For very short load durations deflections can be calculated, but the calculation of bending moments yields doubtful results. High natural modes have to be taken into account, which mean that the influence of rotary inertion and shearing deformation cannot be neglected.

To enable the calculation of the beam response for short load duration a more complicated equation of motion is needed.

#### 3. TIMOSHENKO BEAM

An equation of motion that takes into account the influence of rotary inertia and shearing deformation is given by Timoshenko [3]. Fig. 1 shows a free body diagram of a beam element.

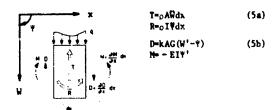


Fig. 1. Free body diagram of beam element

The equations of motion are derived from the equilibrium equations for forces and moments which after filling in the relation (5a) and (5b) result in

$$EIW'''+\rho AW-\rho I (1+\frac{E}{kG})W''+\frac{\rho^2!}{kG}W''=q-\frac{E!}{kAG}q''+\frac{\rho I}{kAG}\ddot{q}$$

$$EIY'''' + \rho AY - \rho I (1 + \frac{E}{kG})Y''' + \frac{\rho^2 I}{kG} W'' = q^4$$
 (6b)

Parameters W, Y, D and M are functions of x and t. To establish W(x,t), D(x,t) and M(x,t) we have to solve eq. (6a) and (6b). And here again the normal-mode technique described before is used. The determination of the frequencies of the normal modes produce two sets of natural frequencies' (see Fig. 2). This means that for each value of n there are two different frequencies. Analysis of the nature ofthe types of motions corresponding to these two sets of frequencies show [4]:

The lower frequencies in the first set describe mainly the bending part in the response and the higher frequencies in this set describe mainly the shear part in the response. Generally speaking this set of frequencies describes the transverse motion of the response.

The second set of frequencies originates from the coupling term for rotary inertia and shear force deformations in the equation of motion. The combination of this set to the response is equal for bending and shear but the corresponding displacements for shear and bending are always opposite in

phase. This results in a more longitudinal type of motion in the beam response.

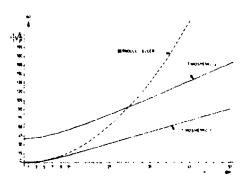


Fig. 2. Natural frequencies as function of n [4].

From Fig. 2 it is seen that for the Timoshenko beam the frequencies of the higher modes are proportional to n, the number of the mode, instead of n<sup>2</sup> in case of a Bernoulli-Euler beam. This means a better chance for determining the impulse response, including shear force, because the series will converge better. Response calculations [4] for the impulse load yield the deflection, bending moment and shear force diagrams shown in Fig. 3.

The parameter values used in the computation are:  $E = 30.10^9$ ,  $\rho = 2400$ ,  $\nu = 0.2$ , K = 0.845,  $\frac{1}{n} = 20$ .

The deflection is given for time steps  $\Delta t = \frac{1}{200} T_1$  where  $T_1$  is the duration of the first mode. The bending moments and shear forces are given for  $t = 1,6.10^{-5} T_1$ , 0,0006  $T_1$ , 0,005  $T_1$  and 0,0185  $T_1$  respectively.

Letter n denotes the number of natural frequencies that are taken into account. As unit for the scale is chosen the maximum value of deflection, moment and shear force respectively when only the first mode is taken into account.

Worth noting in Fig. 4 are in the first place the high shear force peaks at the supports immediately after loading and secondly the disturbances in shear force and moments that run from the supports to the middle of the beam. The velocity at which these peaks travel is about 2075 ms<sup>-1</sup> [4], which equals the Rayleigh wave velocity calculated from

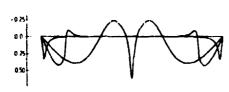
$$\frac{1.14v + 0.862}{1 + v} \checkmark \frac{G}{\rho}$$
 [5]  
with G = 1.25.10<sup>10</sup>  
v = 0.2  
 $\rho$  = 2400

This is a very promising result because a velocity of the order of the transverse wave velocity is expected. DEFLECTION

n = 41



BENDING MOMENT n = 251



SHEAR FORCE n = 2501

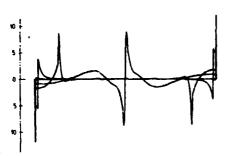


Fig. 3. Deflection, bending moment, shear force diagrams

Questions that remain are: what is the influence

of the damping on the results, and how close is

#### 4. DISCUSSION OF THE RESULTS

theory.

this approximation to reality. Damping: Especially for the shear force calculations which need a high number of natural frequencies [4] damping may be an important factor. The important peak values at the supports, however, appear immediately after loading so that damping does not have any influence here yet. In the middle of the beam the peak values may be a bit lower as a result of the reduced influence of the higher modes (Material damping in concrete - 0,01 for all frequencies [6]). Validation of the theories: The validity of the theories are judged on the basis of an example. Suppose a semi-infinite elastic beam having a circular cross-section with radius a. For the wave velocity c of a harmonic disturbance placed at the beginning of the beam an exact solution for v=0,29 is available (known as the theory of Pochhammer and Chree [7]). The wave velocity is also established with both the Bernoulli-Euler and Timoshenko

The wave velocity appears to be dependent on the frequency of the disturbance. The Bernoulli-Euler theory yields one dispersion relation, Timoshenko two, one for each frequency set, and Pochhaumer-Chree give an infinite number of dispersion relations.

The results are presented in Fig. 4. It shows the dispersion relations of Bernoulli-Euler and Timoshenko and three of the Pochhammer-Chree relations.

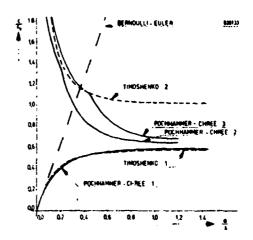


Fig. 4. Wave velocity as function of wave length

From Fig. 4 we learn the following:

- a. For increasing frequency values the B-E wave velocity reaches infinity. This means that high frequency disturbances are transmitted instantiously. Only very low frequencies coincide with the first F-C curve.
- b. The first P-C and tirst T wave velocity curves coincide and have as asymptote the Rayleigh wave velocity [4].
- c. The second T-curve envelopes the other P-C curves and has an asymptote the longitudinal wave velocity C<sub>O</sub> (velocity of sound).
- It can be concluded from this exercise that:
- BE-theory gives proper solutions for dynamic loads that are governed by low frequency components.
- T-theory can be applied in all cases. The measure in which this theory is exact is determined by the contribution of the second frequency set to the solution.

Calculations with the Timoshenko-theory applied to simple beams show that the response is mainly determined by the first frequency set. The influence of the second frequency set is strongest in the determination of the shear force. The difference in maximum shear force values calculated with or without the second frequency set, however, is less than 4 percent

#### 5. CONCLUSIONS

- a. For load durations t<sub>d</sub> > T<sub>1</sub> the first mode is governing the response. Methods for response calculations as given in [1] and [2] can be used.
- b. For load duration  $t_d \leq T_1$  higher modes have to be taken into account.
- c. For very short load durations t<sub>d</sub> << T<sub>1</sub> very high modes become important in the beam response. Rotary inertia and shearing deformation have to be taken into account.
- d. For short load duration peaks in shear force appear near the supports. These peaks are a qualitative explanation of the deviating fail behaviour mentioned in the introduction. To be able to design for these high shear force peaks it is necessary to know the material behaviour under extreme deformation rates.
- e. Thanks to the aid of the computer the analytical solution derived earlier leads readily to surprising results, which with the finite element methods which are frequently applied at present cannot or can hardly be determined.

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## THE EFFECTS OF INDIRECT-FIRE MUNITIONS ON FRAMED STRUCTURES

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ABSTRACT

TABLE 1. CRITICAL MID-MEIGHT LATERAL DEFLECTIONS

This paper reports an effectiveness evaluation
of the use of indirect-fire munitions against steel-
and reinforced concrete-framed structures in an
urban environment. Effects include collapse of
columns due to lateral blast loads, crushing of
columns by vertical blast loads, response of inter-
ior and exterior walls to blast and fragments,
response of personnel to blast overpressures and
wall debris, and the formation and location of
rubble caused by the detonations of these munitions,

#### "TYPICAL" STRUCTURES

Two "typical" office/hotel structures, each 200 ft by 200 ft in plan and ten stories tall, were designed using reinforced concrete or steel structural frames. Columns were spaced at 20-ft centers in each direction with a flour-to-floor height of 12 feet, and the designs were governed by References 1 and 2 for the concrete and steel structures, respectively. While the required column sections wary through the height of the structure, the firstfloor members are considered typical of all stories for ease of presentation. For the steel structure, the corner, exterior wall and interior columns are W8x67, W12x106 and W14x211 sections, respectively. The concrete corner column is 12 in. square with 5.08 sq. in. of steel reinforcement, the exterior columns are 16 in. square with 10.2 sq. in. of steel, and the interior columns are 22 in. square with 15.2 sq. in. of steel.

#### COLUMN RESPONSE TO LATERAL LOADS

An explosion between building floors will produce a lateral load and deflection on the columns between those floors. If the permanent deformation of the column, A, is great enough, the dead and live structural loads, P, will cause collapse of the column because of its inability to resist the now-combined axial load and moment produced by the deflection. The critical, mid-height deflection of the steel sections was calculated from

$$\Delta = \frac{1.18 \text{ M}_p}{P} (1 - \frac{P}{P_y})$$

where the moment capacity, M<sub>p</sub>, was determined for the weaker axis. The reinforced concrete columns were analyzed using conventional interaction diagrams. These critical deflections are summerized in Table 1.

Column	Deflection (inches)		
Location	Steel Column	Concrete Column	
Corner	5.4	6.9	
Exterior	5.8	10.7	
Interior	7.7	12.6	

The response of any of these columns to a lateral, time-varying load is dependent upon both the peak pressure or force and on its duration (impulse). Isodamage curves (relating the peak pressure and impulse required to provide the critical deflections of Table 1) were generated for a point load at mid-height of each of the mix column types. Since a blast does not produce a true point load, the pressures were assumed to act over an area equal to the exposed width of the column squared. These curves are displayed in Figure 1. A pressure/impulse pair falling above and to the right of a curve will produce a mid-height deflection greater than that specified in Table 1, while a pair below and to the left will produce a smaller deflection. The curves for the steel columns reflect bending about the weaker axis of the section.

All of the munitions selected for evaluation (the 105 mm HE M1, the 155 mm HE M107, the 8-in. HE M106 and the 4.2 in. mortar HE M329Al) are capable of producing the required minimum impulses shown in Figure 1, but the required stand-off distance from the loaded surface of the column is at most six inches. A blast this close to the column requires some means to assure detonation of the shell at that location, but no such mechanism exists. A direct hit is then the only way to destroy a column. The likelihood or probability of achieving a direct hit on the selected columns by any of the munitions above is, at best, a function of the probable errors (a round-to-round variation for a fixed aim point) in both range and deflection. References 3 through 6 provide these data for a chosen range of fire of 5000 meters. The number of rounds required to achieve a 0.95 probability of hit on a single column was calculated and results are presented in Table 2. It must be pointed out that these results assume that there are no mearby buildings which would interfere with incoming rounds and that the walls and upper floors of the structure under attack do not shield the interior columns. We also assume that none of the projectiles are duds. None of these conditions

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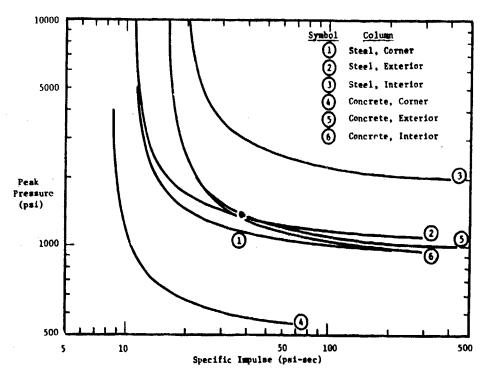


Figure 1. Isodamage Curves

TABLE 2. NUMBER OF SHELLS REQUIRED FOR A 0.95 PROBABILITY OF HIT ON A SINGLE COLUMN\*

		Steel Columns		C	Concrete Columns	
Shell	Corner	Exterior	Interior	Corner	Exterior	Interior
105 🖚	586	403	355	403	355	236
155 mm	564	393	324	393	324	233
8-inch	276	188	157	188	157	113
4.2" Morta	6240	4340	3608	4340	3608	2603

would exist in a real structure and with real projectiles; therefore, the number of shells required would be much higher than those shown in Table 2.

#### COLUMN RESPONSE TO VERTICAL LOADS

An artillery round detonating between floors of a framed structure will produce vertical loads on the columns supporting the floor slab and beams near the detonation point. These vertical loads are the result of the reflected pressure from the shell and of the quasi-static pressure buildup in the room in which the explosion occurs. Venting through windows is treated. This quasi-static pressure is a strong function of the volume into which the explosion products expand, and this volume is determined by the strength of the internal walls (weaker walls will be destroyed by the initial blast and will cause a

lower qua i-static pressure as the games expand into adjacent rooms). While the columns immediately under the detonation will likely crush, the columns which support them are protected somewhat in that the maximum load which they must resist is limited to the carrying capacity of columns above them. Extensive structural collapse from an internal detonation is thus possible but will not be discussed further because of the many unknowns which affect the pressure loadings.

# RESPONSE OF INTERIOR AND EXTERIOR WALLS TO BLAST AND FRAGMENTS

Exterior walls of framed structures serve primarily as an environmental shield and are not part of the load-carrying system of the building. They range in thickness from a heavy brick-and-block com-

bination to relatively light panels of glass, metal or other material. Interior walls range from nominal dry-wall construction to 4 in. hollow tile and planter. Reference 7 has given an average room size for these structures of 13 ft by 20 ft. If one of the previously listed rounds detonates in the center of such a room, any of the above walls will be removed by the resulting initial blast and/ or quasi-static pressure. There is the possibility, however, that the very early-time failure of light interior walls would sufficiently increase the volume into which the quasi-static pressure expands that the heavy exterior wall may scand after the detonation of a 105-un round.

The 105 um, 155 mm and 8 in. HE shells depend upon fragmentation for a major portion of their effectiveness against personnel. The Gurney equation (Reference 8) predicts initial fragment velocities of 2950 ft/sec, 3320 ft/sec and 3570 ft/ sec for these shells, respectively. An average fragment weight of 90 grains is typical. Fragments of this weight and the above velocities can perforate a wall consisting of a total of two inches of plaster and still have a residual velocity greater than that required to penetrate winter clothing (References 9 and 10). These fragments also have the capability to perforate up to three or more drywall partitions and still pose a severe threat to personnel in other rooms. However, the floor slabs form an effective shield protecting personnel on adjacent floors from fragments.

#### RESPONSE OF PERSONNEL TO BLAST OVERPRESSURE

The blast overpressure from a detonating shell can kill or injure nearby personnel through any of several mechanisms: primary blast (damage to aircontaining tissues of the lungs), secondary demoge (impact by objects which are accelerated by the blast), tertiary effects (whole body translation and impact on rigid surfaces), and eardrum rupture. Secondary damage will not be considered further. Researchers at the Lovelace Foundation (References 11 and 12) have developed pressure versus duration lethality curves for humans due to primary blast damage. These curves suggest that the initial blast at a distance of 10 ft from any of the selected munitions is below the threshold for lung damage, but the quasi-static pressure from the 8-in. shell in a 20 ft x 13 ft room will result in loss than 1% survival and the 155 mm shell will result in less than 10% survival. Personnel have a 98% or greater chance of survival from primary lung damage due to blast from the 105 mm or 4.2 in. mortar HE

Blast overpressure and impulse serve to produce whole-body motion and, if rigid impact surfaces are assumed, an impact velocity of 10 ft/sec represents a "mostly safe" level (References 12, 13 and 14). The method developed in Reference 15 indicates that the velocity imparted to a 154-1b (70 kg) person is much less than this "mostly safe" level.

Hirsch (Reference 16) has concluded that there is a 50% repoure probability of eardrums of exposed personnel at an overpressure of 15 psi, and Reference 13 supports this value for "fast" rising overpressures with durations of from 0.003 to 0.4 seconds. The threshold for eardrum rupture occurs at 5 pai. The direct blast from a 155 mm, 8-in. or 4.2-in, mortar shell in the 20 ft by 13 ft room exceeds the level for 50% eardrum rupture as does the quasi-static pressure from the 105 mm round. It must be observed that all of these blast effects or injuries are in addition to the more lethal fragmentation effects of the munitions.

#### PERSONNEL RESPONSE TO DETONATION DEBRIS IMPACT

The impact and point detonation of an artillery shell on the outside of a brick building wall will probably produce brick-size fragments in the room behind the wall. The velocity of these fragments is dependent on the amount of explosive in the shell, and the velocities for a 6.2-1b brick can range from 138 ft/sec to 300 ft/sec for 105 mm and 8 in. shells, respectively. The probability of death (P) from projectile-induced trauma to the thorax has been given in Reference 17 as

$$P = \frac{1}{1 + \exp\{\alpha + \beta \ln(MV^2/WD)\}}$$

where M = projectile mass, grams

V = velocity of projectile, m/sec

D - projectile diameter, cm

W - mass of target animal, kg

a = 34.90

6 - -4.39.

Combining the above brick mass and velocity with a 70-kg human target, the 105 mm, 155 mm and 8-in. shells all provide a probability of death greater than 0.95 for a person struck by such a projectile. There are, however, a very few such projectiles, and the probability of being hit by one in small.

#### FORMATION AND LOCATION OF RUBBLE &

Suscained artillery and aerial bombardments of World War II produced enormous quantities of building rubble from the collapse of the load-bearing brick wall structures which were prevalent at the time. Today's framed structures do not have the amounts of material available to convert to rubble if one agrees that the floor slabs of the structures will not be destroyed and that entire structures should not collapse. Shell detonations in the center of a room behind the building exterior walls will probably (as shown earlier) rupture those walls and propel the brick or other material pieces into the street below. The maximum ground range for a brick or block piece coming from the top floor of our "typical" building is approximately 25 feet. A 10-atory, heavy clad structure (brick and block exterior walls) will have around 38% of its exterior surface covered by glass (Reference 7), and the in-place volume of the wall materials is 39 ft<sup>3</sup> per foot of street frontage. If a 1.3 expansion factor is used to include the effects of partly bucken blocks and if the total exterior wall were blown out from the structure, the rubble volume would be 51 ft<sup>3</sup> per foot of building frontage. Each 13 ft by 10 ft room wall section must be removed individually. The

resulting rubble pile should be triangular in shape, extending 25 feet from the building base and approximately 4 ft deep at the building wall.

The debris from a light clad structure (glass, metal or other thin material exterior walls) can consist of a number of relatively large-in-area, thin panels. These walls have an average thickness of b.7 in. (Reference 7), of which 4.1 in. is light, non rubble-producing insulation. The expected ground range impact distance is difficult to predict because of lifting or sailing effects on the panels, and the expected rubble depth should be less than the effoct. Such walls would produce trash instead of rubble. Trash would not be an effective barrier to vehicular travel.

These rubble distribution patterns are based on wall failure under the effects of the direct blast from a shell detonating at room center. If a super quick fuze mode shell hits the outside vall, the debris will be blown into the building and will not contribute to the rubble in the street below. If the wall should fail under the quasi-static rather than initial blast loading, the debris velocities and ground impact distances would be slightly greater because of the increased impulse imparted to the wall materials.

#### SUMMARY

The above analyses have shown that modern, framed buildings should not suffer severe structural damage or collapse under the effects of the indirect fire munitions considered. The exterior and interior walls can be destroyed on a room-by-room basis, and personnel in the rooms on the same floor are not afforded any real protection against the normal fragmentation of the rounds. The rubble produced by artillory bombardments of urban areas should not seriously hamper vehicular traffic in the streets.

#### ACKNOWLED SEMENT

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# AD POOI735

MODELS FOR DAMAGE DIAGNOSIS IN SDF STRUCTURES

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#### **ABSTRACT**

In structural engineering it is imperative to design each system to survive the inputs anticipated over the design life of the structure. Strong motion inputs cause systems to execute nonlinear responses, and during strong motion responses structures accumulate damage. Therefore, the capability to model nonlinear response and to assess the damage level in a structure is essential for optimal design.

Techniques for the diagnosis of damage in inelastic structures have been developed. The dissipated energy in mechanical systems is taken as a measure of damage accumulation. Two models for the simulation of damaged structural response have been developed. The objective of this study is to use these models to estimate the amount of energy dissipated due to a strong motion input.

The results show that structural damage can be predicted, even in the presence of measurement noise.

#### 1. Introduction

The ultimate goal of the structural engineer is to design structures to survive preestablished environments. Structures subjected to strong motion inputs respond inelastically and accumulate damage. This damage accumulation may lead to failures. Therefore, in an accurate analysis of structural behavior, nonlinear response as well as the potential for damage accumulation must be considered. In this investigation, it is assumed that the dissipation of energy is related to the accumulation of damage.

To assess damage accumulation, a model describing structural behavior is required. This model is characterized by its parameters. In order to determine the parameters of a system, measured input and response data can be used with

Research Assistant, Dept. of Civil Engineering Associate Professor, Dept. of Civil Engineering Professor, Dept. of Mechanical Engineering a structural identification procedure. In this study the least squares approach is used to identify the parameters of damaged systems using simulated measured input and response data. In order to make the simulated data realistic the ideal input and response are first generated, then measurement noise is added to the signals.

Two models for the simulation of inelastic single-degree-of-freedom (SDF) structural response are proposed. The first is a higher order linear ordinary differential equation with constant coefficients. The second is a second-order linear ordinary differential equation with time varying coefficients. Methods for the identification of the parameters of these systems are presented in this paper.

The differential equation governing the response of an inelastic SDF system is a second-order ordinary differential equation with hysteretic stiffness term. Some recent investigations (e.g., Reference I) have used a higher order linear model to simulate the behavior of the actual system because the hysteretic character of the response of an inelastic system can be approximately matched by the hysteresis in the response of a higher order linear system.

It is known that a structure subjected to an extreme environment displays a response with time dependent characteristics. Particularly, a structure executing an extreme response can display diminished stiffness and variable damping. The investigation summarized in Reference 2 Gemonstrates this behavior.

As damage accumulates in a structural system, its strength diminishes. It is assumed that dissipated energy is a measure of structural damage. As the energy dissipated by a system increases, the residual strength decreases. The basis for this assumption is established in Reference 3.

The objective of this study is to demonstrate that the two models described above can be used to simulate the response of a damaged structure. The relative merits of each model are discussed. The results of some numerical experimentation using simulated data are presented. These investigate the feasibility and accuracy of the models.

# 2.0 Parameter Identification for Structural Hodels

The differential equation governing the response of an SDF system is

$$m\ddot{z} + u = f \,, \tag{1}$$

where m is the structural mass, z is the displacement response, dots denote differentiation with respect to time, f is the forcing function, and u is the restoring force. This equation models the response of an actual system. When the system response is nonlinear, u(t) is a complicated function reflecting the hysteretic character of the system. In this study, two models will be developed to simulate the behavior of a hysteretic system. These are equivalent linear models.

#### 2.1 Higher Order Linear Model

The first model to be considered is a higher order linear equivalent model. It is assumed that the restoring force in Eq. 1 is governed by the equation

$$\sum_{j=0}^{M} c_{j} u^{(j)} = c_{M+1} \dot{z} + z, \qquad (2)$$

where  $c_j$ ,  $j=0,\ldots,M+1$  are constants characterizing the model; a superscript (j) refers to the jth time derivative of the quantity it follows; and M reflects the order of approximation of the linear system to the actual system. The objective of the analysis is to use measured data to identify the parameters in the model. Once this is some, the energy dissipated in the system during structural response can be evaluated.

The following procedure is used to perform the parameter identification for the higher order linear model. Combine Eqs. 1 and 2 in the following way. Solve Eq. 1 for u, then take derivatives of the resulting expression. Use these in Eq. 2. The result is

$$\sum_{j=0}^{M} c_{j}(f^{(j)} - mz^{(j+2)}) = c_{M+1} \dot{z} + z .$$
 (3)

Since the parameter identification is to be carried out in the frequency domain, Fourier transform Eq. 3. Evaluate the modulus squared on both sides of the equation; the result is

$$\left|\sum_{j=0}^{M} c_{j}((i\omega)^{j} F(\omega) - m(i\omega)^{j+2} Z(\omega))\right|^{2}$$

$$= \left|\left(c_{M+1}(i\omega) + 1\right) Z(\omega)\right|^{2}.$$
(4)

This equation is assumed to govern the response amplitudes in the frequency domain. If 1) the system under consideration were linear, 2) all measurements were noise free, and (3) all Fourier transforms were exact, then measured data could

satisfy Eq. 4. But Eqs. 1 and 2 are meant to model nonlinear systems; noise is practically always present in physical signals, and the discrete Fourier transform is often used in practical analyses. Therefore, measured data will not generally satisfy Eq. 4. An error term,  $\epsilon(\omega)$ , must be added to Eq. 4 to establish equality. This yields

$$\varepsilon(\omega) = \left| \sum_{j=0}^M c_j ((i\omega)^j \ F(\omega) - m(i\omega)^{j+2} \ Z(\omega) \right|^2$$

$$-\left|\left(c_{M+1}(i\omega)+1\right) \ Z(\omega)\right|^{2},$$
 (5)

where  $F(\omega)$  and  $Z(\omega)$  are the Fourier Transforms of the measured input and response signals. The optimum model parameters are those which minimize the error, in some sense,

Define the square of the model error as follows.

$$e^2 = \int_{\omega_a}^{\omega_b} e^2(\omega) d\omega$$
 (6)

 $\omega_{a}$  and  $\omega_{b}$  are frequencies which band the characteristic frequency of the SDF system. The system constants,  $c_{j}$ ,  $j\approx0,\dots,M+1$ , are those whose values satisfy the sequence of equations

$$\frac{ac^2}{2c_j} = 0$$
,  $j = 0,...,M + 1$ . (7)

These constants are optimal in a least squares sense.

In this investigation computations involving two specific cases, where M = 0 and M = 1, were performed. The governing equations (Cq, 3) in these cases are second and third order differential equations, respectively. In all cases, a search procedure can be used to solve Eqs. 7. In the cases where M is shall, approximate analyses can also be executed.

When M = 0, the constants  $c_0$  and  $c_1$  must be evaluated. An approximate analysis can be carried out (Reference 3) where small-valued cross terms are neglected. Then the solution of Eqs. 7 can be evaluated in closed form. Numerical investigations have shown the approximate analysis to be quite accurate in this case.

When N>1 approximate analyses of Eqs. 7 can still be performed, but more accurate results are obtained using an exact search procedure. In the present study an iterative Newcon-Raphson approach was used to find the solution of Eqs. 7. Other techniques, including gradient search techniques, can also be used to solve Eqs. 7. Numerical examples have shown that the analysis described here can be executed.

Some numerical examples, solved using the techniques developed in this section, are summarized in Section 3.0.

#### 2.2 Time Varying Linear Model

The second model for inelastic system response is a time varying linear model. It is assumed that the restoring force in Eq. 1 is governed by the equation

$$u(t) = c(t) \dot{z} + k(t) z$$
, (8)

where c(t) is a time varying damping and k(t) is a time varying stiffness. The specific forms used to represent c(t) and k(t) are given below.

$$c(t) = (1 + \alpha t) c_0$$
, (9)

$$k(t) = (1 + \beta t) k_0$$
 (10)

 $\alpha,\ C_0,\ \beta,\ and\ k_0$  are constants. As in the previous analysis, the objective is to use measured data to identify the parameters in the model. Once this is done, the energy dissipated in the system during structural response can be evaluated.

The following procedure is used to perform the parameter identification for the time varying linear model. It is assumed that the parameters a and B are relatively small compared to one. Then the perturbation method can be used to express the response. The response is assumed to be approximately

$$z(t) = z_0(t) + \alpha z_\alpha(t) + \beta z_\beta(t)$$
. (11)

This expression can be used, along with Eqs. 8, 9, and 10, in Eq. 1 to obtain the governing differential equation. The coefficients of the terms 1, a, and 8 can be established, and equated to zero, to obtain the sequence of governing equations

$$m\ddot{z}_{0} + c_{0}\ddot{z}_{0} + k_{0}z_{0} = f$$
, (12a)

$$m\ddot{z}_{a} + c_{0}\dot{z}_{a} + k_{0}z_{a} = -c_{0}t\dot{z}_{0}$$
, (12b)

$$m\ddot{z}_{g} + c_{0}\dot{z}_{g} + k_{0}z_{g} - k_{0}tz_{0}$$
 (12c)

Since the parameter identification is to be carried out in the frequency domain, Eqs. 11 and 12 must be Fourier transformed. The results are

$$Z(\omega) = Z_0(\omega) + \alpha Z_0(\omega) + \beta Z_0(\omega) \qquad (13)$$

$$(-mu^2 + 1c_0u + k_0) Z_0(u) = F(u)$$
 (14a)

$$(-mu^2 + ic_0u + k_0) Z_{\alpha}(\omega) = c_0(Z_0(\omega) + \omega Z_0^*(\omega))$$
(14b)

$$(-m\omega^2 + ic_0\omega + k_0) Z_{\mu}(\omega) = -ik_0 Z_0^*(\omega)$$
 (14c)

where  $Z(\omega)$ ,  $Z_0(\omega)$ ,  $Z_0(\omega)$  and  $Z_g(\omega)$  are the Fourier transforms of z(t),  $z_0(t)$ ,  $z_g(t)$  and  $z_g(t)$ ; and primes denote differentiation with respect to frequency.

Equations 14 can be solved sequentially and used in Eq. 13 to obtain an approximate expression for the Fourier transform of the response. The modulus of the resulting equation can be evaluated to obtain

$$|Z(\omega)| = |\{1 + cc_0(H(\omega) + \omega H^*(\omega))\}|$$

+ 
$$(\alpha c_{\alpha} \omega - ik_{\alpha} B) H^2(\omega) F'(\omega)$$
 (15)

where

$$H(\omega) = [(k_o - m\omega^2) + i(\omega c_o)]^{-1}$$
. (16)

This equation is assumed to govern the response amplitudes in the frequency domain. Measured data will not generally satisfy Eq. 15 for the reasons discussed following Eq. 4. An error term  $c(\omega)$ , must be added in Eq. 15 to establish equality when measured data are used. Let  $Z^{(m)}(\omega)$  be the modulus of the Fourier transform of the measured response. Then,

$$e(\omega) = |Z(\omega)| - |Z^{(m)}(\omega)|,$$
 (17)

where  $I(\omega)$  is the expression obtained when the Fourier transform of the measured input is used on the right side of Eq. 15.

The optimum model parameters can be détermined, in a least squares sense, by minimizing the square of the model error. The square of the model error is

$$c^2 = \int_{-\infty}^{\infty} c^2(\omega) d\omega$$
 (18)

 $\mathbf{u}_a$  and  $\mathbf{u}_b$  are frequencies banding the characteristic frequency of the SDF system. The error is minimized when the model parameters are chosen to satisfy

$$\frac{3e^2}{3a} = 0 = \frac{3e^2}{3c_0} + \frac{3e^2}{38} = \frac{3e^2}{3k_0}.$$
 (19)

These equations can be solved simultaneously using a search procedure. In this study an iterative Newton-Raphson approach was used to solve Eqs. 19. Other search techniques could also be used.

Some numerical examples were solved using the technique developed in this section. One of these is summarized in Section 3.0.

#### 2.3 Computation of Dissipated Energy

It was stated in the introduction that the energy dissipated in a structure is a measure of the damage accumulated in the system. The energy dissipated in a structure can be calculated in the process of computation of the structural response. Once the parameters of a structural system have been identified the restoring force can be calculated using either  $\Gamma_{\rm s}$ , 2 or Eq. 8. The formula for dissipated energy is

$$\hat{F}_{0} = \int_{z(-\infty)}^{z(n)} u(z) dz , \qquad (20)$$

where u(z) is the restering force as a function of displacement, and  $z(-\omega)$  and  $z(\omega)$  are the displacements at the times minus and plus infinity. A change of variables can be made in the above expression to obtain

$$E_{D} = \int_{-\infty}^{\infty} u(z(t)) \dot{z}(t) dt . \qquad (21)$$

In the numerical solution of Eq. 1, z, ž, z, and u are determined at each time step. The energy dissipated can be incrementally computed using these values.

#### 1.0 Numerical Example

Two numerical examples are solved in this section using the approaches established in Section 2. In both examples the parameters of an SDF system are identified. The higher order linear model of Section 2.1 and the time varying linear model of Section 2.2 are used. The parameters of the higher order linear model are identified for the cases where M = 0 and M = 1. Once the model parameters are identified, the method of Section 2.3 is used to calculate the energy dissipated in each model.

The input used in this study is an oscillatory random function with decaying exponential amplitude. The input is modeled by the expression

$$f(t) = e^{-at} \sum_{j=1}^{N} c_{j} \cos(\omega_{j} t - \phi_{j}) , \qquad 0 \le t \le T .$$

(22)

a is the amplitude decay rate of the input; N is the number of harmonic components in the input;  $c_j,\ j=1,\ldots,N$  are the input amplitudes;  $\omega_j,\ j=1,\ldots,N$  are the frequencies where the input has power,  $\phi_j,\ j=1,\ldots,N$  are mutually independent uniform random variables distributed on the interval  $(-\pi,\ \pi)$ . The input is an approximately normally distributed, nonstationary random process. The parameters of the input used in the examples are listed in Table 1.

Table 1. Parameters of the Forcing Function

$$a = 0.1$$
  $N = 50$   
 $c_j = 10.0$ ,  $j = 1,...,50$   
 $\omega_j = (1.8 + 0.008 j) \pi$ ,  $j = 1,...,50$ 

The input generated using these parameters is shown in Figure 1.

In each example a different SDF system was analyzed. In the first example a linear system was considered. In the second example a polinear hysteretic system was used. The system parameters are listed in Table 2.

Table 2. Sysiem Parameters

Example 1	Example 2
m = 1.0	m = 1.0
c = 1.26	c = 1.26
k = 39.48	k = 39.48
E <sub>D</sub> = 11028	k <sub>y</sub> = 0
	D = 4.0
	E <sub>D</sub> = 8225

m, c, and k are the mass, damping, and elastic stiffness. ky and D are the yield stiffness and yield level of the inelastic system. The actual response of the inelastic system is shown in Figure 2. The energy dissipated during each response is given in Table 2.

It is assumed that noise may be present when the input and response are measured. To simulate this, the generated input and response are modified by the addition of white noise. A ten percent noise-to-signal ratio was used in the examples. The noisy input and inelastic response of Example 2 are shown in Figures 3 and 4.

The parameters of the higher order linear model (M = O and M = 1) and the time varying linear model were identified using the input and the responses, described above, in a computer program—(Reference 3). The parameter identification was performed using both the noise-free and noisy signals. The results of the computations are given in Tables 3, 4, and 5. The model responses are compared to the actual response in Figures 5, 6,

Table 3. Linear Model Parameters (M = 0), Energy Dissipated

		ree Case Response:	Noisy Case Actual Response:		
c o	Linear (ex. 1) 40.0	Nonlinear (ex. 2) 34.6	Linear (ex. 1) 39.2	Nonlinear (ex. 2) 32.0	
c 1	1.28	1.75	1.37	1.95	
ED	10720	7700	10900	6476	

Table 4. Linear Model Parameters (M = 1), Energy Dissipated

	Noise-Free Case Actual Response:		Noisy Case Actual Response	
	Linear (ex. 1)	Nonlinear (ex. 2)	Linear (ex. 1)	Nonlinear (ex. 2)
c o	39.2	30.3	34.3	32.0
c 1	1.28	3.95	2. <b>9</b> 8	2.60
C 2	0	0.07	0.05	0.02
E	11090	7598	11710	6803

Table 5. Time Varying Linear Model Parameters, Energy Dissipated

		ree Case Response:	Noisy Case Actual Response:		
	Linear (ex. 1)	Nonlinear (ex. 2)	Linear (ex. 1)	Nonlinear (ex. 2)	
G	0	0.0010	-0	0.011	
c <sub>0</sub>	1.27	1.71	1.29	1.54	
ß	0	-0.9078	-0	0.0026	
k <sub>o</sub>	39.3	40.3	38.4	32.8	
£D	10741	8186	10929	7016	

and 7 for Example 2 (where the actual response is nonlinear).

The results show that all models match the actual response quite well. Especially, the peak response in each model matches the actual peak response well. Of course, the linear models do not permit permanent set; therefore, the final displacement of each model is in error. Using displacement response as a criterion, the third order and time varying models appear to provide the best results. Using dissipated energy as a criterion, the time varying model provides the best result.

#### 4.0 Summary and Conclusions

The objective of this study was to develop approximate linear models for the simulation of inelastic system response and the measurement of damage accumulation in a structure. It was assumed that energy dissipated is related to the accumulation of damage. The model parameters were identified, then the energy dissipated during a strong motion was calculated. The displacement response and the energy dissipated in each model were compared with the displacement response and energy dissipated in the actual structure.

Three basic models were considered in this study. These are second- and third-order linear models with constant coefficients, and a second order linear model with time-varying parameters. The frequency domain approach was used in all the parameter identification computations.

The results of the numerical examples lead to the following conclusions.

- 1. Linear and nonlinear hysteretic SDF systems can, in some respects, be accurately modeled using second- and third-order linear differential equations with constant coefficients, and a second-order linear differential equation with time-varying coefficients. The models provide accurate simulations when displacement response and energy dissipated criteria are used.
- The frequency domain approach can be used to identify model parameters of all three models when the force and response measurements are noisy.
- 3. The second-order model with time-varying coefficients provides the best simulation of system response and energy dissipated among the three models considered.

#### **Acknowledgement**

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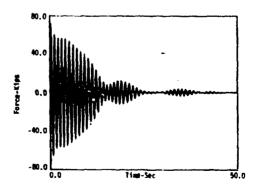


Figure 1. Signal used to simulate actual input.

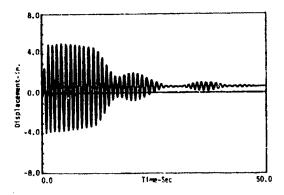


Figure 2. Signal used to simulate actual displacement response.

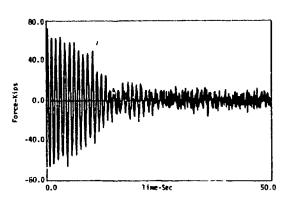


Figure 3. Input force plus noise.

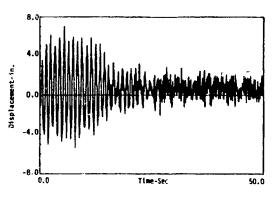


Figure 4. Displacement response plus noise.

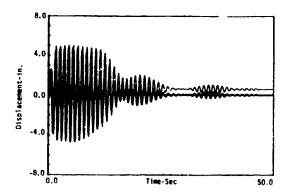


Figure 5. Comparison between actual response (thin line) and model (M = 0) response (thick line).

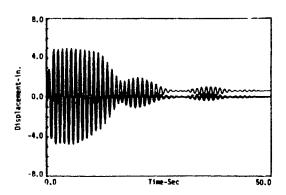


Figure 6. Comparison between actual response (thin line) and model (M = 1) response (thick line).

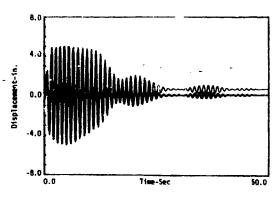
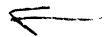


Figure 7. Comparison between actual response (thin line) and model (time varying parameter) response (thick line).



#### TODAY'S CONSTRAINTS DRIVE ANNO MAGAZINES UNDERGROUND

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#### **ABSTRACT**

Aboveground magazines for storage of ammunition are increasingly difficult to accommodate within constraints imposed by explosives safety, physical security, survivability, and fleet operational requirements. The Navy has developed an alternative design concept, called a chimney magazine. The chimney magazine consists of a box for weapons storage, two chimneys for access to storage, a horizontal sliding door over each chimney, a blanket of soil over the box, and a straddle trailer to retrieve and transport weapons. The concept dramatically increases the physical security and survivability of storage and dramatically decreases the encumbered land area without compromising explosives safety requirements for noncommunication of explosions, damage to storage from explosions, and protection of life and property in inhabited areas from blast, ground shock, and debris. It is concluded the chimney magazine offers high potential of being a cost effective concept to meet DOD requirements for tomorrow's ammo depot,

#### INTRODUCTION

Ammunition storage magazines comprise the largest investment of repl property inventory at abore activities supporting the Naval ammunition logistics system. The traditional magazine design is an aboveground, arch- or box-shaped structure berned with soil. The soil bern, 2 feet deep over the roof, extends burisontally beyond the walls where it slopes down over three sides of the structure. The fourth side is a vertical headwall with Goors for h rizontal access to storage. The design courept is perennial, dating back almost to the discovery of gun-powder.

Safety is achieved by separation distance. Freedom from risk of sympathetic detonation between magazines is achieved by providing a minimum separation distance between magazines. Freedom from risk of damage to contents from emplosions in other magazines is achieved by blast hardening headwalls and doors. Safety of unrelated areas outside the magazine depot is achieved by providing sufficient separation distance to limit the risk of injury and damage from blast, fragments and debris caused by an imadvertent emplosion. For 350,000 pounds Net Emplosive Weight (NEW) of storage per magazine, the required separation distance to unrelated areas exceeds 3,524 feet and encumbers over 896 acres of land.

#### PROBLEM

The existing concept for ammo storage encumbers large areas of valuable real estate - at a time when the Navy is already faced with a rising cost of land acquisition (which is sometimes not available at any price), shrinking supply of buildable land, and increasing encroachment by the private community. Further, aboveground magazines provide limited physical security - at a time when both the terrorist threat and the arms, ammunition and explosives requiring secure storage are increasing. The problem is particularly acute at coastal activities and certain installations in Europe. Faced with this dilemma, the Navai Civil Engineering Laboratory (NCEL) is developing techaclogy and concepts for alternative solutions. The goals are new design concepts for ammo storage, maintenance, testing and transfer facilities which are affordable and also meet explosives safety, physical security, survivability, and fleet operational requirements.

#### SOLUTION

A new design concept fo, ammo storage magazines is illustrated in Figures 1 and 2. The



Figure 1. Ammunition depot of chimney magnaines.

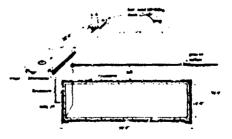


Figure 2. Interior of chimney magazine.

magazine depot has a flat surface. The minimum spacing between magazines in any direction is about  $1.50^{1/3}$ , where W is the MEW limit of any magazine. This is the minimum spacing allowed by DOD explosives safety standards to prevent explosion communication between underground storage chambers. For W = 300,000 pounds MEW, the minimum spacing between magazines, would be 100 feet, compared to 84 feet  $\left(1.25\text{W}^{1/3}\right)$  side-to-side spacing and 402 feet  $\left(6\text{W}^{1/3}\right)$  front-to-rear spacing required by DOD safety standards for aboveground, earth-covered, box-shaped magazines.

Essential elements of the design concept are a rectangular-shaped box for weapons storage, two chimneys for access to storage in two bays, a horizontal sliding door over each chimney, a blanket of soil over the storage box, and a straddle trailer to retrieve and transport weapons.

Storage Box: Ammunition is stored in a large box-shaped structure constructed of conventional reinforced concrete. Many magazines in the current Navy inventory are arch-shaped structures but studies of the present and projected types and mix of Navy weapons call for a box-shaped structure for maximum space utilization. Interior dimensions of the box are about 70 x 70 x 18 feet high. The box has two storage bays, separated by two reinforced concrete columns designed to safely support the roof loads (Figure 3). The entire box is designed to safely resist dead plus live loads. Effects from an explosion in an adjacent magazine are not expected to dictate the design loads - the effective mass of the roof slab plus the soil above it should be sufficient to safely absorb the blast energy from explosions in other magazines. The storage capacity of the box is about 300,000 pounds NEW.

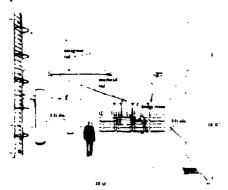


Figure 3. Cargo transport system inside chimney magazine: overhead-rail system and bridge crane.

Chimney Access: Access to storage is through a reinforced concrete chimney cast monolithic with the storage box, as shown in Figure 2. A chimney is located at one end of each bay to service storage in its bay. Interior horizontal dimensions of the chimney are about 28 x 6.5 feet to allow easy access to the largest containerized weapon and palletized unit of ammunition in the projected Navy inventory. The chimney extends about 12 inches above the elevation of the soil blanket. The chimney easion above the ground surface serves

as a curb to prevent surface water from entering the chimney and to force alignment of a straddle trailer over the chimney.

An interior view of the chimney is shown in Figure 3. The floors of the chimney and box are at the same elevation. Each chimney has a personnel access-escape ladder and a floor drain leading to a sump pit. The area of the vertical wall common to the chimney and storage box is open for ease in moving weapons between the chimney and box.

Sliding Door: Each chimney in the magazine depot supports a horizontal sliding door, as shown in Figures 1, 2 and 4. The door, constructed of massive concrete and steel, is designed to safely resist the blast overpressure from an explosion in an adjacent magazine. It also is expected to meet minimum requirements of a high-mecurity door to provide a minimum delay time for forced entry. Further, the mass and construction of the door can provide a much longer delay time to a larger spectrum of terrorist attack scenarios, compared to conventional hinged and hanging vertical doors common to aboveground magazines.



Figure 4. Blast-resistant, high-security sliding door over chimeny.

The door consists of two leafs. Each leaf has heavy-duty rollers that ride on the chimney curb and set in groves when the door is either open or closed. The mass and mechanical system of the door is such that only the straddle trailer can operate the door. A circular hatch in one door leaf allows for personnel access via the chimney ladder.

Bridge Crane: Pallets of bombs or gun ammunition and metal containers of missiles, torpedos or mines are transported between the storage bay and its chimney by a bridge crane, illustrated in Figure 3. The bridge crane, one in each bay of the storage bex, rides the full length of the storage bay on two overhead rails fastened to the ceiling of the storage box. All cargo in a bay is serviced by its own bridge crane; no cargo passes across the column line of the storage box. Hetal containers are fastened to their spreader bar and lifted by a hoister (mechanical or electrical) connected to the bridge crane. Transport of pallets is similar except the pallet is lifted by metal forks that reach under the pallet like "stacker" blades. The overhead rails in the chimney area span the width of the chimmey to ledge supports on the far wall of the chimney. When not in use, the overhead rails in the chimney area swing back into the storage box to allow unobstructed flow of cargo up and down the chimney.

1 L

Design of the cargo handling system in the storage box is extremely critical to acceptance by field personnel and safety authorities. Haintainability, availability, simplicity and reliability of operation are paramount. The bridge crane concept is no panacea – alternative cargo handling systems must be studied.

Soil Blanket: The soil blanket forms a flat surface over the entire magazine depot (Figure 1). The depth of soil over each storage box is the key to explosives safety performance and reduction in eucumbered land area. Given an inadvertent explosion involving the entire rated MEW capacity of the magazine, the soil blanket serves three very important functions.

First, the soil blanket must provide sufficient mass to limit shock waves reaching the atmosphere to those escaping from the two chimseys - not through the roof. Thus, the roof must not breach and offer a major escape route for shock waves before internal pressures have decayed sufficiently. Given the desired performance, the far-field blast environment will be significantly less than that from the same explosion in an aboveground magazine. Consequently, the required separation distance to unrelated areas, e.g., inhabited facilities, is significantly less than that required for an aboveground magazine.

Secondly, the soil blanket serves to reduce the maximum possible strike range of concrete debris missiles significantly below that from an aboveground magazine. The logic is an follows. The total shock plus gas impulse applied to the roof slab plus soil cover must equal the charge in their momentum. Therefore, the initial launch velocity of concrete debris missiles is directly proportional to the total mass of the roof slab plus soil cover per unit area of roof slab. Thus, doubling the soil depth reduces the launch velocity of concrete debris missiles by almost one-half. Finally, reducing the debris launch velocity by one-half happens to reduce the maximum possible strike range of debris missiles by a factor of four. Thus, the maximum possible strike range of debris is inversely proportional to the square of the soil depth, approximately.

Third, the mass of the soil blanket substantially reduces the threat of forced entry into the magazine via the roof, which is a custern for standard aboveground magazines.

Simply stated, the soil blanket allows the Navy to release land normally encumbered by explosives safety arcs and to significantly enhance the physical security and survivability of storage. The cost-benefit of this strategy depends upon the cost of soil fill (or excavation as the case may be) and the value of Navy real estate. Based on the high value of coastal real estate and the extent of encroachment by the private community, a cost-benefit analysis is expected to show that the Mavy can easily justify today's market price of straddle trailegs and the extra soil fill and/or excavation associated with chimney-magasines.

Straddle Trailer: Pallets of ammunition and containers of weapons are moved to and from the storage box, via the chimney, and transported over land in the straddle trailer shown in Figures 1, 5 and 6. The straddle trailer is a rubber-tire vehicle

with a steel frame superstructure and a timber bed or platform. The platform is allowed to be raised or lowered by means of a motor-driven winch attached to the trailer frame. The lift capacity of the straddle trailer is about 20 tons.

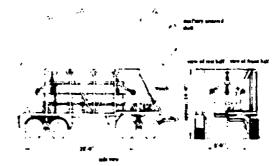


Figure 5. Straddle trailer for retrieving ammo from magazine and over land transport.

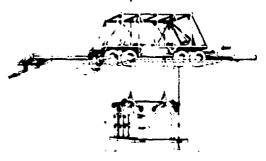


Figure 6. Straddle trailer lowering its platform with ammoload down chimney.

The straddle trailer passes cargo into and out of the storage box as follows. To retrieve cargo, the straddle trailer is first drawn into position over the chimney. The chimney curb assures alignment. Hext, the trailer winch is used to liftand-slide open both leafs of the chimney door. The mass and mechanical system of the door allows only the straddle trailer to open the chimney door - physical security is thus assured. trailer platform is then lowered down the chimney to its floor. Guide wheels above the trailer platform assure alignment of the platform in the chimney and prevent sparks from friction. Should the trailer winch malfunction, safety against freefall of the platform is assured by a dog-ear ratchet guide fastened to each wall of the chimney. probe under the platform sounds a bell on the trailer and gears down the winch when the platform is within 6 inches of the chimney fluor.

Once the platform rests on the chimney floor, the overhead rail extensions in the storage-box are awang out into position across the chimney. This allows the bridge crane to position its cargo on the platform. The platform loaded, the overhead rails are swung back out of the chimney. The trailer winch now raises the platform up the chimney and automatically locks it into position on the straddle trailer. During the lift operation, the dog-ear ratchet operates in reverse to prevent possible free fall of the platform and its cargo.

The trailer winch is then operated to close and lock the chimmey down. Locked and loaded, the streddle trailer is pulled away by a vehicle to its final destination.

The physical security of ammunition during transportation is an ever increasing concern. The straddle trailer can be easily outfitted with a "SAFEPOT" type armored shell to provide required levels of physical security for special weapons. The armored shell would be optional equipment.

At a transfer point, the platform of the straddle trailer is raised or lowered to the deck elevation of the other vehicle, e.g., rail boxcar, or platform, e.g., deck of pier, to facilitate transfer of the cargo.

The straddle trailer and vertical access to storage are counter to tradition, i.e., horizontal access to magazine and forklift trucks for cargo handling. But vertical passage of amounition is not new to the Navy - all amounition ships pass cargo vertically into magazines located below deck. Further, the straddle trailer is not new - the agriculture industry in California has used straddle trailers for years to retrieve produce in the field and haul it over the highway to processing plants. Thus, the straddle trailer is a reliable concept that has already been debugged. Given deployment of the concept, the straddle trailer would become as common and popular as forklift trucks are today at Naval Ordnance Activities. Transportation of all amountion within the confines of the Navy base would be by a single type of equipment - the straddle trailer.

The acquisition cost of the straddle trailer is not cheap - but neither is a forklift truck. The estimated cost of a straddle trailer is \$100,000 without an armored shell. The cost of a forklift truck is about \$80,000.

#### PERFORMANCE

Major performance goals are achieved with a chimney magazine. Physical security and survivability of storage increase dramatically. Encumbered land area decreases dramatically. Bot h benefits are achieved without degrading the level of explosives safety and without substantial increases in the construction cost. Achievement of these goals stems from the application of new NCEL technology to the design and predicted performance of a chimney magazine. Among the technologies are criteria for the external blast environment from confined explosions, the effects of semi-frangible covers on the blast environment inside structures containing explosions, the effects of internal explosions on the dynamic response of soil-covered structures, and the delay time of facilities and their components to forced entry. Based on NCEL technology, the following is a gross overview of the predicted safety performance of a chimney magazine from an internal explosion.

<u>lafety From Blast</u>: Given an explosion of magnitude W(1bs NEW) inside a chimoey magazine having a volume  $V(ft^2)$  with vertical chimneys having a total vent area,  $A(ft^2)$ , the peak incident blast overpressure, P (psi), at ground range R(ft) from the chimney is:

$$P_{ao} = 290 \left(\frac{A}{v^{2/3}}\right)^{0.401} \left(\frac{M}{v}\right)^{0.0025} \left(\frac{R}{v^{1/3}}\right)^{-1.490} \dots (1)$$

Note that P at any R depends on not just V but also other parameters related to the design of the chimney magazine, i.e., A and V.

Con-ider the specific chimney-magazine design shown in Figure 7. For this particular design, A = 360 ft<sup>2</sup> and V = 97,600 ft<sup>3</sup>. Now, if the safe inhabited building distance, IBD(ft), is defined to be the ground range R(ft) where P = 1.20 psi maximum for W < 100,000 lb NEW and P = 0.90 psi maximum for W > 250,000 lb NEW (current DOD safety criteria for inhabited buildings) then it follows from Equation 1 that the scaled safe inhabited building distance for the chimney magazine is:

For W < 100,000 1b NEW,

$$IBD/W^{1/3} = 23.8 \text{ ft/lb}^{1/3}$$
 (2a)

For W > 250,000 1b NEW,

$$1BD/V^{1/3} \approx 29.3 \text{ ft/lb}^{1/3}$$
 (2b)

For a standard aboveground magazine, DOD safety criterion requires:

For W < 100,000 1b NEW,

$$IBD/W^{1/3} = 40.0 \text{ ft/1b}^{1/3} \tag{3a}$$

For W > 250,000 1b NEW,

$$IBD/W^{1/3} = 50.0 \text{ ft/1b}^{1/3} - (3b)$$

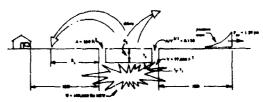


Figure 7. Design parameters for a chimney magazine and the anfeseparation distance from blust and debris.

Comparing Equations (2) and (3), IAD for this particular chimney magazine is 41% less than IBD for a conventional aboveground magazine, regardless of W! More importantly, the encumbered land area is reduced by 65%, regardless of W! Note that the encumbered land area could be reduced even further by reducing the chimney area, A. However, doing so will increase the blast environment inside the box which, in turn, will increase the depth of the soil blanket required for adequate containment of explosion effects. The coat-benefit of further reductions in IBD needs to be studied.

It is important to understand that the vertical chimney is a key feature of the chimney magazine concept. Vertical venting of explosion effects is necessary to achieve a large reduction in the encumbered land area. Morizontal access tunnels - the alternative - would encumber work

land area (and the construction cost would be higher for horizontal access tunnels vice vertical access chimneys).

Safety From Debris: The safe distance from debris is derived from the principle of conservation of energy and the flight dynamics of a missile. Referring to the soil blanket in Figure 7, the scaled total impulse of gas plus shock pressures inside the magazine is  $i_n/M^2$  (psi-macc/lb²). The soil-blanket thickness over the roof is d (ft). The mass density of the soil blanket is  $\gamma_s(1b^2fc^2)$ . The reinforced concrete roof slab has a thickness t (ft) and a mass density  $\gamma_s(1b/ft^3)$ . From the principle of conservation of energy and flight dynamics of a missile, the maximum possible strike range of debris missiles is:

$$R_g \leq \frac{0.334 \left(i_T/V^{1/3}\right)^2 V^{1/3}}{\left(\gamma_g d_g + \gamma_r d_r\right)^2} \tag{4}$$

Equation (4) is approximate but conservative. It neglects energy lost in breaking the missile free from the chimney magazine and energy dissipated by tumbling and air drag during missile flight. Further, it assumes that the debris missile is launched from the magazine at the critical launch angle producing the maximum possible strike range.

Safety From Ground Shock: The soil blanket in a chimney magazine is thicker than in an aboveground magazine. The added soil mass increases the confinement of an internal explosion. This increased confinement increases the ground shock at any distance to a level above that from the same explosion in an aboveground magazine. However, inhabited building, distance from a chimney magazine, IBD = 23.8W to 29.3W , exceeds minimum safe distance requirements of MAVSEA OP-5 by a factor of about two. Thus, ground shock is not expected to present unacceptable risk of damage to inhabited buildings.

The ground shock applied to an adjacent chimney magazine spaced at 1.5V will also be greater. MAYSEA QP-5 requires a minimum separation distance of 1.5V between underground atorage magazines to prevent emplosive communication and 3.5W in sandstone (5W in granite) to prevent damage to stored amounition. But the difference between the shock propagation characteristics in annistone and soil should more then compensate for reduction, in the separation distance from 3.5W to 1.5W for chimney magazines. Thus, ground shock is not expected to cause sympathetic detonation between chimney magazines or damage to storage in an adjacent magazine. Should this prediction be incorrect, the "whiskey bottle" concept can easily be deployed to dissipate ground shock energy to safe levels.

<u>Safety Criteria</u>: Operational requirements are expected to dictate the value of A, V and W for the chimney magazine. In this case, the value of land, cost of soil fill, cost of excavation and the elevation of the water table will dictate the most cost-effective thickness of the soil blanket over

the storage box. However, a cost-benefit analysis is expected to abov the soil-blanket thickness should be such that the maximum possible strike range of debris, R, never exceeds the safe inhabited building distance for blast.

$$R_e \leq IBD$$
 (5)

Combining Equations (2b), (4) and (5), preliminary design criterion for soil blanket thickness required for safety against both blast and debris ( $R_u \leq 1BD$ ) is:

$$d_{n} = \frac{0.1195 \left(i_{T}/W^{1/3}\right) W^{1/6} - \gamma_{T}t_{T}}{\gamma_{n}}$$
 (6)

Solution of Equation (6) has led MCEL to the limits of existing explosion effects technology large uncertainting exist in today's technology for predicting in/W for the range of parameters characteristic of a chimney magazine. Prediction error in the component of in/W resulting from internal gas pressures is believed to be small. But prediction error in the scaled appulse resulting from shock pressures, the other component of is believed to be large. The large uncerin/W", is believed to be targe. The targe uncer-tainty in the shock impulse applied to the roof alab stems primarily from lack of knowledge about close-in effects of a large charge density  $(W/V = 3.1 lb NEW/ft^3)$  and a thin pancake-shaped charge (representing 300,000 pounds NEW of bombs on pallets stacked two-high and uniformly spaced over the entire floor area). Further, large uncertainties exist on the extent and effects of the crater on the maximum debris range. Data from field tests planned for FY84 should reduce these uncertainties. For the interim, NCEL believes it has bracketed the value for a chimney magazine where W = 300,000 lbs NEW, y = 150, t = 1.25 and y = 120. Based on computer analysis, extrapolation of test data and engineering judgment,

$$10 < d_{\parallel} \leq 20 \text{ ft} \tag{7}$$

#### COST-REWEFIT

The cost-benefit of a depot of chimney magazines depends upon the increase in construction costs relative to the value of all benefits derived. One added cost is the extra soil fill and/or excavation required for a chimney magazine. One benefit is the value of land freed from large safety arcs. A gross estimate of this cost-benefit and description other benefits follows.

MCON Cost: The structural cost (\$/ft²) for a chimney magazine is estimated to be about the same as for a conventional, box-shaped, reinforced concrete, missile storage magazine (aboveground magazine). The quantity of reinforced concrete in the chimney magazine is about 39% greater than in an aboveground magazine having the same floor area. This increase stems primarily from the two chimneys, the greater ceiling height, and a thicker roof slab (because of the higher dead load from the deeper soil cover — even though the blast loads from an adjacent magazine will be less).

But other cost components will be less. The structural and mechanical costs of the doors in the chimney magazine should be less because the total area of openings is less (two doors at 28 x 6.5 feet vice two doors at 28 x 12 feet in an aboveground magazine), the clear span of the door is less, and the applied blast load from explosions in adjacent magazines is less. Further, the chimmey magazine requires to blast hardened headwall and doors to protect contents from explosions in adjacent magazines, no reinforced concrete pilasters to support the door from being blown-in, no headwall extensions to support the soil berm, no elevated platform forward of the headwall for transferring cargo and no complicated electrical trolley system to open doors. The designer need only be instructed to provide a water-tight, reinforced-concrete box with two chimneys that safely supports a prescribed depth of soil cover. Knowledge of blast resistant design is not required.

One measure of the cost-benefit is the dif-ference between the HCON costs of a chimney magazine and an aboveground magazine, divided by the total acres of land unencumbered by use of the chimney magazine. This ratio (\$/scre) is the price the Navy is paying to unencumber land by using chimney-magazines. This cost-benefit ratio is shown in Figure 8 as a function of depot size, depth of excavation, and thickness of soil blanket (10 and 20 feet). The curves assume a depot with a

square array of magazines.

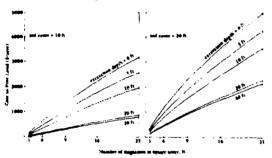


Figure 8. Cost benefit of chimney magazines relative to above ground box

Figure 8 assumes the aboveground magazines are spaced at  $1.25 \text{W}^{1/3}$  side-to-side and  $6.0 \text{W}^{1/3}$  frontto-back, and are covered with 2 feet of soil cover. Encumbered land includes the depot area and all land within the confluence of 50 ft/lb13 measured from the skin of any magazine.

The chimney magazines are spaced at 1.5W<sup>1/3</sup> side-to-side and front-to-back. The depth of soil cover over the chimney magazines for the left and right set of curves (Figure 8) is 10 and

20 feet, respectively.

Unit costs are based on a survey of cost data for Southern California. Both depots are based on the structure costing 150 \$/ft2 floor area, fill 4 \$/yd3 and excavation 3 \$/yd3. Aboveground magazines are assumed to require no excavation and ao fill under their elevated floor and loading platform.

The curves illustrate major savings would be realized at most Navy installations, based on the

"cost of freed land." For example, a deput of 9 chimney magazines with 10 feet of soil cover (vice 9 aboveground magazines) frees Navy land for other uses at an effective cost of between 310 and 1,350 \$/acre, depending on the depth of excavation allowed by the water table. In other terms, the NCON cost of the aine-magazine depot would increase by 5 to 20% based on an MCON cost of 150\$/ft2 for an aboveground depot. Actually, the effective cost is such less than this because all the benefits are not included - and many of these are significant. In any case, Figure 7 shows that the chamney magazipe offers a very cost-effective scheme "purchase" land.

Total Benefit: Other benefits of a chimney magazine, in addition to a major reduction in encumbered land area, are the following: Major increase in level of physical security, increase in survivability, reduction in plutonium (for special wear pens) that could escape to atmosphere, increase in environmental control, greater concealment, less logistics burden (the haul distance is reduced 41% and one piece of equipment does all the work), standardization of design, a solution for depots in Europe (where 69% of the floor area of existing magazines cannot be utilized because explosives safety arcs would encumber inhabited buildings), and a scheme to increase the buildable land area at Navy bases by using unbuildable land as the source of fill for the depot. Regarding physical security, a chimney-magazine depot designed to store 300,000 pounds NEW per magazine offers secure storage for special wespons. Given an inadvertent explosion, the chimney magazine offers almost complete containment because of the low NEW associated with special weapons. Given a mix of conventional and special weapons stored in a chimney-magazine depot, the "shell game" applies - no one knows which magazines (and which Navy Activity) have the special weapons. Further, the labor cost for special security forces is such lower.

#### FUTURE WORK

The chimney magazine is only a concept, but work is underway to refine its cost-benefit and verify its predicted performance, given an explosion equivalent to 300,000 lb NEW in small-scale structures. In view of the anticipated resistance to any changes from the traditional concept for ammo storage, the authors welcome any opinions regarding the utility of the chimney-magazine concept for tomorrows' ammo depots.

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#### SWEDISH DESIGN MANUAL FOR PROTECTIVE STRUCTURES

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#### ABSTRACT

The design of Swedish military hardened concrete structures is based on different manuals among those RSFA publ Bk 25. This publication gives design values for three different classes of structures A-C where e g different degrees of deformations are accepted. The paper describes the design procedures, according to the manual, with respect to fragment penetration.

#### BACKGROUND

During the early seventies the Swedish manual for the design of concrete structures exposed to non-nuclear weapons effects was revised by the Royal Swedish Fortifications Administration (RSFA). The revision which was outlined by Dr Håkan Sundquist, at that time by the RSFA, resulted in RSFA Publ nr 25 in 1973. This manual has been updated in 1977, /1/.

#### CLASSES OF STRUCTURES

An elastic design of structures exposed to weapons effects will often result in conservative and ureconomical solutions. While some structures have to be intact after being subjected to blast and fragments other might sustain different degrees of damages withour their primary function of protection being violated.

For this reason hardened structures are organized in classes  $A_{\rm b}$  B and 0 according to /1/.

Class C is for structures to give survival to people in it accepting damages to the structure itself and to installations in it. Spalling from fragments is accepted on every 3rd square meter of exposed walls and a small risk of penetration is accepted.

Clase B structures may have permanent deflections not greater than 3% of the span. Spalling may occur on every 10th square meter and the risk of penetration is reduced compared to Class C structures.

Class A structures are to fulfill requirements for Class B structures and are also to be secure for gasoverpressure after exposure to blast and fragments. This often leads to an elastic design.

The requirements for the different classes of structures are put together in Table 1.

CLASS OF STRUCTURE	PERMANENT DEFLECTION	RISK OF SPALLING (FROM FRAGMENTS)	RISK OF PENETRATION (FROM FRAGMENTS)
A	100	0.1 = 2	MINOR
В	≤ 37 OF SPAN	0.1 m <sup>-2</sup>	HINOR
С	YES	0,3 m <sup>-2</sup>	SMALL

Table i

#### PENETRATION

The manual is based on the fragmentation concept given by Nott & Linfott in /2/. According to this reference the number of fragments with a mass greater than mo is given by

greater than 
$$m_0$$
 is given by
$$N (m_0) = \frac{m_0}{2K^2} = \frac{\sqrt{m_0}}{K}$$

where  $\mathbf{m}_{C}$  is the mass of the case and K a constant depending on the geometry and the fragmentation of the  $b\not\equiv ab$  .

This gives the fragment density,  $\boldsymbol{Q}$  , on a wall at a distance R from the bomb

$$Q(m_0, R) = \frac{C}{2 \pi R^2} \cdot N(m_0)$$

C a distributing factor to be 1 with a uniform distribution of fragments in all directions. In /1/ C is taken equal to 2 giving credit to the increased density of fragments perpendicular to the axis of the projectile for a vertical wall and a vertical projectile.

The maximum fragment mass for a certain fragment density can then be calculated with bombweight and bomb geometry given for d'fierent distances. This is illustrated in Table 2 for a 500 kg GP homb.

FRAGMENT DENSITY		DISTANCE (m)			
(m <sup>-2</sup> )	5	10	15	20	
			(		
0.01	0.89	0.65	0.52	0.44	
0.1	0.51	0.33	0.24	0.19	
0.3	0.36	0.22	0.15	0.11	

Table 2. Haximum fragment mass (kg) at different distances from a 500 kg GP bomb and for different fragment densities.

The wall thickness, d, has been calculated according to  $d = 2.7 \cdot 10^{-4} \cdot \sqrt[4]{m_0}$ 

where w is the velocity of a fragment at the wall. Table 3 gives d for Class B structues (9 = 0.3) for different bombs.

BONB		DISTANCE			
		5 m	10 m	15 m	20 🗭
1000	kg		0.50	0.45	0.40
500	kg	0.45	0.40	0.35	0.30
250	kg	0.40	C. 32	0.30	0.25
100	kg	0.30	6.25	0.20	0.20

Table 3. Wall thickness (m) for Class B structures with GP bombs at different distances.

By this method the minimum thickness of a structural element can be determined. Additional requirements e g from bending and shear actions of course might make greater thickness necessary.

#### CONCLUSIONS

The concept adopted in RSFA publ Bk 25 for classification of structures has proved to be very useful. The method for calculating minimum thickness of concrete elements with respect to fragments and penetration has shown to be a versatile instrument for design engineers.

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# DESIGN OF UNDERGROUNT THELTERS INCLUDING SOIL-STRUCTURE INTERICTION EFFECTS

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#### ABSTRACT

Soil-structure interaction significantly affects the loads acting on buried shelters subjected to nearby explosions. Recent research has improved our understanding of this complex phenomenon and led to a new design method for buried shelters. This method recognizes the coupling between dynamic response of a buried structure and the loading exerted on it by the neighboring soil. It is simple to use, inexpensive and sufficiently accurate for most underground shelter designs,

#### DYNAMIC SOIL-STRUCTURE INTERACTION

Dynamic soil-structure interaction involves very complex wave mechanics. The process is a coupled phenomenon, i.e., the motion and deformation of the structure depends on the loading acting on it, and the loading, in turn, is affected by the structural motion and deformation. This is illustrated in Fig. 1. A buried slab is impinged by a one-dimensional stress wave propagating in soil. Since the soil is assumed elastic, the free-field stress wave propagates unattenuated until it encounters the slab (dashed line in the figure). If the slab is assumed fixed, the pressure loading on

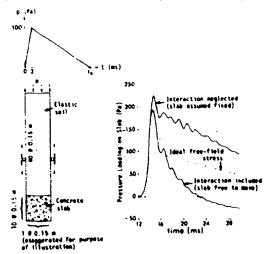


Fig. 1. Beneficial effect of dynamic soilstructure interaction in reducing loading on buried structures, onedimensional illustration.

the slab is equal to the incident plus the reflected soil-stress waves, or twice the free-field stress. This is the assumption used in most prevalent shelter designs. In reality, the slab moves as a result of the soil loading, and this leads to significant reduction in the loading, as Fig. 1 indicates.

#### INTERACTION ALGORITHM

While the beneficial effect of soil-structure interaction is well-known, it has not been integrated in the structural design process because of the complex nature of the interaction phenomenon, and the lack of an efficient design procedure which includes this effect. Recent research at Weidlinger Associates with the aid of analytical and numerical methods indicates that, for impulsive loading of shallow-buried shelters, the interaction is governed mainly by the velocity of the structure relative to the velocity of the free-field soil particles. The loading is considered impulsive when the effective duration of the free-field ground shock pulse is comparable to the fundamental period of the major deformation mode of the structural element of interest. A shelter is shallow-buried when the depth-of-burial i; of the order of the span of the structural element of interest. Under these conditions, the generalized plane-wave interaction algorithm

$$\sigma_{\text{int}} = \sigma_{\text{ff}} + \rho c \left( v_{\text{ff}} - \dot{x} \right) \tag{1}$$

(oint denotes the interaction loading, off the free-field stress, x the velocity of structure, vff the free-field particle velocity and pc the soil impedance) provides a good approximation to the actual interaction loading. This algorithm leads to a new design method for underground buried shelters which is simple to implement and provides a better and more consistent estimate of the effect of dynamic soil-structure interaction at little additional expense.

#### DERIVATION OF DESIGN PROCEDURE

Consider the design of the roof slab of a buried rectangular shelter against a top threat (Fig. 2). Suppose the design is pursued using the beam equation

$$\mu \frac{\partial^2 x}{\partial t^2} - E I \frac{\partial^4 x}{\partial s^4} = \sigma_{int}$$
 (2)

where  $\mu$  is the mass density per unit length, EI the bending rigidity, x the lateral deflection of the beam, and  $\sigma_{int}$  is the interaction loading exerted

by the soil on the roof. Substituting Eq. (1) for  $\sigma_{\text{int}}$  gives

$$u\frac{\partial^{2}x}{\partial \xi^{2}} + cc\frac{\partial x}{\partial \xi} - EI\frac{\partial^{4}x}{\partial \xi^{4}} = c_{ff} + ocv_{ff}$$
 (3)

Note Eq. (3) is a beam equation similar to Eq. (2), with a loading function which depends only on the free-field environment. Hence, the design procedure can be divided into two uncoupled parts: definition of the free-field environment, and the design of the beam subjected to an equivalent (free-field) loading. The effect of dynamic soilstructure interaction is included explicitly in the beam model in the form of viscous damping.

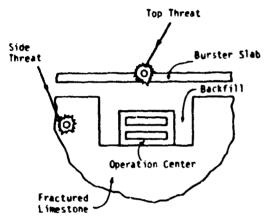


Fig. 2. Buried shelter subjected to top and side munition attacks.

It is easy to generalize the above derivation. The equation of motion of a shelter can be represented as

$$L\{x\} = \sigma_{int} \tag{4}$$

where x is the structure displacement and L(+) the differential operator. The use of the simplified soil-structure interaction algorithm in the equation of motion gives

$$L\{x\} = o_{gg} + pc (v_{gg} - x)$$

Or

$$L(x) + \rho c \dot{x} = \sigma_{ff} + \rho c v_{ff}$$
 (5)

Again, the forcing function is a function of the free-field environment only. The structural system on the lefthand side of the equation is the original system i  $\{x\}$  with the added damping term pcx to represent the interaction effects.

A new design procedure is developed based on Eq. (5). This is illustrated in Fig. 3. The structural model (numerical or otherwise) is modified to include the interaction damping. The equivalent free-field loading is then applied to the bare structure. Other than these changes, the design procedure is identical to the prevalent procedure for unburied shelters.

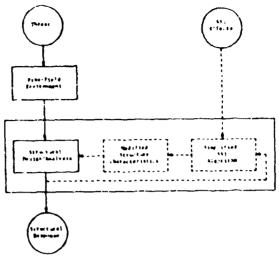


Fig. 3. New design procedure with simplified spil-structure interaction (SSI) algorithm.

#### **VERIFICATION**

The accuracy of the new design procedure depends on the walidity of Eq. (1). Based on extensive comparisons of the design results with detailed finite element soil-structure analysis results, the new design method is found to yield good approximations under the conditions specified for Eq. (1), i.e., impulsive loadings and shallow-buried shelters. Fig. 4 is representative of the results obtained. The interaction loadings on the midspan of the roof of a buried shelter are obtained using the direct coupled finite element method and the new design method with a beam model to represent the roof. They are compared in the figure. The comparison is excellent despite the fact that the free-field loading is non-planar. This is because the intensity of the soil stress decays rapidly with distance from the source and at midspan where the loading is most severe, the interaction is approximately planar. This is often the case for conventional weapons.

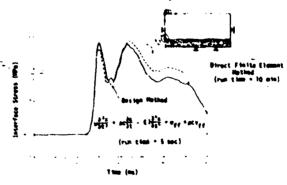


Fig. 4. Comparison of interface stress at midspan of an 18 m roof, direct finite element calculation versus design method.

The same design procedure has been used for inelastic soil-structure systems; the impedance coefficient, pc, is represented as a function of the soil stress at the interface in accordance with the inelastic stress/strain relationship of the soil. Tensile interaction loading should also be limited to reflect the limited tensile strength of the soil-structure interface. The algorithm as outlined has been incorporated in computer programs commonly used in structural design, e.g., SAP and STRUM.

#### **CONCLUSION**

Soil-structure interaction effects are propagation in the model. The cost and complexity of an explicit wave analysis often deter a designer from including the beneficial effect of soil-structure interaction on the design. A new design procedure based on an approximate interaction algorithm has been developed, which greatly simplifies the supporting analysis. It allows the designer to obtain an excellent estimate of the peak interaction loads on the structure with little additional cost or labor compared to a conventional procedure. It is also compatible with any reasonable structural model the designer chooses to evaluate candidate designs.

# 001739

# GAS PRESSURE LOADS FROM EXPLOSIONS WITHIN VENTED AND UNVENTED STRUCTURES

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#### ABSTRACT

Gas pressures from explosions within enclosures, as opposed to shock loads, can be the dominant loads causing structural failure. This paper reviews test results and prediction methods for gas pressures for many types of internal explosions including high explosives, high explosives plus combustibles, gas mixtures and dust suspensions,

#### INTRODUCTION AND BACKGROUND

For explosions in enclosures involving high explosives, solid propellants, high explosive with combustible materials in contact, or combustible mist, dust, or gaseous explosive mixtures, the long-duration gas pressures caused by confinement of the products of the explosions can be the dominant loads causing structural failure. These quasi-static pressures are determined by the total heat energy in the explosive and/or combustible source, the volume of the enclosure, the vent area and vent panel configuration, the mass per unit area of vent covers, and the initial ambient conditions within the enclosure.

Previous analytic work, similitude analysis, and numerous experiments have addressed several aspects of this problem and provided a good data base for more general predictions. Ref. 1 collates much of this information for gas pressure parameters for bare high explosive detonations in enclosures with open vents, while Ref. 2 includes analytic predictions of these parameters for similar explosions with covered vents with various masses per unit area. Maximum pressures for gas and dust combustible mixtures initiated in unvented and vented enclosures are reported in Ref. 3 and 4. Host recently, frat data for gas pressures in a scaled structure from high explosives surrounded by combustible liquids and solids are reported in Ref. 5.

Tests of solid propellants burned in vanted structures are reported in Ref. 6 and 7. Ref. 6 also includes derivation of a scale modeling law for pressures for this situation. Scale modeling of dust and has explosions in enclosures is inherent in work in L.f. 3, while a more thorough law for vented dust explosions appears in Ref. 8.

In this paper, the authors will review the literature and present methods for predicting internal gas pressure loads under the following conditions: 1) bare high explosive detonations in

structures with open vents, 2) high explosive plus combustible explosions in closed structures, and 3) gas and dust explosions in closed and vented structures. The predictions will be based on graphs and/or numeric fits to scaled parameters from appropriate similitude analyses.

#### GAS PRESSURES FOR INTERNAL HE EXPLOSIONS

The loading from an explosive charge detonated within a structure consists of two phases. The initial phase consists of several high amplitude, short duration, reflected pressure shocks. This phase of the loading is very geometry dependent, with the highest loads generally occurring on the surfaces nearest the charge. On each reflection, the shock strength is attenuated until at some point the internal pressure has settled to a slowly decaying level. This is the quasi-static pressure loading phase. This phase is characterized by essentially uniform pressures throughout the structure at any point in time. The rate of quasi-static pressure decay is a function of the vent area. structure volume and the nature of the explosive source.

A typical pressure trace obtained during an internal explosion in a vented structure is shown in Figure 1. Traditionally (Ref. 9), the peak quasi-static pressure is established by fitting a smooth line through the data beginning at the end of the pressure trace and extending back towards time zero, the time of charge ignition. This line is shown in Figure 1 as a solid line. The peak  $P_{\rm qg}$  is then taken as the intersection of the fitted line and a vertical line at time zero (shown as a dotted line in the figure). This point is labeled A in Figure 1. For a vented structure, a more appropriate technique has been auggested (Ref. 1, 5). This method is applied by drawing a ramp increase in pressure extending from time zero, which follows the base of the pressure shocks. This 'ine is shown as a dashed line in Figure 1. The intersection of the ramp pressure increase with the line . fitted through the pressure decay is the peak quasi-static pressure. This point is labeled B in the figure. For explosions inside sealed enclosures, points A and B will have nearly the same ordinates, whereas for explosions with increasing went areas, the difference in ordinates between points A and B

in Ref. 1, a wery complete analysis of gas pressures from internal explosion data was presented. The authors performed a similitude analysis to

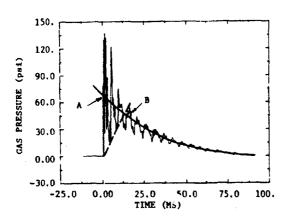


Figure 1. Typical Pressure Record from an Internal Explosion in a Vented Structure

determine the functional form of the quasi-static pressure, as a function of the physical parameters pertaining to the problem of an internal explosion inside a vented structure. Based on this analysis, the following equation was derived:

## Peak Quasi-Static Pressure:

$$\log \hat{P}_{QS} = 0.30759 + 0.51815 \log (W/V) - 0.150534 [\log (W/V)]^2 + 0.31892 [\log (W/V)]^3 + 0.10434 [\log (W/V)]^4 - 0.14138 [\log (W/V)]^5 + -0.019206 [\log (W/V)]^6 + 0.021486 [\log (W/V)]^7$$

Equation (1) was the result of curve fits to 177 experiments. Figure 2 presents the curve fit together with the measured data. One approximation was made in the analysis of the test data. The explosive energy contained in any high explosive is directly proportional to the explosive mass. As it turns out, the charge energy-to-explosive mass ratio for most explosives is nearly the same. For convenience, the analysis performed in Ref. 1 utilized the charge mass, rather than the charge energy.

Based on the results of the analysis of the internal explosion data, the authors of Ref. 1 found that the peak quasi-static pressure was independent of the vent area, but dependent on the charge weight-to-structure volume ratio.

# GAS PRESSURES FOR HE PLUS COMBUSTIBLES

Recently (Ref. 5), a series of experiments was conducted in which various combustible materials were placed in varying degrees of contact with high explosive charges. The object of the tests was to determine whether the combustible materials could contribute to the quasi-static pressure development within a scaled enclosure. The combustible materials investigated in this effort are listed in Table 1. In every case, the high explosive was 0.592 lb of PRX-9404. All of these experiments were conducted in the same enclosure, so the only parameter not held constant was the combustible

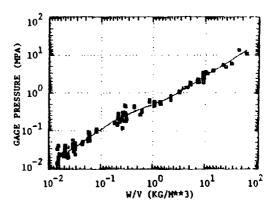


Figure 2. Peak Quasi-Static Pressure as a Function of the Charge Weight to Enclosure Volume

	Table 1. Combustible Materials and Configurations Tested*				
Series	Material	Configuration			
1	Polycarbonate	A 67.6 gm polycarbonate disk was attached to the end of a cylindrical (t/d=1) charge.			
2	Polycarbonate and Aluminum	A 135 gm aluminum casing surrounding the side of a cylindrical charge. A polycarbonate disk covered one end of the charge.			
3	50/50 Mix of DMF and Acetone	A spherical charge was sub- merged in 5 oz of the fluid.			
4	Polycarbonate	Two polycarbonate hemi- spheres were attached to opposite poles of the charge. The total poly- carbonate weight was 48.25 gm.			
5	50/50 MLx of DMF and Acetone	Five 1 or containers of the fluid were equally spaced on a circle 36 in. in diameter around the charge.			
6	Low density polyethylene	Polyethylene beads suspended in an epoxy base, and formed into a four-sided box, centered on the charge. The weight of the box was 273 gm.			
*The explosive was 0.992 lb of PBX-9404. Test Series 1 and 2 utilized cylindrical charges, while the remaining tests utilized spherical charges.					

The charge location was the same in all experiments.

configuration. Note that the Pqs for a bare 0.992
1b PBX-9404 charge is 48.7 psi. In every case, the addition of combustible materials in near contact

with the HE charge increased the quasi-static pres-

sure, in some cases dramatically.

The degree of quasi-static pressure enhancement produced by a combustible is related to the heat energy content of the material. This is shown in Figure 3 where the excess Pqs (the Pqs produced by the combustible plus the HE, less the Pqs produced by the HE alone.) is plotted as a function of the combustible energy content. The combustible energy content is defined as the mass of combustible energy content is defined as the mass of combustible times the appropriate heat of combustion from Table 2. As seen in Figure 3, the enhancement in the quasi-static massure increases uniformly with increasing combustible energy, as long as the combustible is in intimate contact with the charge. The only point not following the general trend of the data corresponds to the series of tests in which the combustible fluid was dispersed a large distance from the charge.

The phenomenon of quasi-static pressure enhancement produced when combustible materials are placed near HE sources has only been recently discovered. The effect has been observed for a variety of combustible materials, but no variations in charge to combustible mass, charge type, structure volume, or degree of venting have been tested. The implications of the data accumulated so far are that quasi-static loading calculations should include estimates of contributions from the burning of combustible materials whenever such materials are expected to be in intimate contact with HE sources.

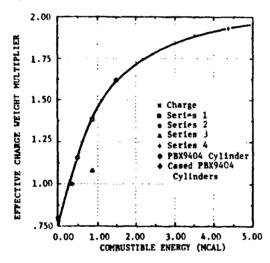


Figure 3. Excess Quasi-Static Pressure (psi)

# GAS AND DUST EXPLOSIONS IN CLOSED AND VENTED CHAMBERS

Hany accidental explosions occurring in industry involve the ignition within enclosures of combustible mixtures of gases with air, or suspensions of combustible dusts in air. Such mixtures ignited in the open do not cause blast waves or significant pressure waves, but instead generate only transient fireballs as flame fronts progress at rather low rates (meters per second) through the combustible mixtures.

But, when the combustible mixtures are ignited inside a sealed or vented enclosure, the confinement provided by the enclosure can allow significant pressure rises which can disrupt the structure. A typical pressure history for such an explosion within an unvented enclosure is shown in Figure 4.

The maximum rate of pressure rise  $\frac{\dot{u}p}{dt}$ , and the maximum pressure  $P_m$  are determined by the reactivity of the particular material, the fuel-air ratio, the amount of material, and the volume of the enclosure. When the enclosure has a vent area, covered by a vent designed to open at pressure  $P_u$ , the pressure-time history is modified as shown in Figure 5. The amplitudes and times of the maxima  $P_1$  and  $P_2$  are functions of the gas flow dynamics through the vent, and either  $P_1$  or  $P_2$  may be the maximum pressure.

Table 2. Heat of Combustion for the Various Combustible Test Materials

Material	Heat of Combustion (cal/gm)
PBX-9404	2369
Polycarbonate	7223
Acetone	7363
DMF	6259
Polyethylene	9400
Aluminum	7400

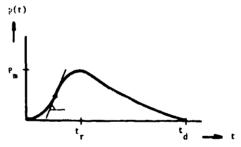


Figure 4. Schematic Overpressure-Time History in Confined Gas or Dust Explosions (Ref. 10)

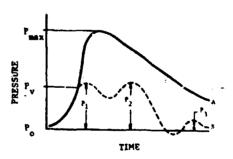


Figure 5. A Representation of a Pressure-Time History of an Unvented (Curve A) and Vented (Curve B) Deflagrative Explosion (Ref. 13)

The voluminous data and analyses in the literature (see Ref. 10) on the characteristics of these pressure histories can be condensed and presented in compact form based on similitude analyses

(Ref. 6 and 7). Bradley and Micheson (Ref. 11 and 12) present scaled upper limit curves for gas explosions in vented vessels. These are reproduced here as Figures 6 and 7. In these figures, the dimensionaless terms are

$$\vec{A} = \frac{AK_d}{A_g}$$
 ,  $\vec{S}_o = \frac{U}{a_o}$  ,  $\vec{P}_m = P_m/c$  (2)

where A is vent area,  $A_{\rm S}$  internal surface area,  $K_{\rm d}$  discharge coefficient (\*0.6), U is gas velocity ahead of a flame front,  $a_{\rm O}$  is ambient sound speed,  $P_{\rm m}$  is maximum pressure and  $p_{\rm O}$  is ambient pressure.

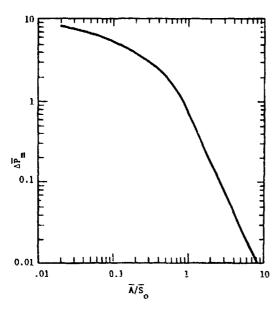


Figure 6. Safe Recommendations for Uncovered Vent Areas. Gaseous Explosions (Ref. 12)

For dust explosions, maximum pressures are also a function of the dust reactivity, and a scaled vent area. Figure 8 shows scaled plots of  $\overline{P}_m$  for dusts of increasing reactivity, STI through ST3. Here  $\overline{A}$  is defined somewhat differently, as

$$\overline{A}_{v} = (A/v^{2/3}) \tag{3}$$

where V is volume of the enclosure.

In either gas or dust explosions of this nature, the dimensionless maximum pressure rate for a given combustible mixture is

$$\frac{\tau}{P} = (P V^{1/3}/a_0 P_0)$$
 (4)

This scaling is consistent with Bartknecht's "cubercot law." (Ref. 3)

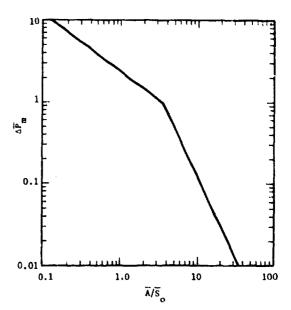


Figure 7. Safe Recommendations for Covered Vent Areas, Gaseous Explosions (Ref. 12)

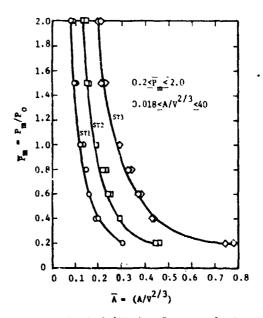


Figure 8. Scaled Maximum Pressures for Dust Explosions Versus Scaled Vent Area Ratic (Ref. 10)

It is also clear from Ref. 11 and 12 that the maximum pressures accainable within enclosures for gaseous explosions are remarkably constant for all

combustible gases, varying from about 8 atmospheres for natural gas to only 10.25 atmospheres for acetylene.

## CLOSURE

Even though the material on gas pressures for explosions within enclosures which is summarized in this paper shows an extensive experimental and analysis base, there are still a number of significant data gaps which limit our ability to predict these pressures. These include at least:

- Lack of data on pressures generated by HE-combustible combinations
- Lack of data and validated analytic methods for effects of vent cover parameters for HE explosions
- Lack of data for mixtures of combustible gases and dusts
- Lack of data for dust explosions in real configurations, such as grain elevator gallenes.
- lack of data for effects of vent cover parameters for gas and dust explosions.

Not all of these gaps are important to weapons effects analysts, but all are quite important in the explosives safety community.

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STRUCTURAL RESPONSE OF RC-MEMBERS IN CASE OF IMPULSIVE LOADING Failure Analysis in Bending and Shear

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## ABSTRACT

Beams and one-way slabs subjected to impulsive leading are analyzed with aid of a numerical model, which is kept as simple as possible, and which is sufficient powerful to simulate real beam response. Therefor the beam is schematized as a system of rigid sections and elasto-plastic hinges which can account for hysteresis. The equations which hold for this discrete model are presented. They are solved by use of the systems dynamics language Dunamo.

In case of the application of an impulsive loading to a simply supported beam a very typical pattern of 'traveiling' plastic hinges may occur, different to what is known from static loads.

to what is known from static loads. In case of the application of an amplosive load to a beam with clamped ends, the similarity with static results is much greater. In the example of the flat roof of a traffic tunnel however, the shear failure criterion is extremely dominant, yielding strongly reduced allowable peak values of the explosive loads.

# PROBLEM STATEMENT

Increasingly more we need to examine the strength of rc-structures in case of dynamic loading. The load can be a local impact or more general some kind of distributed impulsive loading. This paper reports on a study which has been originated by questions whether or not to transport explosive liquified gasses through traffic tunnels of rectangular cross-section. Especially the roof slab of the tunnel is studied, and for this purpose a strip of 1 m width has been examined. So the study regards a beam type structure, and in fact the results have been more general purpose than strictly spoken was needed for traffic tunnels.

The understanding of the structural behaviour of rc-structures is increasing rapidly. Research of last ten years has yielded a fastly growing number of tools to analyse total structures or members. At least as far as static loading is concerned which increases monotonically, Progress is also being made for repeated static loading and cycling static loading, in which the problem of stress reversal has to be dealt with. A less covered area is the dynamic response of rc-structures. In this case all mentioned aspects of static loading play their role, but above that the equations of motions have to be integrated in the

time domain. Authors feel that the present-day finite element programs have proven to be powerful in the field of nonlinear static analysis of elastic structures, and even for the nonlinear dynamic analysis of metal structures. Experience and expertise for the nonlinear dynamic analysis of rc-structures is still poor however. A number of problems arise simultaneously in that case, for instance the correct choise of failure criteria, a satisfactory formulation of the softening problem after cracking, and particularly the problem of numerically stable processes for the integration in time of the equations of motion in case of such specific nonlinear phenomena. Therefore the nowaday finite element programs may give rise to problems which are connected with the mathematical algorithms, rather than relevant for the structural problem which is being studied. Authors expect much futural improvement in this field, but for the time being a well-proven approach is preferred which yields immediately insight in the structural respons, whithout being troubled to much with numerical problems.

The adopted simple beam model is used to gain improved understanding of elasto-plastic flexural structural response in the case of a beam subjected to impulsive distributed loading. Two special cases are discussed in some detail. The first one is the response of a simply supported beam, and the second one is the behaviour of a clamped beam. The simply supported beam is of interest to explain experimental results. In experiments it has been found that beams which have been subjected to distributed load of short duration may not get plastic hinges or fail in the mid of the span, but at positions more close to the supports. The clamped beam more or less reflects the situation of a strip which can be taken from a roof slab in a traffic tunnel. Now questions arise which reinforcement is optimal, and which capacity a beam has for severe combinations of dynamic moments and shear forces.

# DESCRIPTION OF THE BEAM MODEL

To achieve the simple beam model which has been aimed at, two decisions were made. The first one regards the mechanical modelling of the beam. We used the well-known discrete model in which a continuous beam in bending is replaced by a set of rigid sections and flexible rotational hinges at the nodes where sections join together, fig. I. The mass of the sections is lumped at the nodes,

and likewise the time-dependent distributed load on the sections. The length of the sections is y. The flexible hinges are modelled as elasto-plastic springs.

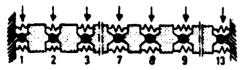


Fig. 1 Example of a clamped continuous beam in bending which has been modelled by a system of rigid sections and flexible springs.

The second decision regards the integration of the equations of motion. In stead of once more writing a specific computer code, we profited by the available systems dynamics package Dynamo. This language facilitates the stepwise integration in time of any set of first-order linear or nonlinear differential equations. Though Dynamo has been developed at MIT for socio-economical time-dependent problems, it proved to be possible to use it in the engineering field as well. Be it, that structural plastic irreversal deformation had to be interpreted as some type of an economical delay!

The two decisions, to use the discrete beam model and to make use of Dynamo, are in fact just one decision. Due to the discrete model we are able to use Dynamo, because of the fact that this model description can yield first-order differential equations in a simple way.

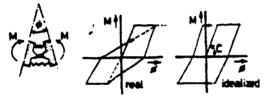


Fig. 2 Elasto-plastic characteristics of the Maxible appliques

We have to become more precise on the characteristics of the flexible springs in the discrete model. We will discuss the situation of a prismatic beam in which different percentages of top- and bottom-reinforcement can be used. First of all, it is important to describe hysteresis in an appropriate way, because of its strong damping action. In literature a 4-1 diagram is used as is shown in the mid part of figure 2. This diagram is derived from the relation between the moment N and the curvature  $\kappa_*$  for in fact  $\ell$  is equal  $y\kappa$  , and the diagram holds for situations as occur with earthquakes during which cycling of the loads may last a number of seconds. In our case of a puls load or explosive loading one may expect that we do not run through the diagram a couple of times, but just one time due to strong plastic damping. After that the vibration will vanish elastically. This made us decide to use the more schematized M-# diagram which is shown in the right-hand part of figure 2. The stiffness c of the elastic branch is easily derived from the bending stiffness EI which holds for a rc-beam. We consider a part of the beam of length y and require that the discrete model yiekis

an equal angle # as will occur in the real continuous beam when the same moment M is applied. From this we derive M=CØ in which C=EI/u. The horizontal plateaus in the N-Ø diagram are determined by the plastic bending moment which follows from the applied percentage of reinforcement. Also the ultimate value of # and the inelastic ro-

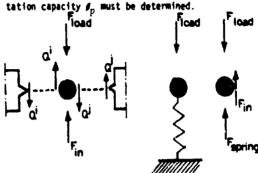


Fig. 3 Each node of the discrete model our be considered as a mass-spring-system.

Each node of the discrete model can be considered as a mass-spring-system (fig. 3). Three forces act on each node:  $F_{load}$  which is the external loading consisting of a static part  $F_{dtat}$  and a dynamic part  $F_{dyn}$ ,  $F_{i:t}$  due to the inertia of the mass, and  $F_{apring}$  which is the difference of the shear forces on both sides of a node. We introduce a for the acceleration of a node, v for the velocity of a node, w for the displacement of a node and m for the lumped mass. The integration process is as follows. Starting from known values u(t), v(t) and a(t) at the beginning of a time step  $\Delta t$ , we calculate for each node using Euler's method the values  $\omega(t+\Delta t)$  and  $v(t+\Delta t)$  at the end of the time step by  $\omega(t+\Delta t)=\upsilon(t^{1}+\Delta t,\upsilon(t))$   $\Delta v(t+\Delta t)=\upsilon(t)+\Delta t,\upsilon(t)$  (1)

From the new values of we successively calculate for each node j  $\beta i = (-u^i + 2u^j - u^k)/y + M^i = c^i \beta^i$ 

$$\mathbf{p}_{1}^{2}(-u^{2}+2u^{2}-u^{2})/y + \mathbf{p}_{1}^{2}=c^{2}\mathbf{p}_{1}^{2}$$
 (2)

$$Q^i = (M^i - M^i)/y$$
  $\bigwedge Q^j = (M^j - M^k)/y$  (3)

$$F_{sprin,j}^{j} = i^{j} - i \lambda^{j} \tag{4}$$

Herewith a new value a(t+At) is calculated for each node:  $a(t+\Delta t)=(F_{1,oad}-F_{apring})/m$  which facilitates to use (i) again for the next time step. The scheme has to be adapted sligthly for a node at a clamped edge; equation (2) has a modified form in that case. The scheme implies that we have known values at t=o for the quantities w, v and a, which are derived from the boundary conditions at that time. If the bending mofrom (2) exceeds the value of the plastic moment, this value is taken. Also specific attention is given to unloading processes and the re-lated hysteresis, which will not be discussed here.

## ULTIMATE STRENGTH AND ROTATION CAPACITY

The characteristics of the N-# as were adopted in figure 2 presuppose that the beam has been designed in such a way that no failure in shear occurs before the plastic moment has been reached. It has also been adopted that the rotation capacity is not influenced by the presence of a shear force.

In general this is true because of the applied stirrup reinforcement in beams.

However, another situation applies for slabs, because of the absence of stirrups. So the strip which can be selected from a tunnel roof—though being treated as a beam—may behave in another way. In that case a cross-section can fail for combinations of a bending moment and a shear force in which the bending moment is smaller than the plastic moment. Brittle failure will be the case then. Or, in case that the plastic moment can be reached, the rotation capacity may be reduced. So, limitations on strength and deformation:

As for the strength, shear failure strongly depends on the relation of M and Qh, in which h is the effective depth of the beam. For different values of N/Qh different failure mechanisms will occur, each with its particular strength. In case of static loads one normally differentiates in the following modes:

-a shear crack grows from an existing bending crack
(flexural shear failure);

-a diagonal crack in the web occurs due to tension stresses (tension shear failure).

We need not consider cases with diagonal crushing which only might occur when stirrups are applied. Neither we need view the case of failure in the anchoring zone of the main reinforcement.

For static loads Rafla has proposed an appropriate formula to estimate the flexural shear strength of a beam. He derived the formula in a statistical way from a large number of tests. We adapted the 5% lower boundary of all results for application in dynamically loaded structures, yielding

in dynamically loaded structures, yielding  $\tau_{u,dyn} = \alpha_{dyn} \, f_{cc}^2 \, \omega_o^3 \, h^{-\frac{1}{4}} \, (N/m^2)$  (6) Herein  $\tau_{u,dyn}$  is the nominal shear stress which has to be multiplied by the effective depth and the width of the slab strip to find the shear force,  $f_{cc}$  is the cube crushing strength,  $\omega_c$  is the percentage of reinforcement, and h is the effective depth of the slab strip. The value  $\alpha_{dyn}$  depends on the relation of A and A:

 $\alpha_{din}=0.9$ -0.03 M/Qh (7) The Other failure criterion for tension shear more likely will occur for values of the bending moment which are smaller than the flexural cracking moment at which bending cracks come into being. For such small moments (thus small values of M/Qh) no flexural shear failure mechanism can develop. The tension shear failure will occur if the principle tension stresses in the mid-plane of the strip exceed the dynamic tensile strength  $f_{ot,dyn}$ . Therefore, a good approximation of  $\tau_{u}$  at tension shear failure reads

The determination of the flexural cracking moment can not be done very accurate however, because we use average dynamic properties of the concrete. Therefore we preferred to make the transition dependent on the value of M/Qh. Rather arbitrarily we decided to use the tension shear failure criterion for values M/Qh < 0.75 and the flexural shear failure criterion for values of M/Qh > 1.75. In between of these values a gradual transition has been proposed from the one failure criterion to the other.

Figure 4 shows the result of this decision for a specific slab strip.

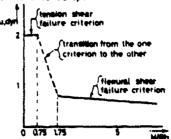


Fig. 4 The failure envelope for the shear strength in case of a particular concrete quality, percentage of reinforcement, and depth of the slab.

We now concentrate on the deformation capacity. In the case that no stirrups are applied, the shear force must be partly transferred by the compression zone of a cross-section. When a plastic moment starts to occur, the compression zone will become smaller for increasing curvature. However, in this plastic case almost all shear force has to be transferred by the compression zone, due to large crack widths. At certain deformation the compression zone will have become so small that failure (by shear) occurs. Hence the rotation capacity  $\ell_{pQ}$ , which is left over when a shear force is transferred, is smaller than the rotation capacity ≠p which is at disposal when no shear force occurs. The reduction depends on the ratio of the present shear force qand the ultimate shear force  $Q_n$  which anyhow can be transferred by the concrete. This latter value, holding before large shear cracks come into being, can be calculated with aid of the Rafla-formula (6) which has been adapted for dynamic conditions. Figure 5 represents the adopted dependency of the rotation capacity on the shear force.

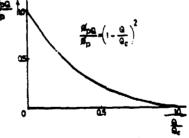


Fig. 5 The rotation capacity podecreases for an increasing shear force 2.

# APPLICATION TO A SIMPLY SUPPORTED BEAM

In this application it is assumed that the beam can not fail in shear. So it has been adopted that sufficient shear reinforcement is applied. The span is 15000 mm, the depth of the beam is 1200 mm and the width is 1000 m. Top and bottom reinforcement percentage is 0.3%. The concrete quality is B22,5 and steel quality is FEB 400. For the concrete material we introduced

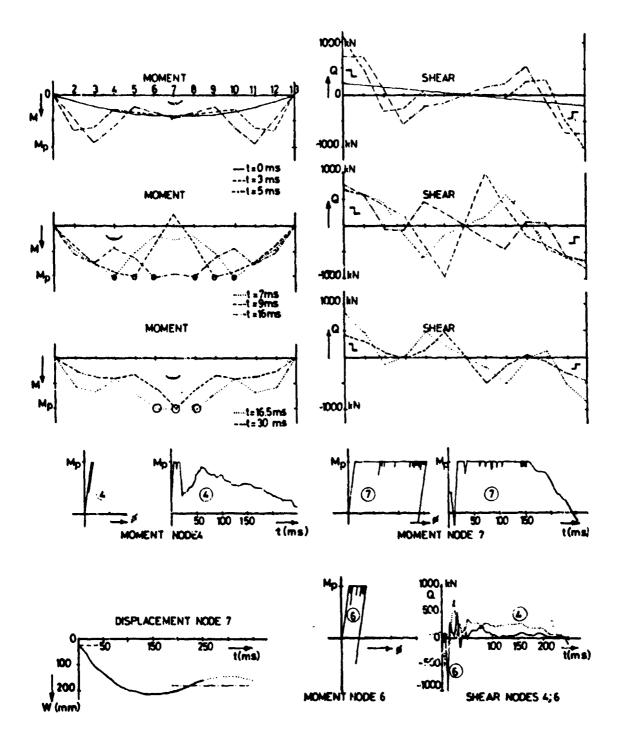


Fig. 6 Typical re rense plots for an impulsive distributed load on a simply supported beam.

 $\epsilon_{smeshing}$  = 1.78%;  $E_s$  = 86.7  $10^{8}N$  mm $^{2}$ ;  $\epsilon_{so}$  =00.8 N/mm $^{2}$  and for the steel strength  $\epsilon_{so}$  = 480 N/mm $^{2}$ ;  $\epsilon_{so}$  = 60.8 N/m $^{2}$ 

 $T_{\rm of}=880~N/mm^2$ . The span is modelled with 12 discrete sections, which implies that the length of a section is to be compared with the depth of the beam. The load in each node consists of an impuls  $\delta$  kNa at r=0. The lumped mass  $\pi$  in each node is 3600 kg, so the impulsive load yields an initial value of the velocity  $\nu$  = 6000:3600  $\approx$  1.7 m/sec. One could interpret the analysis as an experiment in which the beam falls freely from some height until it hits at time t=0 the two supports.

Results of the analysis are given in fig. 6. Herein the distribution along the span of the beam is shown for the moment M and the shear force Q for different times c. At small values of time c the beam hardly feels that the supports have been hit. Only at the end strong curvatures and thus moments occur. Also big shear forces appear in these parts of the beam. When time goes on the bending moment diagram changes of shape and the displacement diagram developes in an expected way. One can easily see that a wave of shear force travels through the beam. In total agreement with the development of the moment diagrams one also can note from the plots in fig. 6 that plastic hinges come into being at some distance from the supports and then "travel" to the mid of the span. Also some plots in the time domain of a displacement w, a moment N, and a shear force Q are shown in fig. 6. The alternating character is demonstrated once more in these plots. In the same figure it is shown for a couple of hinges which path has been run through in the elasto-plastic . diagram. From this it appears that the beam after some time vibrates in an elastic way over its whole length.

In conclusion, it is felt that the runs made, have shown that the elasto-plastic discrete model is able to represent the main characteristics of the benaviour of a beam for impulsive loading in a satisfactory way. Though the real behaviour in detail may be slightly different, the global behaviour is modelled in an appropriate way. Available experimental data are confirmed by the results of the model. This holds at least in a qualitative sense, but also the quantitative information sounds profound.

## APPLICATION TO BEAM WITH CLAMPED ENDS

We now consider a beam with clamped ends, which is representative for the response of the roof of a tunnel in which an explosion occurs. Fig. 7 shows the cross-section of a typical traffic tunnel as it is applied in the western part of the Netherlands. The pressure-time plot of the shock wave due to an explosion in a tunnel is shown in fig. 3. Herein  $P_{\max}$  is the peak value of the pressure, which is expressed in bars (1 bar = 100 kN/m²), and  $t_J$  is the duration of the phase at which the pressure is present (positive phase). After  $t=t_d$  suction may set in (negative phase). The pressure-time plot appears to be described accurately by the formula  $p(t)=p_{\max}\left(1-\frac{t}{t_d}\right)e^{-\frac{t}{2}}$ 

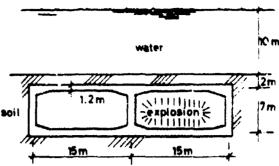


Fig. 7 Exemple of a typical traffic tun of in the Netherlands.

The coefficient  $\alpha$  is a shape factor of the shock wave. In a tunnel its value can be set to 4. Dependent on the type of liquified gas, the peak value can be of the order of 10 bar up to 25 or 30 bar for the worst type. Tests in small scale tunnels show a positive phase duration  $t_J$  of about 50 ms. It is not quite clear which model law applies to determine the value of  $t_J$  in a real tunnel, but it should be expected that  $t_J$  may increase. Therefore we have examined the influence of three values of  $t_J$ , namely 50 ms, 100 ms and 150 ms.

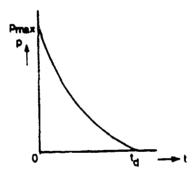


Fig. 8 Pressure-time plot for an explosion in a tunnal.

Firstly we made an analysis of a beam with clamped ends, assuming that no failure due to shear will occur. The span is 15 m and the slab thickness 1.2 m. We started with a high percentage of main reinforcement at the top and bottom of the slab of 2.5%. This yields the following capacity of the beam, which is determined by exhausting the ultimate rotation capacity.

	$t_{.j}$	p <sub>max</sub> (rot.sup.)		
พ. = 2,5%	50 ms 100 ms	60 bar 34 bar		
w <sub>g</sub> = 2,5%	150 ms	36 hac		

We see that  $P_{max}$  reduces for increasing Q. Though not exactly true, one can roughly say that the product of  $P_{max}$  and  $E_{Q}$  is constant. Or said in another way, that the total impuls is more of less determining. In all three analyses plastic hinges come into being at the clamped ends and at mid span, in the same way as is found for a static load (so

different from what we experienced for a simply surnorted beam).

The analyses may produce insight and understanding, they have however no practical value because of too high shear forces. In slabs without shear reinforcement the allowable nominal shear stress  $\tau_{ii}$  is of the order 1 N/mm², and we have found values between 8 and 8 N/mm². So the real applicable  $F_{max}$  will be much lower.

To demonstrate the influence of the shear failure criterion, a new series of analyses have been then executed, for reinforcement percentages 0.7, 1.1, 1.8 and 2.5. Here we only present the results for  $\omega_{c} \approx 1.14$ .

	t <sub>d</sub>	r (rot.cap.)	p (shear failure)
	50 me	26 bar	7 bar
ω <sub>o</sub> ≈ 1.1 <b>5</b>	100 ma 150 ma	14 bir 2 bir	4.5 bar 3 bar

We see that the application of the shear failure criterion strongly reduces the allowable  $P_{\max}$ , as compared with the situation in which one just checks the exceedence of the rotation capacity. Roughly  $P_{\max}$  decreases to one third. And for higher percentages of the reinforcement the reduction is still more severe.

An inspection of the results learns that even no plastic moments occur anymore, because of early shear failure. Whilst the moment diagram along the span is similar to the distribution which is found for a static load, the distribution of the shear force is quite different. Failure does occur rather close to the mid of the span in node 5 or 6. The analysis for  $t_{eff}=150~ms$  has also been carried out for the other percentages of reinforcement which have been mentioned before. Supprisingly enough, the allowable  $F_{max}$  in all cases was 3 bar. It is true, the allowable shear force does increase for an increasing percentage of reinforcement, but apparently also the acting shear force can become bigger, due to an increasing bending stiffness.

# CONCLUSIONS A discrete beam model consisting of rigid sections

and flexible hinges is a powerful tool for better understanding of the elasto-plastic response of reinforced concrete beams which are subjected to impulsive loading. This is achieved thank to the fact that the governing equations of such a model are easily solved by the use of an available systems dynamics language Dynamo. For simply supported beams impulsive load yields a moment distribution and shear forces which strongly differ from the ones which hold for simular static loads. Provided that no shear failure occurs, plastic moments can occur at positions along the span at some distant of the mid. The plastic hinges thereupon travel to the mid of the

In case of the examined beam with clamped ends (simulating a tunnel roof) the results are different. The moment distribution is more similar to the one which appears for static loads, but the shear force still differs, be it less than in a simply supported beam.

From this one can conclude that an idealization of a tunnel roof to a simple-mass-spring-system is accurate for the displacement and moments, but may be misleading for the ralue of the maximum shear force and the position along the span of its occurance.

If no stirrups are applied a shear failure criterion has to be introduced, which strongly reduces the allowable load, and in most cases no plastic hinges will come into being anymore.

## **ACKNOWLEDGEMENT**

The study has been executed as part of the fulfillment of the requirements for the degree of civil engineer at Delft University of Technology. Much thank is indebted to prof.Dr.-Ing. H.W. Reinhardt and his co-worker dr.ir. J. Walraven for their advice and support in deriving an appropriate dynamic shear failure criterion. We also highly appreciate the readiness of mrs. Joke Oud for typewriting the paper.

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## ABSTRACT

Numerous methods for predicting structure response to airblast caused by HE explosions were developed during the last twenty years. The rigor, complexity and sophistication of the methods are known to cover a wide spectrum. Some the less complex but widely accepted methods are examined, assessed, and discussed relative to their degree of conservatism. To support their assessment, the authors critically examined the structural design parameters used in the predictive methods.

## BACKGROUND

The Corps of Engineers, as the Army's designer and builder of military facilities, maintains a continuing interest in the technology of the effects of weapons and explosions on structures. The earliest design techniques were related to projectile penetration and then came the great interest in effects of nuclear weapons including blast, shock, and other associated effects. During World War II, there developed relatively crude procedures usually "rule of thumb" methods to estimate effects of accidents at the many munitions and explosive manufacturing facilities which we rapidly erected during the period 1941-1945. In the last 30 years, problems of design of structures to resist the effects of HE explosions have been addressed on a more rational basis.

Two of the most recent non-nuclear documents reflecting the Corps' efforts are TM 5-1300, Structures to Resist the Effects of Accidental Explosions (1969), and HNDM-1110-1-2, Suppressive Shield Design and Analysis Handbook (1977). These documents, among other Corps references, provide our basic guidance. However, the Corps design activities have not been restricted to these two documents.

Many methods conforming to other authorities are also used. Some of the most frequently used methods are: (a) ASCE Manual 42, (2) Air Force Manual 500-8, (3) Defense Civil Preparedness Agency (now Federal Emergency Management Agency) Protective Construction, and other texts usually associated with structural dynamics.

### APPROACH

Our experience with HE explosions typically centers on three basic types of airblast loading:
(1) pressure-time (triangular), (2) impulsive, and (3) the combination of impulsive and pressure-time loading as shown in Figure 1.

Accordingly, each of these loads was separately included in the analysis. It was considered important that these loads be treated separately in view of possible variances in conservatism in the methods under the different loading.

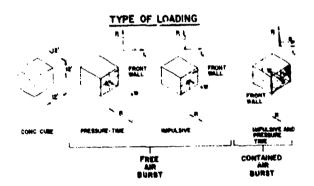
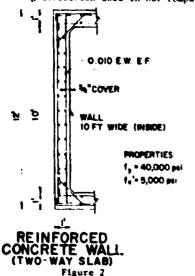


Figure 1

Since reinforced concrete prevails among protective structures, we selected a reinforced concrete wall as the structural element for our assessment of the methods. After determining the loads and the structural elements, we proceeded with our analysis.

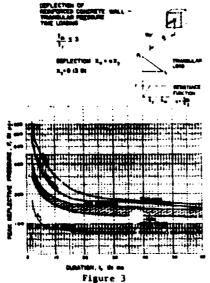
## S"RUCTURAL CAPABILITY

The two-way reinforced concrete wall in Figure 2 was designed for flexure as indicated by the main reinforcement. No shear calculations were made. For our purpose, it is assumed that shear may be adequately provided. Flexural strength and other structural properties are tabulated in Table 1. These were used as the basis for calculating deflection used in our comparison.



## TRIANGULAR LOAD

A family of curves is plotted for the reinforced concrete wall to predict the wall deflection resulting from a triangular pressure-time load. Each curve represents a specific ductility ratio, u, hence deflection. See Figure 3.



By locating the coordinate  $(t_a, P_a)$ , the ductility ratio may be estimated by interpolating between the u's. For a ductility ratio, u=3, two curves are shown; one for TM 5-1300 method and the other for the suppressive shield method. All the other methods previously discussed are distributed in the shaded band. A close observation indicates that the TM 5-1300 curve is more conservative than the others, because being on the lower side of the shaded band it has more restrictions on the limits of pressure and duration for the given ductility ratio, u=3. The Suppressive Shield Handbook curve is less restrictive, allowing 25 percent higher pressures for the same duration and ductility ratio.

## IMPULSIVE LOAD

When the wall is impulse sensitive from close-in explosions, deflections are also predictable. Based on the curves in Figure 4, the TM 5-1300 curve on the lower side of the shaded band is conservative because being on the lower side of the shaded band, it has more restrictions on the limits of the impulse for a given deflection. The Suppressive Shield Handbook curve is less restrictive allowing 20 percent higher impulse for the same deflection. Curves for the other methods are distributed within the shaded band.

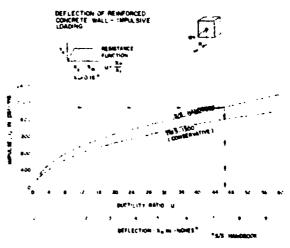


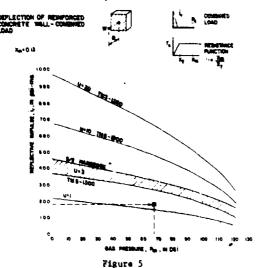
Figure 4

## COMBINED LOAD

The combined load consists of an impulsive load followed by a prolonged gas pressure. A family of curves is shown in Figure 5 and each curve represents a specific ductility ratio, u.

\_.1

After locating the coordinate  $(P_{gg}, i_T)$ , the ductility ratio, u, can be estimated by interpolation between u's. The ductility ratio curve u = 3 for TM 5-1300 and the Suppressive Shield Handbook methods are shown. It can be demonstrated again that the TM 5-1300 curve on the lower side of the shaded band is more conservative than the Suppressive Shield Jandbook curve on the upper side of the band. TM 5-1300 is more restrictive on the limits of impulse and gas pressure for a given ductility ratio, u = 3. The Suppressive Shield curve is less restrictive allowing 15 percent impulse or 30 percent higher gas pressure for the same ductility ratio.



EXAMPLE

The charge weight, distance and load parameters are shown in Figure 6. These numbers provide an appreciation for the magnitude involved and an understanding of the curves. Applying load parameters on the well, deflections are estimated by using Figures 3, 4, and 5. These examples are not restricted to any one method, i.e., both TM 5-1300 and Suppressive Shield methods are used below.

For the 8000f TWT at 100 feet, where  $P_T=90$  psi and  $t_T=16$  ms, select from Figure 3 (TM 5-1300 curve) approximate u=1.4 or  $X_m=uX_m=1.4$  x 0.13 in. = 0.2 in. For the 512 lb. TWT at 10 feet, where  $t_T=1920$  psi-ms, select from Figure 4 (Suppressive Shield curve)  $X_m=7.4$  in.

For the contained 8 lb. TMT at 5 feet, where  $i_T=184$  pairs and  $P_{\rm SM}=64$  pai, select from Figure 5 (TM 5-1300 curve) approximate  $v\approx 1.3$  or  $X_{\rm M}=1.3\times 0.13=0.2$  in. These deflections compare well with the calculated  $X_{\rm M}$  in Table 1.

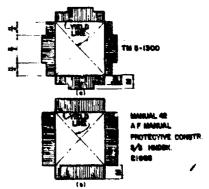
## **ASSUMPTIONS**

Four factors influence the differences in the predictive methods; yield line assumption, moment of inertia, modulus of elasticity and stiffness. As expected, the variance within these factors are the basis for the differences in the predicted deflection.

## YIELD LINE

In most two-way siab designs, the effective unit resisting moments are assumed to be uniformly distributed on the yield lines. In TM 5-1300, the effective resitting moment at the corners are reduced by one third. This reduction cruses the TM 5-1300 method to be significantly conservative. See Figure 7.

# TWO-WAY SLAB YIELD LINE DISTRIBUTION OF MOMENTS



MOVENT OF INERTIA

The formulae for moments of inertia are shown in Figure 8.

# FORMULAS FOR MOMENT OF INTERTIA

10 = \$1, #\$(4), mat\_(17), AM 8-1200

Le" MA (8.5p+0.0 43) (APPROXL) 8/2 HODEK.

I d = Mg + PER, E) + MANAGELIANE COMBLE

# Pigure 8

Appreciable difference in  $I_A$  appears when the slab thickness is small. This is attributable to the use of "T" in TM 5-1300 and "d" in the other methods.

## MODULUS OF ELASTICITY

When 3600 psi concrete is specified, the  $E_{\rm C}$  in Figure 9 is the same for all methods. See intersection of curves.

# MODULUS OF ELASTICITY (CONCRETE)

E. W" 33 11

TM 5-1300 A F MANUAL

1/5 HHOEK 81863

Ec= 1000 fc'

MANUAL 42 PROTECTIVE CONSTR

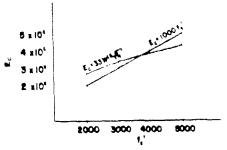


Figure 9

Since most concrete strength for sirblast loads exceed 4000 psi, a difference in modulus of elasticity is unavoidable.

## STIFFNESS

With the exception of protective construction and Manual 42, the equivalent stiffnesses are used. From our preceding example, the stiffness by Manual 42 is significantly higher as shown below:

Others

$$k = 605 \left( \frac{E_c I_a}{4} \right)$$

## DISCUSSION

The assessment on the relative conservations are based on airblast data from TM 5-1300 curves. The more recent data in the Suppressive Shield Handbook is significantly different. The difference in impulse is seen in Figure 10. TM 5-1300 is as much as 60 percent higher.

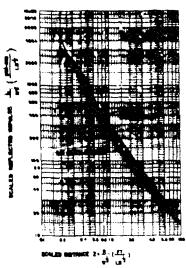


Figure 10

If the latest data were separately used in the Suppressive Shield Handbook method, the differences in conservation between methods would be more pronounced.

We have examined the extremes in the predictive methods. Of the dix methods, no comparison was mad- as to how how each related to the other in convervation. The best basis for judgement is the comparison of deflections in Table 1.

In our examination of the methods, we assumed all methods are conservetive. This assumption is supported by testing of full scale and model structures in previous Army programs associated with the development of Corps of Engineers manuals for hurdened structures. Accordingly, we consider the assumption to be reasonable.

# CONCLUSION

In assessing the relative conservation of the methods, the focus was on both ends of the spectrum; the most conservative on one end and the lesst conservative on the other. We identified the TH 5-1300 method as the most conservative and the Suppressive Shield Handbook method as the lesst conservative.

Based on the maximum deflection,  $X_{\mathbf{m}}$ , in Table 1, the order of conservation beginning with most conservative to least conservative follows:

- 1. TH 5-1300
- 2. menual 42
- 3. Protective Construction
- 4. Air Force Manual
- 5. Bigge
- 6. Suppressive Shield Handbook

In general, because of similarity, it would be more appropriate to group conservation as follows: TN 5-1300 by itself as the most conservative; Hanual 42, Protective Construction, and the Air Force Hanual in the intermediate group; and Biggs and the Suppressive Shield Handbook as the least conservative group.

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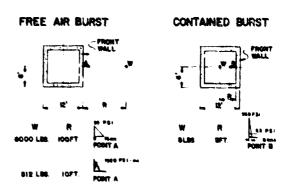


Figure 6

Table 1

# COMPARISON

ME THOSE	TM8-1800	-	AF YANGAL	CONSTR	<b>ÇĞ 10000</b> €.	21000
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BY AMERICA	47,900	- 199	140	147	150	47,990
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xa-10	0.5	01	0.5	01	0.4	•1
TH-HI BRALIE	<b>3</b> )	10.0		10-8	73	13
u= m	44			0.2	B2	



# RESPONSE OF A LINEAR STRUCTURE TO AN EXPONENTIAL PRESSURE PULSE

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#### ARSTRACT

Explosion dynamics is concerned with the response of structures to intense pressure loadings from shock waves. Most interactions that occur in practice are very complex, so that scaling laws are often employed to reduce the number of independent variables to a lesser number of dimensionless variables. Very often, this makes the results easier to interpret. Here, new similarity variables are introduced which lead to flatter response curves than those obtained previously.

The energy transfer from the fluid to the structure is treated by computation of the fluid work done on the structure and the increase in electic energy stored in the structure,

## INTRODUCTION

Underwater explosions produce a complex fluid-structure interaction at the surface of a submerged body. The pressure at the body surface is dependent not only on the shape of the body, but is modified by the induced motion of the body surface. In general, because of the non-linear behavior of the water, the surface pressure at may particular time will depend on the previous history of the motion of the surface.

This means the free field pressure from the amplosion is modified not only by shock reflection from the body, but also by the particular path taken by the surface as it moves under the pressure loading.

This paper is concerned with the special case where the pressure medification from body surface metion is neglegible. This usually occurs in the case of emplosions in sir. The structure is assumed to be a linear spring-mass system subjected to an exponential pressure load. A development of model laws for this case appears in Reference 1. In this paper, now similarity variables are introduced which give further insight into the dynamics of explosion induced motions of structures.

## DYNAMICS OF A LINEAR STRUCTURE

The single degree of freedom spring-mass system is governed by the differential equation

$$\Psi + \omega^2 x = P \exp(-t/T) \tag{1}.$$

make x is the displacement, x is the acceleration, P is the peak pressure, t is the time, and T is the characteristic time of the pressure pulse. The natural frequency w is given by

$$w = \sqrt{k/N}$$
 (2).

where k is the linear spring constant, and M is the mass of the body surface per unit area. The boundary conditions at t = 0 are

$$t = 0: \frac{1}{2} = x = 0$$
 (3).

where x is the velocity of the surface. The solution of this system is oscillatory with the maximum displacement on resched at time to.

It is convenient to introduce the following dimensionless variables:

$$\overline{x} = k x/P \tag{4}.$$

In terms of these new variables, the solution to Equation (1) that satisfies the boundary conditions given by Equation (3) is

$$\overline{x} = \frac{\overline{\tau^2}}{1 + \overline{\tau^2}} \left[ \exp(-\overline{t}/\overline{t}) - \cos \overline{t} + (\sin \overline{t})/\overline{t} \right]$$
 (9).

The relationship between the exponential pressure loading and the resultant displacement of the atructure is shown in Figure 1.

### TIME OF MAXIMUM DISPLACEMENT

As indicated in Figure 1-A, the maximum displacement we of the structure is reached at time to when the velocity vanishes. Differentiation of Equation (9) leads to the expression

The time or maximum displacement is shown in Figure 2 as a function of the characteristic loading time.

## MAXIFREM DISPLACEMENT BASED ON PEAK PRESSURE

Substitution of tm into Equation (9) leads to the distribution of the maximum displacement function methods in Figure 3. The maximum displacement function, as leftined by Equation (5), is the ratio of maximum displacement to the displacement that would occur under a static load equal to the peak pressure. A disadventage of this definition is that it is independent of the shape of the pressure pulse. This produces the large variation in m shown in the Figure 3. A flatter response curve can be obtained by basing the displacement on an average pressure exerted on the well, rather than the peak pressure

# AVERAGE PRESSURE AND APPLIED IMPULSE

The definition of total impulse is

$$I = \int_{0}^{\infty} p(t) dt$$
 (11).

For the exponential loading used here,

$$P = 1/T$$
 (12).

Secause the total impulse includes the pressure loading applied to the structure after it has reached its maximum displecement, we introduce a new similarity variable, the applied impulse J defined by the sheded region in Figure 1-3. By fixing the upper limit of integration to the time of maximum displacement, the applied impulse is

$$J = \int_{0}^{\infty} p(z) dz \qquad (13).$$

From Figure 1-B, the average pressure, applied up to the time of maximum deflection, is

$$Po = J/to (14).$$

For the exponential loading considered here, Equation (14) becomes

$$Pa = (p T/ta)[1 -exp(-ta/T)]$$
 (15).

## MAXIMUM DISPLACEMENT BASED ON AVERAGE PRESSURE

A new displacement function analogous to Equation (3), but based on the average pressure instead of peak pressure is

A plot of this function, showing the relatively flat response is shown in Pigure 3. A quasistatic load with T = 1000 will produce a maximum deflection that is 1.273 times larger than that produced by a impelsive load with T = .01, if the average pressure Pa is the same for both loadings. In this comparison, the maximum deflection mm is not very sensitive to the shape of the pressure pulse.

#### PRAK AND AVERAGE PRESSURE PURCTIONS

In Reference 1, a peak pressure function was defined as

$$\overline{P} = 2 P/(k m)$$
 (17).

The denominator on the right represents the maximum electic energy stored in the spring. This occurs at the time of maximum displacement. Mere, an average pressure function is introduced in the form

$$Pa^{+} = 2 Pa/(k xm) = 2/mc^{+}$$
 (18).

This function gives the ratio of the average pressure to the average spring force. Plots of these pressure functions appear in Figure 4. The applied pressure function is relatively flat compared to the peak pressure function. This means that, over a wide range of values of the characteristic time of the pressure pulse, the ratio of average pressure to the maximum elastic emergy stored in the structure is almost constant.

# TOTAL AND APPLIED DUPULSE FUNCTIONS

In Reference 1, a impulse function was defined as

$$\tilde{1} = I/(a + ma) = \tilde{2} \tilde{1}/2 = \tilde{1}/ma$$
 (19).

Here, this is replaced by an applied impulse function defined as

As shown in Figure 5, J\* varies from 1.0 for impulsive loads to 1.57? For quesi-static loads.

The pressure function, total impoles function response curve from Equation (19) is shown in Figure 6. The curve is a hyperbola extending to infinity along force and impulse asymptotes. A corresponding applied pressure function, applied impulse function response curve from Equation (20) is gloo shown. The latter curve is a small segment of a hyerbola that gives the combinations of applied pressure and applied impulse that produce the same maximum displacement of the system.

### EMERCY COMMERCIANTION

If viocous dissipation and rediction damping from well motion are neglected, the work does on the structure by the fluid is converted directly into kinetic energy of the atructure and elastic energy stored in the spring. If time is measured from shock impingement with the structure, the work done on the structure by the fluid pressure up to the time of maximum displacement is

$$H = \int_{0}^{t_{0}} x p(t) dt$$
 (31).

Where x is the surface velocity. A work function is defined by the expression

where the denominator is the fluid work dose on the structure by a static load equal to P. With the aid of Equation (21), Equation (22) becomes

$$y = \frac{T[1 + V^2 - 2 \text{ H cos } \overline{tn}]}{2[\sin \overline{tn} - T \cos \overline{tn} + \overline{T} \text{ H}]}$$
 (23).

where

$$H = \exp(-\epsilon \pi/T) \tag{24}$$

The fluid work function is shown in Figure 7. As the pressure loading becomes more impulsive, the work done by the fluid on the structure is a smaller percentage of that produced by a quesi-static load.

At any instent in time, the fluid work is in equilibrium with the elastic energy stored in the spring and the kinetic energy of the mass. This can be expressed as

where the electic energy is

$$x = k x^2/2$$
 (27).

and the kinetic energy is

$$0 + M x^2/2$$
 (28).

Remarion (26) can be written in the form

$$C^* = E/V = 1 - Q/V$$
 (29).

After some menipulation, we obtain

$$u_0 = \frac{\left[ \sin \overline{t} - \overline{T} \cos \overline{t} + h \, \overline{T} \right]^2}{(1 + \overline{t}^2)(1 + h^2 - 2 \, h \, \cos \, \overline{t})} \tag{50}.$$

This function is pletted in Figure 8 for three values of the characteristic time ranging from 0.1 to 1000. These curves correspond to impulsive, dynamic, and quasi-static loads, respectively. Each curve starts at zero time and ranks at the time of maximum deflection when all the fluid work on the structure is stored as elastic energy. For times between these two endpoints, only a fraction of the fluid work done on the structure is stored as elastic energy. The belence, as indicated by Equation (29), is stored as kinetic energy.

As the well starts to move under the intense pressure loading, most of the work done by the fluid goes into kinetic energy. Only a small percentage goes into elestic energy stored in the spring. After the well has reached its maximum velocity, a greater percentage of the work has been converted into elestic energy. When the well finally comes to ro:t at the maximum displacement point, all the fluid work is stored as elestic energy.

#### CONCLUBIONS

The response curves for a linear spring-mass system have been modified by the introduction of new similarity variables. The applied impulse is defined as the impulse received by the atructure up to the time of maximum displacement. Any impulse received after this time does not have any influence on the magnitude of the maximum displacement, and is therefore neglected. An average pressure over this time intevel was also introduced to be used in place of the peak pressure. This was chosen because two different pressure loadings with the same initial peak can have completely different responses because their charactistic times are different.

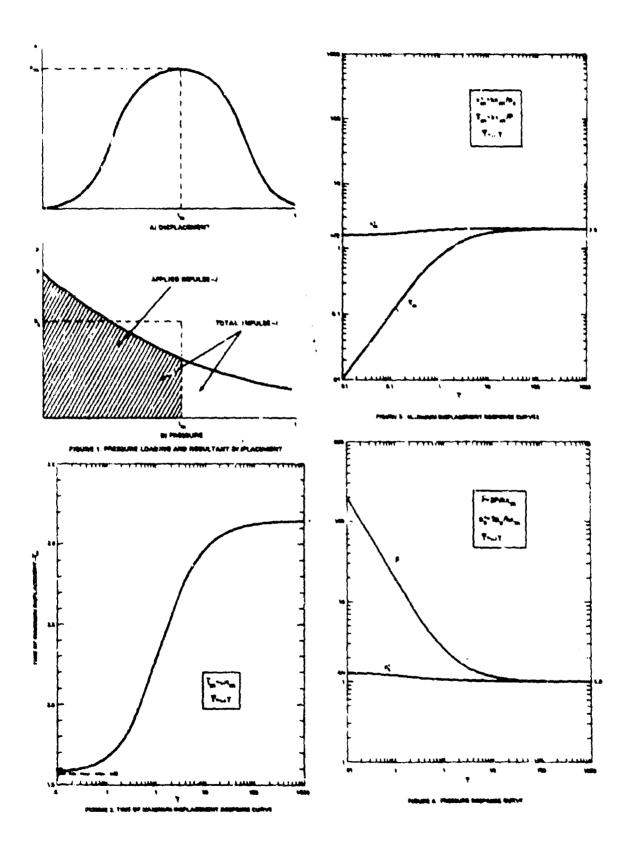
The response curves for the new functions introduced here are fairly flat and do not approach zero or infinity as when the looding is static or very impulsive. A structure that receives the usus applied impulse from two different pressure pulses will receive approximately the same maximum deflection. This cannot be said for two different pulses that have the same total impulse.

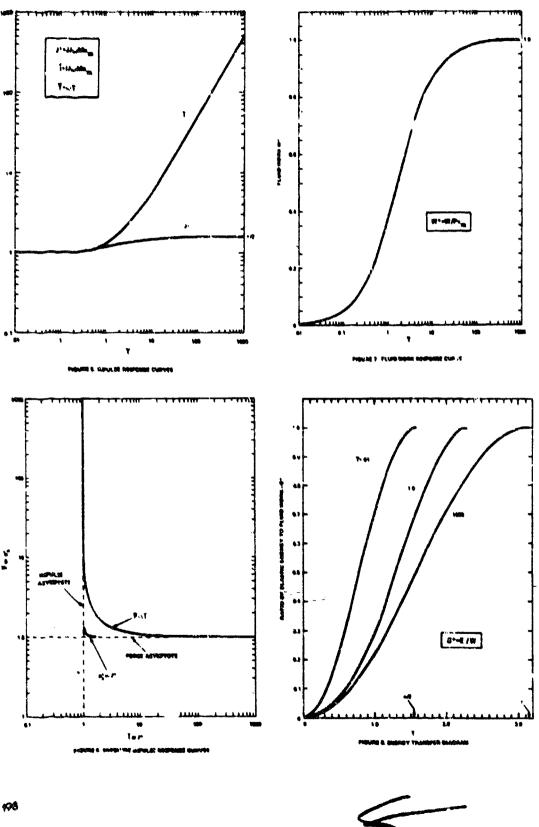
A study of the energy transfer from the fluid to the structure indicates the work don. by the fluid is initially transformed mostly into kinetic energy. Later, after the structure has reached its maximum velocity, a greater percentage of the fluid work is stored as elastic energy in the spring. Mean the structure has reached its maximum displacement, all the fluid work is stored in the spring as elastic energy. Any energy remaining in the pulse after the time of maximum displacement is irrelevent, and is essentially useted, since it cannot have any influence on the maximum displacement.

It is expected that these results will be significantly modified when the pressure loading is changed by redistion desping produced by fluid-structure interaction. Even when the free field pressure is expensential, the setual pressure at the surface of the structure will no longer have that form of docay. This case, which applies to most underwater explosions, will be the subject of a future study.

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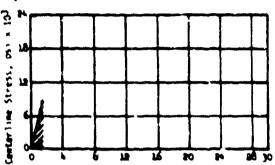
# THE USE OF STEEL FIBER REINFORCED CONCRETE IN FUNTATIONENT AND EXPLOSIVE-RESISTANT STRUCTURES

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# ABSTRUCT

The results of several investigations of steel fiber reinforced concrete (SFRC) under explosive loading are presented. Tests using high explosives were performed by the U.S. Corps of Engineers to compare reinforced concrete slabs using conventional concrete to similar slabs using SFRC. The conventional slabs were completely disintegrated. The slabs containing SFRC retained their integrity even though severely demaged. Similar results were obtained with explosive tests on slabs by Lemrance Livermore Laboratory, impect loading by a pendulum-type impact machine, ballistic impact by small arms fire, impulsive leading on beams and a drop weight impact test. Use of SFRC for blast resistance in structures are listed.



Centerline Deflection, in. x 10-3

# FIGURE 1.

13. Load-Deflection Curve for 3-1/2 x 4-1/2 x 16 in. (89 x 114 x 406 cm) Plain Concrete Geam. Maximum Size Acquerate Used was 3/8 in. (9 cm) (Mef. 1, page 5).

# INTRODUCTION

Probably the most outstanding improvements of stael fiber reinforced concrete over that of plain concrete are in its energy absorption characteristics and its resistance to impact and explosive loading. The advantage is not merely that of greater toughness, but the presence of fibers prevents the total disintegration and shartering of concrete associated with chock loads. With fibers, the crecks cannot extend without stretching and debonding the fibers. As a result, substantial energy inputs are necessary before complete frocture of the material can occur. A measure of the energy absorption properties or toughness of stael fiber reinforced crecipte compered to plain concrete can be seen from the area under the load-deflection curves shown in Figures 1 and 2 [1]. Many tests show that the toughness of stael fiber reinforced concrete is an order of magnitude higher than that of plain concrete [2,3].

With explosive loading, steel fibers reduce the fragment velocity and the fiber reinforced slabs retain their integrity. This unique property of spell and shatter resistance, and the ability to retain the shape and integrity of structural elements and to hold them together can be vital in the design of certain types of structures. Because of these properties, random steel fiber reinforcement is well suited for use in beens or other structural elements subjected to impact.

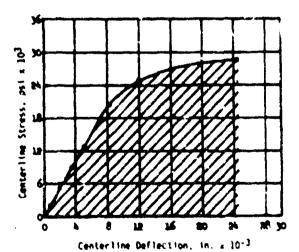


FIGURE 2. Load-Deflection Curve for 2 x 2 x 6 in.
(50 x 50 x 150 mm) Fiber Reinforces Con-

crete Boom. Reinforcement was 1.96% by volume of .017 x 1-1/2 in. (0.43 x 38 mm) Steel Mire. Paximum Size Appregate Used was 3/8 in. (9 mm) (Ref. 1, p. 5).

RESULTS OF EXPLOSIVE LOADING, IMPULSIVE LOADING AND IMPACT TESTING

# Explosive Loading

Tests by Williamson [1] demonstrated that with explosive loading, a shock wave travels through a wall as a compressional wave and is reflected on the opposite face as a tensile wave which then causes spalling and disintegration of concrete. Williamson's tests have shown that while conventionally heavily reinforced slabs disintegrate completely under explosive loading, the inclusion of steel fibers in the concrete reduces the fragment velocity by up to 23 percent. More importantly, it causes the slabs to retain their integrity without producing secondary fragments of sufficient mass and velocity which might cause further damage. Figure 3 shows the effects of a 10 lb. (4.5 kg) charge of HE on a conventionally reinforced concrete slab while Figure 4 shows the effects on a reinforced concrete slat conteining SFRC.



FIGURE 3. The Receives of a 32 x 32 x 4 in.(800 x 800 x 100 mm) Concrete Slab with Conventional Reinforcing After Explosive Testing with 10 lbs (4.5 kg) of HE (Ref. 1, page 12).

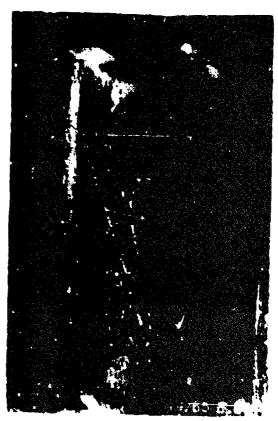


FIGURE 4. This Slab Was Similar to the One in Figure 2 Except That it Contained 1-3/4% by Volume of 0.017 x 1-1/2 in, (0.43 x 35 mm) Steel Fibers (Pef. 1, page 13).

Full scale tests by Lawrence Livermore Laboratory [4] have also demonstrated the effectiveness of steel fibers in reducing the damage from high explosives. Figures 5 and 6 illustrate the effects of 49 lbs (22 kg) of high explosives on 5 ft x 5 ft z 18 in.(1.5 x 1.5 x 0.45 m) thick slabs with Mo. 8 (25 mm dia) Grade 60 reinforcing bars on 6 inch (150 mm) centers, each way, each face. The slab containing fibers used  $0.01n \times 0.022 \times 1$  in. (0.25 x 0.55 x 25 mm) cut sheet fibers at 1.25% by volume in a 7.5 sack, 3/4 in. (19 mm) maximum size aggragete mix designed for 4000 psi (28 MMa) at 28 days. The conventional concrete was similar, using 7 sacks, 3/4 in. (19 mm) aggragete, designed for 4000 psi at 28 days. Actual 28-day compressive strengths were 4300 psi (30 MMa) for the SFRC and 4513 psi (31 MMa) for the plain concrete.



F \* RE 5. Conventional Reinforced Concrete Slab Underside, After Test Shot (Ref. 4, p. 32)

# IP, act and Impulsive Loading

Edgington, et al., [5] used a pendulum-tyre innert machine to evaluate 4 x 4 x 20 in. long (100 x 100 x 500 mm) specimens of steel fiber reinforced mortar and concrete made with different shapes are strengths of steel fibers. Meximum opprepate slies were approximately 3/8 and 3/4 in. (9 and 19 mm). The impact resistance of the steel fiber reinforced concretes increased as the fiber content increased. Of four fiber types tested, a 0. 20 in. (0.5 mm) diameter by 7 in. (50 mm) long, high tensile, crimped fiber proved most beneficial. In reases in impact resistance of more than 400 percent at a fiber content of less than 1-1/4 percent by volume were measured with this fiber. Ritchie and Al-Kuyyali [6] found that steel fibers increased the impact resistance of lightweight concrete by as much as three times.

Swamy [7] has reported improved resistance of steel fiber reinforced slabs subjected to repeated drup hell tests. Failure in these tests was defined as occurring only when a hole was punched through the slab rather than by shattering of the slab into fragments.

The impact test recommended by the ACI in import ACI-544.78-78, "Measurement of Properties of Fiber Reinforced Concrete", uses a 10-1b (4.5 kg) compaction hammer with an 18-in, (460 km) drop to impact a 2-1/2 in. (64 km) thick disc 6 inches (150 km) in diameter. The number of blows to first crack and failure, or ultimati impact resistance, are recorded. Failure occurs when a crack opens enough to allow the sides of the disc to touch the surrounding stoys. The ultimate impact resistance in number of blows is commonly 15 to 40 for plain concrete and ranges from about 40 to as high as 500 or more for 1 to 15 hercent by volume of a deformed or crimied-end wire fiber [8].



FISURE 6. Reinforced SFRC Slab, Underside, After Test Shot (Ref. 4, page 35).

Ballistic impact tests using small arms fire were conducted by Nous and Williamson on SFRC downs and plate specimens [9]. Plate tests showed that i to 4 inch (75 to 100 mm) thick SFRC [1.53 by volume of 0.01 x 0.022 x 1 in. (0.25 x 0.55 x 25 rm) cut showt fibers] resisted penetration from 30 caliber (7.62 mm) machine gun fire and NI6 (7.62 mm) ammunition at 50 yards (4h m) with no spalling of the reverse side, whereas the same thicknesses of plain concrete were either penetrated, cracked through or showed spalling on the reverse side. A 4-1/2 inch-thick (115 mm) SFRC dome resisted all but 50 caliber (12.7 mm) machine gun ball ammunition and a 6 inch-thick (150 mm) dome resisted penetration by 50 caliber ammunition for a limited number of firings. The 50 caliber ammunition penetrated or shattered plain concrete plates 6 to 7 inches (150 to 175 mm) thick with a single impact.

. 1

Romualdi and Ramay conducted impulsive loading tests on concrete beams  $4 \times 6 \times 72$  in. long on a clear span of 63 inches (700 x 150 mm x 1.8 m, 1.6 m span)[10]. Twenty beams were tested, all with tensile reinforcing bars. Half used plain concrete and half used SFRC with 2% by volume of 0.066 in. dia. x 0.5 in. (0.15 x 13 mm) long brass-coated, cold drawn steel wire fibers. Three SFRC beams had no diagonal tension reinforcing (stirrups). All other beams had stirrups. A special spring-loaded apparatus was used to impulsively load the beams at the third points with sufficient force to cause failure. All dynamic tests were performed with an initial total spring load of 14,000 pounds (62,275 newtons).

Typically, the plain beams failed in compression and all load was lost at about 0.025 seconds. The SFRC beams, however, continued to support the load with diminishing oscillations until they stopped at some final residual load. The fiber beams, even though damaged considerably, were able to maintain their structural integrity. The residual loads carried by the fiber beams ranged from 4,900 to 11,900 lbs (21,800 to 53,000 newtons). The residual load carried by the plain reinforced beams was zero [10].

The three SFRC beams without web reinforcing were tested statically and failed in flexure, rather than in shear. An average shear stress of 444 psi (3 MPa) was calculated from the formula  $\tau=P/bd$  from a maximum shear of 8,250 lbs (36,700 newtons). Also, in three of the SFRC statically tested beams, the tensile reinforcing bar broke, an unusual occurrence in concrete beams. This was because the SFRC concrete in compression at the top of the beam, maintained its integrity instead of crushing, providing a fulcrum around which the reinforcing steel could be continuously strained to a higner level.

## The report concluded that:

- Impulsive loading of the magnitude used in these tests does not cause sudden failure in the fiber reinforced beams such as the sudden failure observed in plain beams.
- The internal resisting moment is significantly greater in the fiber beam and, therefore, permits the ber in absorb more energy. The beams retain metric structural integrity and carry considerable residual load through a relatively large any lar distortion.
- In the event that the fiber concrete does fail in compression, the failure is not sudden but preceded by extensive deformation.
- The increased tensile strength of the concrete permits the use of fiber concrete without special shear r \* forcement.

# CASE HISTORY - CONTAINMENT - DOUNREAY REACTOR ROOF

In 1972, SFRC was used in construction of a reactor roof at the UKAEA Fast Reactor at Dounreay, Scrtland. Because of space limitations, it was desired to maintain a minimum depth for the roof slab. The resulting conventional shear reinforcement would have been difficult to locate and fix accurately and its use would have been unduly time consuming on the construction program. The solution was to use SFRC to replace the conventional shear reinforcement. The SFRC aix used 180 lbs/yd $^3$  (107 kg/m $^3$ ) of 0.020 x 1.57 in. (0.5 x 40 mm) deformed fiber in a  $\delta.8$  sack mix. A total of 208 yd $^3$  (159 m $^3$ ) was used.

## DESIGN AIDS FOR CONTAINMENT OF NUCLEAR STRUCTURES

Two general articles on SFRC for reactor and spent fuel shipping cask design/construction are available [11,12]. Ramment [11] proposes a general theory for the elasth-plastic and cracked behavior of SFRC with reinforcing bars and describes a general finite element program which predicts crack propagation until failure of the structure. It also accounts for thermal cycling conditions. Advantages of the SFRC concrete are cited as resisting impact from brittle failures, increasing post-cracking load-carrying behavior, high energy absorption and improved seismic resistance. The fibers are not used to replace normal principal reinforcement but are used together with classical reinforcement. In the process, the safety factor for the structure is improved. In the case of anchorage zones in prestressed concrete construction, calculations indicaced that steel fibers in the amount of 2.8 volume percent are as effective as the normal bar reinforcement and provide a stiffer anchorage zone.

Laug and Lührmann [12] devised and tested a high density steel fiber reinforced concrete to use for radiation shielding in a cask between an inner liner and outer steel shell. The concrete used magnetite, hematite, iron granules and steel fibers. The purpose of the steel fibers was to aid in resisting damage from the impact of a possible accident. The concrete weighed 3.99 kg/dm³ (250 lbs/ft³) and had a comoressive strength of 5075 psi (35 MPa). The proportions of the mix and amount of fibers were not specified.

POTENTIAL APPLICATIONS FOR BLAST RESISTANCE IN STRUCTURES

Potential applications of SFRC reinforced structures to protect against blast or explosives include:

The use of inflation-formed SFRC domes for aircraft protection or personnel protection. Domes of up to 150 ft (45 m) or more in diameter 50 ft (15 m) high and 3 inches (75 mm) thick are feasible. In the spherical shell portion, only SFRC is required. Reinforcing steel bars are used around openings and to tie into the foundation.

- Hardening of missile silos. The blast resistance of such structures would be enhanced by the energy absorbing capabilities and ductility of SFRC.
- Ammunition storage buildings. The reduced spalling of SFRC would reduce detonation of stored explosives by internally-generated missiles.

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SIMULATION OF PRESSURE WAVES AND THEIR EFFECTS ON LOADED OBJECTS Part I: Outlining the Problem, Description of the simulation Device

Günter Hoffmann Kersten Behrens

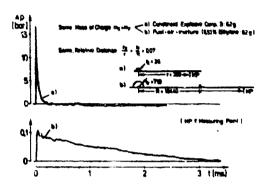
Fraunhofer-Institut für Kurzzeitdynamik, Ernst-Mach-Institut 7800 Freiburg, Fed. Rep. Germany

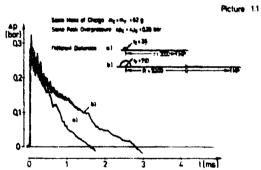
Abstract

Folast waves generated by detonations of HE or fuel-air-mixtures are characterized by their peak pressure and their overpressure phase duration, i.e. by two parameters. But normally unconfined fuel-air-mixtures will deflagrate generating a pressure time hisstory of a quite different shape. In contrast there is a relatively slow pressure rise up to a peak value followed by a suddendecay into a suction phase the minimum value of which is of the order of the overpressure peak value. The overall duration of this pulse is comparatively long. For such a pulse there are more than two parameters necessary for a complete description. Despite the small peak pressure value thase waves proved rather dangerous as numerous accidents have shown. Therefore it is destrable to get some insight into the destructive mechanism of these pulses. To be able to de that a special simulation device was developed which will be described.

# 1. Introduction

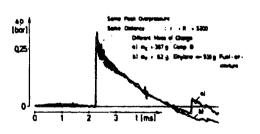
Blast waves generated by deconations of HE (High Explosives) or fuel-air-wixtures as e.g. FAE (Fuel Air Explosives) are characterized by their peak everpressure Ap and their overpressure phase duration t. Their pressure decay with time can be described by a FRIEDLANDER-function p=ap(1-t/t+)e+(-t/t+) for which only these two parameters are necessary. The same is valid for the pressure time history of the detonation of a fuel-airmixture as Fig. 1 demonstrates. One gets very similar pressure pulses -one can say nearly (dentica) ones at appropriate dis-tances- if the mass of the charge of condensed explosive and fuel-air-mixture are in a certain relationship. Figure 1.1 shows the peak overpressure of blast waves generated by a small high exlosive charge -that was in the example 62 g of Composition B- to be much higher and the overpressure phase duration to be much smaller than that one of an equivalent fuel-air-mixture at the same relative distance. In this example the fuelair-mixture was a stoichiometric ethyleneair-mixture containing therefore 62 g of ethylene. If the distances to the hemi-spheric charges are chosen in sucha manner





Picture 1.2

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Picture 1.3

Fig. 1: Pressure Time History ap(t) of Detonating Condensed Explosive and Fuel-mixture

that the peak overpressures are the same. the overpressure phase duration in the case of the ethylene-air-mixture is twice the corresponding value of the condensed explosive as Fig. 1.2 illustrates. But if the mass of the high explosive is six times the mass of ethylene in the stoichiometric fuel-air-mixture one gets no significant differences between the pressure time histories-for high explosive this is restricted to the far field of lower pressuresgenerated by Composition B or by the fuelair-mixture as it can be seen in Fig. This also can be shown in the normalized  $\Delta p/R_{H}$  -diagram and in the  $J_{H}/R_{H}$  -diagram of Fig. 2. Since this diagram demonstrates the overpressure distance relations and the impulse distance relations to be almost identical for Composition 8 and ethyleneair-mixture in a relatively broad range one can conclude the corresponding pressure time histories of the blast waves to be almost identical too, as was shown by Fig.1.3. Thus as to the simulation aspect the pressure time histories can be treated in the manner, that means in both cases the same well-known simulation facilities can be used, e.g. shock tubes.

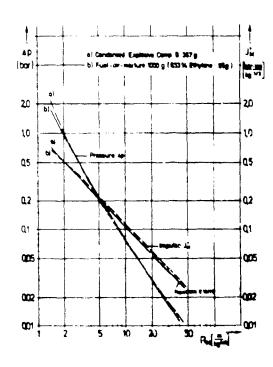


Fig. 2: Comparison of Peak Overpressure Ap and Impulse J\* of 1 Blast Mave Generated by Condensed Explosive and Fuelair-mixture

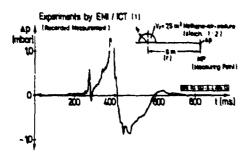
## 2. Outlining the Problem

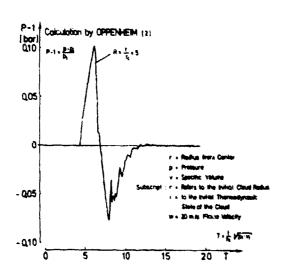
If there is not a high ignition energylike that of a detonator. normally an unconfined fuel-air-mixture doesn't detonate, it deflagrates. The same happens in the case of ignition failure of FAE. Experiments as well as calculations have shown that the time history of purely deflagrating fuel air clouds are quite different from those of detonating mixtures. On account of the quite different combustion process there one finds also quite another pressure time history. In contrast to the detonation the energy conversion is slow: The pressure distortion spreads only with sound velocity and the overpressure rises also slowly to its peak on account of the expansion of the hot burned Tuel-air-mixture which compresses the surrounding pure air. In the near field, out of the cloud boundary, the pressure rises to a value which is estimated not to be higher than about 300 mbars because the flame velocity is limited. If energy conversion is finished, i.e. if all reacting gas is burned, the surrounding compressed air flows quickly into the cloud like animplosion therefore outside an underpressure is generated which equalizes again slowly to the normal atmosphere pressure.

This deflagration mechanism results in a more-parametric pressure time history as it is shown in Fig. 3, diagram 3.1. This curve was recorded at experiments  $\{1\}$  with small methane air filledhemispheres. On account of the small volume and therefore also low flame velocity the peak pressure is also very small, 3 mbars are measured; but its duration is extremely long. From the beginning to the end it takes about  $400~{\rm ms}$ , i.e. t<sup>-</sup> 200 ms. This is very conspicuous in comparison with the detonation: a slight rise and a sudden decay to an underpressure peak and a suction phase with a function of the same order of that one of the overpressure. The corresponding times are nearly the same, i.e. t<sup>+</sup>=t\_ or I<sup>+</sup>= I\_-, resp.

Calculations which OPPENHEIM [2] had done for larger balloons resulted in the same feature of the curve as one can see in diagram 3.2: For a balloon of 50 m in diameter ap- 100 mbars by nearly the same pressure duration in the same relative distance of r/rm = 5. GIESBRECHT et. al.[3] came on the basis of their experiments and calculations with bursting vessels to the conclusion that a real gas cloud explosion in a factory cannot generate a peak pressure which exceeds the value of about 0.3 ber and a maximum duration of overpressure of about 200 ms. That is considered as an upper limit and it is obvious that there are variations depending on the cloud size and shape as well as on the kind of fuel and its concentration distribution. Also it is evident that the deflagration pressure time

history is defined by more than two parameters: e.g. rate of pressure rise, peak over- and underpressure, serval durations as pressure rise time, pressure changing time, duration of underpressure.





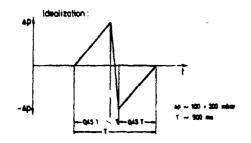


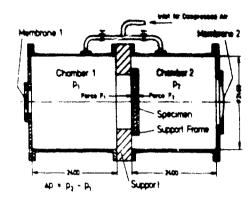
Fig. 3: Pressure Time History of a Deflagration

These waves proved sometimes rather dangerous too despite of the fact that their peak pressure values are much smaller than those of detonations as numerous accidents especially in chemical plants have shown in the past and as e.g. some ones mentioned in [3]. Therefore it seemed to be desirable to get some insight into the destructive mechanism and potential of this kind of pressure pulses. For this purpose the pressure time history was very approximately simplified to a shape shown in diagram 3.3 of Figure 3. For the further considerations and in the beginning of the experiments it seemed allowable to reduce the number of characteristic parameters to two as in the case of detonatively driven blast waves. In the mentioned idealized curve the parameters are coupled in such a manner that  $\Delta p = \Delta p^+$ , in the experiments  $\Delta p = -0.8 \Delta p^+$  or  $\Delta p = -1.3 \Delta p^+$  respective and the pressure rise times  $\{0 \to \Delta p^+, \Delta p_- + \}$  are each 45 % from the total duration. Tand the rest of 10 % remains for the pressure-changing-time.

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An experimental set-up to investigate the effects of deflagrative pressure waves on hit structures could consist of non-scaled free-field gas explosions. But there are some considerable difficulties applying this method. First of all in order to get pressure values in the desired range one would have to handle fuel-air clouds or balloons of up to 50 m diameter. That needs a lot of space, time and not at last much safety requirements. The second difficulty arises from the fact that deflagration is a stochastic process due to turbulences and distribution of concentration thus leading to bad reproducibility of the generated pressure waves. This would require a great number of tests in order to get reliable results by means of statitics.

3. Description of the Simulation Device To avoid these handicaps a simulator had to be found and developed which should permit to approximate the afore-mentioned idealized deflagrative pulse as accurate as possible including the possibility of parameter variations within a broad range After experimenting with a modified shock tube, slowly burning gun-powder or a compressed air driven piston in a tube the solution was found to be a two-chamberfacility. With the help of Fig. 4 the construction principle shall be explained: The simulator consists of a both-endclosed tube with constant diameter which is separated pressure-tightly by a wall -with an open squared section in the middle into two equal-volumic chambers. At the edges are the supports for the areal (twodimensional) specimen. A measuring girder contained displacement transducers fixed also at the specimen. Pressure gages were also mounted in the walls of each chamber. In the end cover of chamber 1 is a small opening, in that one of chamber 2 a port of larger diameter, both closed by a membrane. Both tube sections can be filled simultaneously with compressed air.



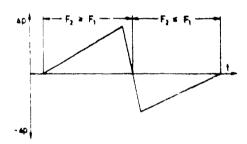


Fig. 4: Construction Principle of a Deflagration Simulator

At the beginning of the experiment both chambers are filled up to a pressure which is twice the wanted peak-pressure, i.e. should the peak over- or underpressurarise up to 100 mbars the filling pressure murt be 200 mbars. No bending or deflection forces, which would break the specimen are acting on it, because they are balanced:  $F_1 = F_2$ . At the time t = 0 the membrane of chamber 1 consisting of plastic or steel sheets is destroyed by a small HE-charge. Air leaves through the port and likewise pressure decreases. That means on the other hand the difference pressure between both chambers rises and a corresponding force  $F_1 = F_2$  is working in the direction to chamber 1 deflecting the specimen. If the pressure in chamber 1 arrives at half of its maximum value, i.e. the peak overpressure of the deflagration pulse (in the example 100 mbars), membrane 2 will be epened. On account of the large epening this chamber empties very quickly, therefore the acting force de-

creases. The pressure decay overtakes that one of the other chamber: In the overtaking moment the point is achieved where the pressures are equal to each other; in the difference pressure time history it means the passing of the t-axis and end of simulating the overpressure part. Off from this moment the force acting direction reverses until chamber 2 is exhausted. Then the underpressure peak is simulated, but in chamber 1 pressure decay is going on, i.e. the force F<sub>1</sub>-F<sub>2</sub> in direction to chamber 2 becomes shaller until it is 0, when chamber 1 is exhausted.

Thus it is possible to simulate the effects of a deflagration wave on an areal structure by reversing the forces. Considering the load it is the same as if forces are acting first from one side then from the other side or at the same side changes over- to underpressure respectively. By a skilful choice of the port diameters in the cover plates which can be calculated by the formula of De Saint-Vena: '/Wantzel (W2 = 2 q x/(x-1) Pim [1-(P)P.))ave(--)\ar  $(w^2 = 2 g \times /(x-1) P_1 w_1[1-(P)P_1)] \exp(x-1)x_1$ and by a convenient adaption of the chamber volumes as well as by coordinating of the time for opening the membranes the mentioned parameters could easily be influenced. By this method there is given a very good reproducibility.

In the upper part of Fig. 5 is shown the simplified pressure time history and that one achieved by the simulation device. The agreement is very good. In the lower part of this figure the deflection of a glass pane loaded with this pressure is plotted.

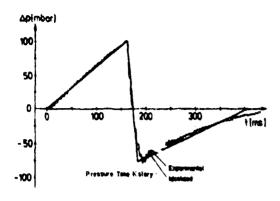
There are three curves: the straight one gives the experimentally found deflection, the dotted one is the result of a linear calculation and the cross-line is that one of a non-linear calculation using the equation

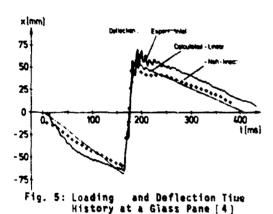
$$F = d_1 \cdot \ddot{y} + d_2 \cdot \dot{y} + d_3$$
with  $F = K_{\parallel} a^{\pm} P(t)$ ;  $K_{\parallel} = 1$  load factor
$$a = side 1 ength$$
of the pane
$$d_1 = K_{\parallel} m \qquad P(t) = acting force$$

$$d_2 = damping constant  $K_{\parallel} = mass factor$ 

$$d_3 = K_{\parallel} R(y) \qquad R(y) = restoring$$
force$$

Significant differences between experiment and calculation are only found in the simulated suction phase, because the presure time history in this part was not sufficiently to approximate with a tolerable effort. The best agreement was found in the pressure changing phase, (what also was best to calculate).





In the beginning of the experimental phase a small simulation set-up was installed with tubes of 1 m in diameter. As its working was successful and on account of scaling effects a bigger one with tubes of 2.4 m in diameter was built. This one is shown in Fig. 6. The upper picture gives a view to the chamber with the big discharge opening. On account of the available membrane sizes and for better handling the orifice contains three openings. The lower picture shows the entrance door through which the specimens were brought in and which contains two small discharge ports.

A great advantage of this simulation facility is that the same specimen under the same supporting conditions can be loaded statically as well as dynamically. In the first case it is only necessary to fill the chamber 2 very slowly with compressed air. Thus it is very easy to compare the dynamic and static behaviour of a specimen without changing its position on the supports. In this way it is also possible to ascertain the restoring force which is

important for the calculations.

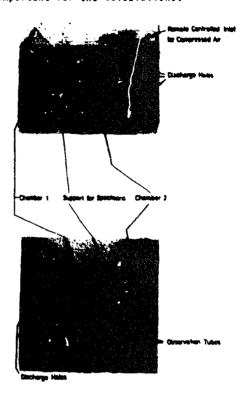


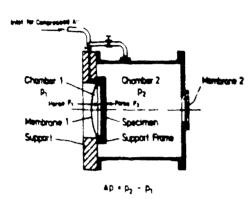
Fig. 6: Views of the Deflagration Simulator [4]

By a small variation of the device it is also possible to simulate the blast waves of a detonation within a certain, a little bit restricted extent. Chamber 1 must be minimized to the smallest volume that is possible. In an extreme case this may be not more than the volume between the specimen and the membrane vaulted by the compressed air, Fig. 7.

Then one finds a very sudden rise of the acting force in chamber 2. The rise time will take a time of about 3 to 5 ms. That is surely more than the infinitely steep rise of a blast wave. But it is acceptable for a specimen with a very long duration of its natural motion, since then there is only a negligible influence an the dynamic behaviour. This is mostly found by specimens with a heavy mass like wells of concrete. In Fig. 8 is plotted the calculated displacement of reinforced concrete plates versus time.

The dotted line shows that case when the pressure rise takes t, = 2.5 ms, the straight line when the rise is infinitely

steep. In the upper couple of curves the reinforcement consists of steel bars in the lower of glassfiber bars. It can be seen that the duration of natural motion is more than one order longer than the time for the pressure rise.



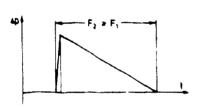
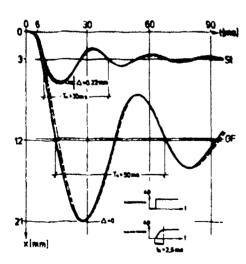


Fig. 7: Construction Principle of a Detonation Simulator



Agriconomic Si Shori Barn OF Mine Plane Barn

Fig.8: Celcyleted Deflection Time Histories for Different Pressure Rise Times

Fig. 9 shows two pressure time historie: In the upper one is shown the simulation of a pressure wave with a very long duration as it may be caused by a nuclear explosion. This is achieved when the membrane port of chamber 2 remains closed or if it is very small one gets a slight decay since the compressed air can escape only slowly. The curve below shows a simulated blast wave as it might be generated by a conventional weapon. Then a large opening will be necessary in the coverplate. It is obvious therefore that the pressure decay can easily be manipulated by the width of the opening.

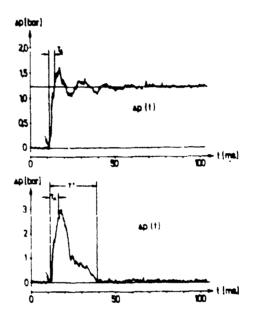


Fig. 9: Pressure Time Histories at Experiments with a Detonation Simulator

SIMULATION OF PRESSURE WAVES AND THEIR EFFECTS ON LOADED OBJECTS Part II: Experiments and Calculations; Destruction Curves

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# Abstract

Experiments to investigate the response of model panes and model brick walls to deflagrative pressure pulses were carried out in the deflagration simulator described in part 1 of this paper.

Calculations based on a one-degree-of-freedom oscillator model were compared with the test results. They led to a set of curves in the scaled pressure impulse plane from which isodamage or destruction curves were derived for the specific objects under investigation. These curves differ from the well known P-I-curves for objects under blast load conditions in that the curves for deflagrative loading split up into two branches in the region of small impulses. This is due to the significant underpressure phase of the deflagrative pulse which causes resonance effects in the response of the loaded object.

# 1. Experiments

Test objects were

- panes of the size 50 x 50 x 0.3 cm<sup>3</sup> and 100 x 100 x 0.6 cm<sup>3</sup> with three different support conditions at the edges (simply supported, clamped by a metal frame, and fixed by permanently plastic putty)
- masonry walls (131 x 131 x 6 cm³) made of 1:2 scaled model bricks (Fig. 1.1) fixed at the edges by steel u-shaped frames and clamping devices (Fig. 1.2). These walls should model a simple structural component of an industrial building frame shown in Fig. 2.

The load consisted of approximated static loading, i.e. very slow pressure rises (slope of pressure rise of about 10 bar/s) until rupture occurred end deflagrative loads. The peak overpressure varied from 30 mbar to 200 mbar in the case of loading the panes and it was always above 230 mbar for the masonry walls. Total pressure pulse times were in the range from 10 ms up to 750 s thus including the natural periods

(10 ms to 28 ms) of the objects under investigation at the lower limit and approximating static loadings at the upper limit of the time interval.





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Fig. 1: Specimen of the Model Masonry Slab and Comparison of Bricks





Fig. 2: Examples for Wasarry in Steel Skeletons at a Workshep-Mall

The essential quantities measured during an experiment were the difference pressures at the test objects and the defloctions in the widdle of the square plates as function of time (see Fig. 5 of Part 1). In the case of static loads the combinations of measured pressure time histories with deflection time histories result in experimental restoring functions some examples of which are shown in rig. 3.

The curves in diagram 3.1 and diagram 3.2 respectively are the functions for small panes with fixed edges and masonry walls. All of them are nonlinear. The increasing

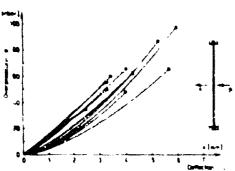


Diagram 31 Olass Panes with Clamped Edges

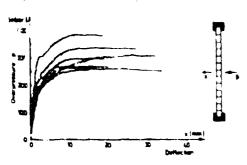


Fig. 3: Static Load Deflection
Curves of Glass Panes and
Masonry Slahs

slope in the case of the panes is due to membrane stresses at larner deflections. The scatter in the copes of the curves is an effect of not completely reproducible clamping of the panes - it is significantly reduced when the adges are only simply supported, dut of coorse there is still a considerable scatter of about 25 % in the resistance to rupture of the panes. Diagram 3.2 shows the maconry walls to be almost linear exactic at small definctions and plastic at larger deflections. Scatter is essentially due to scatter in the material properties. The restoring functions were needed for the calculation of the ballow-mentioned destruction curves.

In the case of short deflagrative loading dynamic effects could be observed. To give an example it should be mentioned that in certain cases of deflagrative leading of the small panes rupture occurred in the underpressur, phase at prossures of approximately -54 mbar and deflections of -8 mm. Peak overpressurer and the corresponding maximum deflections were +83 mbar and +7 mm respectively. Pressure pulse durations were 100 ms and 77 ms. The time it took to change from peak overpressure to peak underpressure was 10 % of the nulse duration and therefore it was in the range of the natural period of the panes (10 ms).

This means that obviously resenances and occurred.

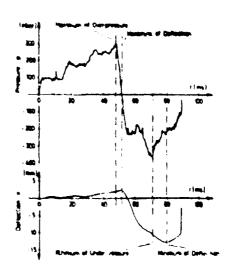


Fig. 4: Recorded Pressure and Deflection Time Histories of Masonry Slabs (Dynamic Load)

Another example for dynamic effects is illustrated in Fig. 4. Diagram 4.1 represents the pressure time history of the load while diagram 4.2 shows the corresponding deflection time history of a meconry wall, there is a definite delay between pressure maximum (minimum) and deflection maximum (minimum) which is caused by the inertia of the Wrll. The minimum deflection is about 6 times larger than the maximum deflection while the relation of pressure minimum to pressure maximum is about 1.3:1.

The wall was not dest-oyed though some cracks had formed. These cracks having a width of some tenth's of millimeter: and therefore being coloured by black ink for visualization purposes are shown in Fig. S. At the front side there are the typical diagonal cracks and at the rear the cracks are parallel to the edges. In this context the front side of the wall is that side on which the overpressure acts at the beginning of the pressure pulse, which means the wall in Fig. 5 being bent away from the chamber 2 during the overpressure phase and being bent towards the chamber 2 during the underpressure phase. Keeping this in mind one can conclude from Fig. 5 that the cracks must have formed as a result of the underpressure phase which is plausible considering the deflections of Fig. 4.

Finally Fig. 6 gives an illustration of a destroyed pane and a destroyed masonry wall. For these objects destruction was defined as complete fragmention, which

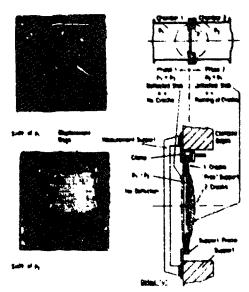


Fig. 5: Formation of Cracks by Dynamic Pressure-Loading

may be self-evident in the case of the brittle panes but which may be differently defined for other objects depending on their purpose, e.g. cracks may be tolerable considering the stability of a shelter but they are not acceptable if gas tightness is of interest.



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Fig. 6: Destroyed Specimens

# 2. Calculations

It is well known from structural dynamics that a one-degree-of-freedom system can be used to describe the gross behaviour of simple structural elements such as plates with sufficient accuracy. Consider the equation of motion

where x is the displacement of the mass m. R is the acceleration,  $R(x^t)$  is a restoring force and F(t) is the time-dependent external force acting on the mass m. In this

equation damping is omitted.

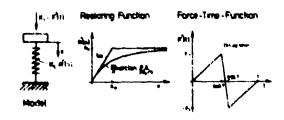


Fig. 7: Simplified Model for Calculation

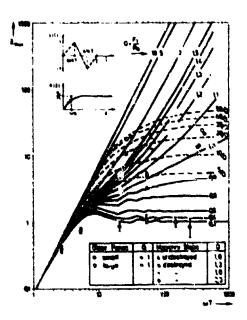


Fig. 8: Deflection Maxima in the 1. Period of Oscillation

The reasons for neglecting damping are discussed extensively by Saker et.al {7}. Equating the work done by the external forces, the kinetic and the potential energy of the model and the real system respectively yields trensformation factors for the mass m°, restoring force R\* and external force F\* of the physical system such that the following relations hold [8].

With respect to the previously shown resistance functions of the masonry walls

the restoring force  $R^{\bullet}$  is approximated by the arctan-function:

$$R^{*} = \frac{2R_0}{n} \operatorname{arctan} \frac{n\pi}{2R_0}/k$$

and the external force  $F^*$  is assumed to be the simplified deflagrative pulse (see Fig. 7).

Applying the following transformations

$$\bar{t} = \omega t = \sqrt{\frac{x_L}{x_m}} \frac{k}{m^2} t$$
 time  
 $Q = \frac{x_1}{y_0}$  force  
 $\bar{x} = \frac{x}{y_1/k}$  displacement

one finally gets the nonlinear dimensionless second order differential equation

$$\frac{2}{x} + \frac{1}{6} = \frac{2}{n} \arctan \left( \frac{n}{2} Q \tilde{x} \right) + f(\tilde{t})$$

This equation is in the limit for  ${\bf Q}={\bf D}$  a linear equation since

$$\lim_{Q\to 0} \frac{1}{Q} \frac{2}{n} \arctan \left( \frac{n}{Z} Q \hat{x} \right) = \hat{x}$$

Hence for small Q it should approximate the response of the above-mentioned panes the resistance functions of which did not deviate too much from linear functions.

Unly the first period of this oszillation is of interest since actually damping will attenuate the deflections of physical structures in later cycles. " ce one can consider the maximum displacement  $\mathbb{R}_{\min}$ , both the minimum displacement  $\mathbb{R}_{\min}$ , both the refront the first period of oszillation as the quantities which are essential for the response and the eventual failure of a structure.

Performing the calculations for different pulse durations T one obtains R and  $R_{\rm min}$  as functions of T with as a persweter (6). Fig. 8 shows a plot of the function  $R_{\rm max}(T)$ . The normalized deflection function for Q=0.2 is almost identical with the curve for a linear restoring force. A comparison of the calculated deflections for small Q with the experimental points for the panes shows a relatively good agreement. Addit

tionally to the displacement curves the broken lines represent curves with different constant multiples of the normalized elastic displacement  $R_{\rm El}$  as parameter (definition of  $\tilde{R}_{\rm El}$  as e. Fig. 7. Since  $0=F_{\rm I}/R_{\rm n}$  and  $R_{\rm o}=kx_{\rm El}$  one gets  $\tilde{R}_{\rm el}=I/Q$ ). In the E experiments with masonry walls the slabs were fragmented at deflections approximatives large as the wall thickness (S). This corresponds to 20 to 30 times the elastic displacement  $x_{\rm El}$  of the walls. Fig. 8 illustrates the corresponding experimental points to be in vicinity of the dashed curve with parameter 30  $R_{\rm El}$ .

Fig. 9 shows the curves  $\overline{\mathbf{x}}_{min}$  as functions of the normalized pulse  $\overline{\mathbf{x}}_{min}$  duration with 0 as parameter.

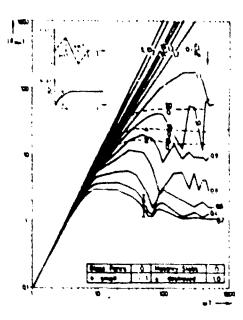


Fig. 9: Deflection Minima in the 1. Period of Oscillation

According to those curves significant resonances should occur. The normalized test values for the destroyed masonry walls are in the range of 15 to 25 times the elastic displacement, that is, in the approximate range of wall thickness. Following the procedures described in [9] one can use the normalized diagrams of Fig. 8 or 9 to calculate dimensionless (P-1)—diagrams. Since the total impulse of the assumed simplified deflagrative pulse is equal to zero one can consider the impulse of the positive phase I\* which together with the peak force completely characterizes the deflagrative pulse. Using the following relations

Fig. 10: P-I-Diagram for the Load of the One-Degree-o -Freedom Oscillator

()

one obtains the curves of Fig. 10 which is simply a somewhat different presentation of the curves of Fig. 6.

finally one can replot the fragmentation curve introducing the physical parameters of the walls to obtain the dimensional P-1-representation of the curve shown in Fig. 11. It must be noted that the pressures and impulses of this diagram are the quantities acting on the wall which means that they are nermally reflected pressures and impulses. Assuming reflection factors of 2 for both quantities as in the acoustic limit (f blast waves one could easily get the corresponding P-I-diagram for the incident waves. The dashed part of the curves indicates that this range of the solution is of no physical meaning since under-

pressure phase and overpressure phase should be of the same magnitude according to the assumptions. It may even be doubted that there exist reflected deflagrative pressure pulses having a peak pressure value close to one bar and still being symmetric. The deflagrative cloud experiments known to the authors which are essentially small scale experiments give no indications of peak pressure values above 300 mbar. (GIESBRECHT et. al.) (J)

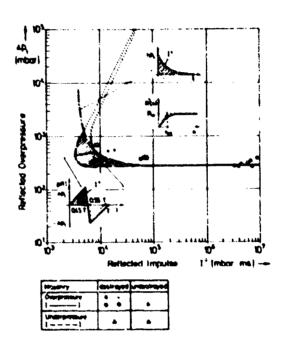


Fig. 11: Destruction Curve for a Masonry Wall

fig. 1: clearly illustrates the effects of the underpressure phase on the loaded object. There is a region of resonances between the two branches of the destruction curve in which deflagrative pulses should destroy the walls (objects) by their underpressure phase but not by the overpressure loading. For reasons of comparison a third curve based on the calculations of MAYR-HOFER and THOR [10] for blast loaded elastic-plastic objects is plotted in Fig. 11. In the static loading range the effects of a blast wave and a deflagrative wave of the same reflected peak overpressure and the same reflected positive impulse are equal. In the range where resonance to deflagrative loading occurs the deflagrative wave may destroy the objects while the blast wave does not.

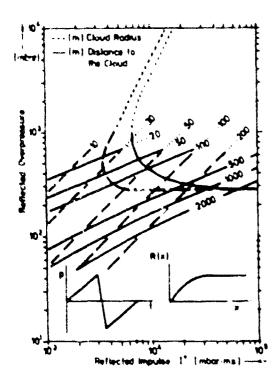


Fig. 12: Destruction Curve for Masonry Walls and P-I-Relation for Deflagrating Clouds ( i2), Flame Speed 20 m/s)

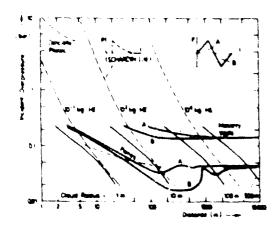


Fig. 13 Destruction Curves (Solid Lines: Overpressure Distance Relations according to Oppenheim 72) Flame Velocity 20 m/s)

Finally one can combine the dostruction curve of the P-:-diagram with the overpressure-distance relations for exploding clouds. Since there are only a few experiments on a small scale basis with deflagrating clouds and since therefore the pressure and impulse distance relations are not really he in for deflagrating clouds as a first approach to the problem the corresponding relations calculated by OPPERMEIN et.al, are taken. Assuming a laminar flame speed of 20 m/s and reflection factors of 2 the straight lines in Fig. 12 represent the OPPERMEIM pressure-impulse-relations for constant cloud radii and constant distance respectively. Reflected pressures and impulses above and to the right of the destruction curve will rupture the wall and it can easily be seen at which cloud radius and at which distance from the cloud the fragmentation could occur.

Another representation for destruction curves was developed by SCHARDIN (ii) for numerous blast loaded objects. Again based on OPPENHEIM's (2) calculations for deflagrating clouds and assuming the flame speed to be 2G m/s as above one gets in this kind of representation the destruction curves of Fig. 13. Pressures and impulses in this diagram are the incident quantities and the destruction curves for panes and walls are derived from the corresponding P-I-diagrams assuming reflection factors of 2.

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# RESPONSE OF STRUCTURES TO DETONATIONS IN SAND

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Tests made at RSFA have unoun how the pressure on the wall of a structure from deconations of explosives in sand depends not only on the explosive and its distance to the wall but also on the properties of the wall (e g mass and stiffness). The paper gives data from these tests and a suggested procedure for design of walls in buried structures exposed to detonations effects. The procedure is based on an energy-absorption concept.

# BACKSKOUND

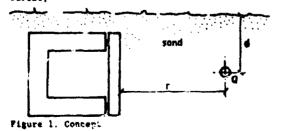
Many data on shock waves in sand generated by explosives can be found in literature. Host of these however are freefield data of limited value to the engineer to design structures in send to withstand the effects of detonations.

Some sources e g /1/ and /2/ give peakpressure and impulse density on an infinitely rigid wall. A pressure increase factor of 2.0 and an impulse increase factor of 2.6 are suggested relative to the corresponding freefield values.

Ordinary structures are more or less compliant when exposed to loads. This is true also for hardened structures. In order to get a better understanding of the effects on different structures from explosives in sand a research program was started at the RSFA a couple of years ago. Responsible for this program is Staffan A Hultgren. Results have been published in /3/ and /4/.

# PROBLEM AND TEST DEVICE

The problem can be identified from figure 1. A rigidly supported well is exposed to a detonating charge, Q, at a distance, r, and with a depth of burial, "



The behaviour of walls with different sizes and different designs for different values of these parameters are studied.

And basic parameters in sencing the structural behaviour of a wall exposed to a dynamic load are the mass and stiffness.

To facilitate a study of these parameters a test device according to figure 2 was designed where the mass and stiffness of the front could be varied independently. The front consisted of a 0.34 m dismeter circular disc supported by a horisontal movable axis on ball bearing: and by a helical spring all within a 295 kg 18 m long steel cylinder.

The mans of the disc was varied from 5.2 to 105 kg and springs were used with springconstants ranging from 0.1 to 1.2 MM/m.

The pressure against the disc and its acceleration, velocity and displacement were measured.

The pressure measured on the disc is then compared with the inertial pressure and the pressure corresponding to the spring force.

The inertial pressure can be calculated from the measured acceleration using Newton: 2nd law of motion. The spring force is equal to measured deflection multiplied by the spring constant.

A comparison between these three pressure components is given for different mannes in figure 3. Hass and stiffness both contribute to the pressure. While the inertia forces develop momentarily the forces from the spring develop as the deflection increases.

Conclusively more wass constitutes a shorter risetime for the pressure.

It should be pointed out, that the duration of the pressure indicates that not only the mass of the disc but also parts of the mass of sand between the charge and the wall contribute to the structural behaviour.

From figure 3 is clear, that the pressure is dependant on the properties of the wall and also that the duration of the pressure exceeds by far the fundamental period of the wall. Neither the pressure nor the impulse is therefor well suited for design purposes. For this reason an energy-concept has been adopted.  $\label{eq:concept} % \begin{array}{ll} & & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ \end{array}$ 

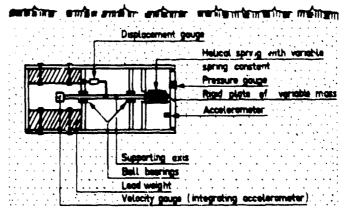
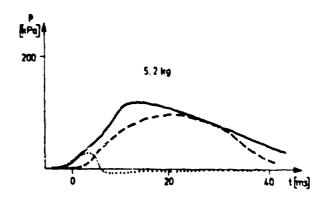


Figure 2. Test device



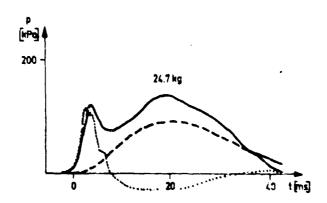


Figure 3. Wall pressure components. Wall stiffness = 0.5 MM/m.

# WALL TESTS

The initial test series with the device in figure 2 was followed by tests where walls supported along the four edges were examined. Concrete wills in scale will 3 and in full scale with different thicknesses and different amounts of reinforcement were tested. Absorbed energy by the wall-slab when deforming was calculated according to yield-line theory. A straight linefit to calculated values gives the specific energy per unit area of the slab to

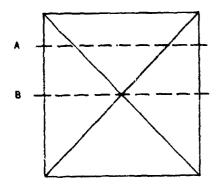
$$E_{\pi/Q}^{1/3} = 1040 \ (\pi/Q^{1/3})^{-4.74} \ \text{Mm/(m}^2 \cdot \text{kg}^{1/3})$$

The idealised deformation of the slab is shown in figure 4. The formula for En shows, that the distance, r, is highly significant for the energy. This means also that the energy density is unevenly spread over the slab. The parts of the slab near the supports are more remote from the charge than the midpoint. Conclusively they will be exposed to a lower density. The specific energy can be averaged over the slab by integrations in an iterative procedure giving a factor § .

Table 1 gives data for the concrete walls tested. It also gives the specific energy, Ea, calculated using the averaging factor . Ea is given as a function of the specific distance in figure 5. The equation for the straight line is:

$$Ea/(1 \cdot q^{1/3}) = 1540 (r/q^{1/3})^{-5.53} He/(n^2 \cdot kg^{1/3})$$

Two of the Lests were made in compacted sand while the other were made in loose sand. This difference in compaction did not give any significant differences in the test results.



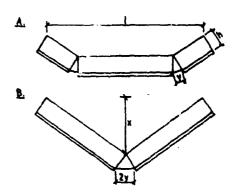


Figure 4. Slab with yield lines. Elevation and sections.

r	Q kg	r/Q.1/3	1	h m	Reinf ratio	x x	Compac- tion	$E_{a}/(\frac{1}{3} \cdot q^{1/3})$ kMm/(m <sup>2</sup> + kg <sup>1/3</sup> )
1.26	1	1.26	0.73	0.04	0.94	12	-	0.33
1.60	i	1.00	11	12	#	39	-	1.18
0.79	Q.5	1.00	11	н	11	37	-	1.65
0.59	0.2	1.00	11	11	II.	24	-	1.87
1.26	2	1.00	11	49	18	56	-	1.25
1.00	i	1.00	ŧŧ		n	42	-	1.28
2.15	10	1.00	1.8	0.13	0.54	56	-	1.76
-,	**	1.00	11	**	*1	54	Yes	1.76
11	11	1.00	þŧ	**	1.0	29	-	1.76
1.70	**	0.79	n	11	H	67	-	4.92
2.71	11	1.26	11	**	0.54	16		0.45
1.70	11	0.79	11	G.28	0.54	34	•	5.27
***	11	"	n	11	11	42	Yes	6.50
1.36	11	0.63	**	**	1.0	44	•	18.6
2.15	11	1.00		0.13	0.30	128	-	2.20

Table 1. Date for the tested conrete walls.

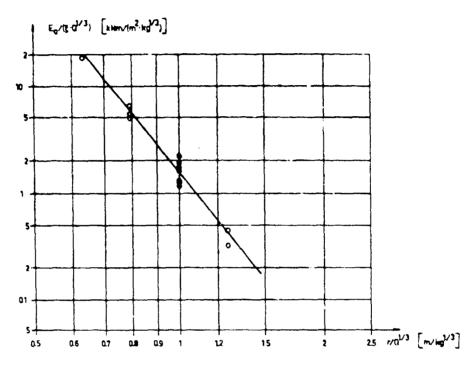


Figure 5. Specific energy vs specific distance for walls tested.

The equation for Re can be used for design purposes. With the energy transmitted to the wall from the detonation calculated with this equation the design engineer then has to find dimensions of the wall and reinforcement in it so that this energy can be absorbed without deformations exceeding permitted values.

The equation so far is based on data within the interval 0.63 to 1.26 for the specific distance,  $r/Q^{1/3}$ , and with the charge on the axis of symmetry of the wall.

In order to check the formula outside these limitations some more tests have been performed. In these tests the shape of the deformed wall is enclysed using photogrammetric methods. Figure 6 shows as an example a plot of the deformed shape of a slab after test. The measured deflections can be used for a more sophisticated calculation of the energy-absorption in the wall than with the model in figure 4.

Preliminary results from these tests support the using of the equation for Es for design purposes.

# CONCLUSIONS

The tests performed on concrete walls exposed to affects from detonating charges in sand support the use of the energy-absorption concept, outlined in the report, for design purposes.

# REFERENCES

- /1/ Schall, R, über Druckwellen bei Sprengungen Sand und sandigen Boden, Hobel Heft, p.76. Hei 1940.
- /2/ Effects of Impact and Explosion. Summary Technical Report of the Mational Defense Research Committee. Mashington D.C., 1946.
- /3/ Hultgren, S.A., Response of Buried Model Structures to Buried TWT-Explosions in Send. Proc 6th International Symposium on Military Applications of Blast Simulation. Cahors, 1979.
- /4/ Hultgren, 3 A, Response of Reinforced Concrete Walls to Buried Explosions in Sand. Proc 7th International Symposium on Military Applications of Blaz Simulation, Medicin Eat, 1981.

Figure 6. Example of deformed shape of 1.8 by 1.8 m wall 0.3 m thick with 1% reinforcement ratio exposed to a 50 kg detonation at 3 m distance. Maximum deflection appr. 0.1 m. 220

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EFFECTS OF BARE AND CASED EXPLOSIVES CHARGES
ON REINFORCED CONCRETE MALLS

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### **ABSTRACT**

This paper represents a summary of an extensive investigation concerning the local effects of bare and cased explosives charges on reinforced concrete walls. The investigation includes a literature search as well as several tes; series. As a main result, charts for the prediction and comparison of the effects of bare and cased explosives charges are developed.

The most important conclusion is that cased charges result in perforation of reinforced concrete walle at distances up to ten times larger than bare charges of the same weight. Vice versa, given the charge weight and the distance, the well thickness required to avoid perforation is up to three times larger for cased charges than it is for uncased charges. Hence, it becomes evident that simulating local effects of weapons with bare charges - as often done for practical reasons - may lead to considerable underestimation of the actual effects.

# 1. INTRODUCTION

In this paper the damage to reinforced concrete slabs from bare explosives charges and weapons detoneting at or near such slabs is discussed.

Is this topic still of such interest as to give rise to a detailed investigation? The need for reliable data on the effects of explosives charges and weapons detonating close to walls is not new. However, it becomes of immediate interest in connection with some actual defense and safety prohibms.

As an example, a small free-standing ammunition megazine is shown in Figure 1. The ammunition stored therein might explode or otherwise be damaged by a hostile attack. In the course of analyzing survivability chances, the probable circular error (CEP) of the relevant weapons has to be compared with the size of the target area. But the virtual target area strongly depends on the distance to the building at which a detonating grenade or bomb can destroy the wall and possibly initiate a detonation of the stored ammunition.

As another example, a safety problem within an ammunition factory can be mentioned. This was, in fact, the actual problem which stimulated our investigation (Figure 2). The question was whether or not a dividing wall, designed to withstand an uncased charge of 10 kg of TMT, could protect a workshop place from a detonating HE grenade of calibre 155 mm containing 6.8 kg of explosives.

Some data referring to these problems can be found in various handbooks and in the literature. Information, however, as to which cases are really referred to, is generally rather poor. In particular, it is not possible to make a distinct comparison between the effects of bare and cased charges. On the other hand, it was clear to us from a few earlier tests that casing does affect the resulting damage significantly.

With the purpose of improving our knowledge concerning this problem, an investigation was performed, including the following three steps:

- Existing data were gathered from earlier tests and from literature. A number of 87 tests was evaluated with respect to information regarding this problem.
- Three complementary test series including a total of 46 tests were conducted in order to allow for a systematic variation of parameters.
- Design charts, both for bare charges and cased charges, have been developed and compared to each other. Moreover, an extensive collection of photographs has been published. This might give a better insight into the actual phenomena than any theoretical model.

As the most important conclusion it has been recognized that cased charges can produce perforation of reinforced connete walls, if detonating at distances of up to ten times larger from the wall than uncased charges of the same unight. In the case of the above-mentioned assumption magazine, the distance from which a projectile or book detonating above ground can destroy an outer wall, determines

the size of the virtual target area. Thus, it is essential to realize the big difference in the destructive range of bare and cased charges.

In the case of the dividing walls in an ammunition factory, the wall designed to withstand 10 kg of uncased TNT proved to be inadequate for the 155 mm HE grenade. The grenade representing a casud charge of only 6.8 kg of explosives required a wall thickness of more than twice as much.

# 2. DEFINITION OF DAMAGE CATEGORIES

Damages on a reinforced concrete wall from near-by explosions may vary from minor cracks up to complete perforation. Figure 3 shows an overview of characteristic damages. For the assessment of the protection provided by a wall, damage effects at its back are most relevant. Three damage categories have been defined for the evaluation of the tests and other data:

Damage Category 0: No relevant damage at the back
Damage Category A: Moderate up to heavy spalling
at the back

Damage Category B: Complete, open perforation

These categories are rather wide and do not represent a sophisticated system, but this grouping facilitries the placing of the observed individual damages in the groups chemselves. These damage categories allow to draw conclusions with respect to the lithality of persons exposed behind a well, or for a detonation's propagation to stored ammunition. Since such considerations usually have to be based on pragmatic approaches, a more detailed classification of the dimage categories would not be useful.

# 3. COMPILATION OF THE EVALUATED TESTS

Number and type of test	Explesives	Pistance_	Thickness of slab t	
Sarry Charges				
Own tests: 31	0.013 - 10 kg	0-1=	8,1 - 0.6 m	
Frec Literatury: 65	8.86 - 227 kg	0 - 1.2 p	0.09 - 1.7 m	
Cased Charges				
Bun tosts: 15	6.37 -6.86 kg	9-5 m	0.1 -0.4 m	
Frem 11torsture: 22	0.2 - 22 kg	0-4 m	0.1 -1.2 m	

Using all 133 tests as data base, the variation of the following parameters has been investigated: 4

- Size of explosives charge; for explosives other than TNT, the TNT-equivalent for corresponding peak overpressure has been used.
- Charge weight to total weight ratio for cased charges
- Shape of charge
- Distance from center of charge to slab surface
- Thickness of concrete slab
- Reinforcement u (weight per volume)
- Concrete compression strength
- Damage category 0, A or B

In a couple of tests, additional parameters have been investigated such as initial velocity of wall-debris, their travel distance and mass. Furthermore, data from 12 earlier tests with bombs and grenades located at the wall surface below ground (i.e. tamped charges) have been included.

# 5. RESULTS OF THE INVESTIGATION

The previously mentioned tests have been evaluated systematically and design charts have been developed showing wall thickness versus scaled distance for the different damage categories. It was found that limited variation of concrete strength, reinforcement and charge to total weight ratio for cased charges did not strongly affect the results. But the observed damage was considerably more severe when the reinforcement of the concrete was less than a threshold value of about 50 kg/m<sup>3</sup>. On the other hand, the extent of damage attenuated for cased charges if the weight of the casing was less than 40 % of the total weight.

In Table 4 the parameter limits for the succeeding design charts are given. Selecting data from tests which meet these limits allows to obtain clear results.

Figure 5 shows the design chart for bare explosives charges. In this chart the two axes are the scaled wall thickness and the scaled distance of the charge from the well respectively. The lower line represents the threshold between perforation and spalling. The upper line correspondingly represents the limit between the spalling category and the one for minor demage. The two threshold lines are parallel in this log/log-plot, i.e. they are separated by a constant factor. Regarding the well thickness, the factor between the beginning of perforation and spalling at the back is always two for bare charges.

Figure 6 shows the corresponding plot for cased charges, i.e. grenades and bombs. The threshold between the different damage categories is again quite sharp. There is one particular data-point from an older test with 50 kg bombs shown, which does not fit into its category. At a scaled distance of 1.5 m/kg $^{1/3}$  only minor damage was reported, whereas the chart indicates that spalling or perforation should occur. Next to this point, at a scaled distance of about 1.6 m/kg1/3 a test with a heavily cased 105 mm HE projectile produced perforation slightly above the threshold line. The analysis of the test has led to the conclusion that damage to reinforced concrete walls from cased charges is dominated by the impact of fragments, particularly at large scaled distances. Of course, the ratio of net explosives charge weight to total weight is important for the damage of light cased charges in the transition range between bare and cased charges. This parameter has not been studied in more detail yet.

All data shown in Figure 6 are based on tests with non-tamped grenades and bombs. A comparison with data from tamped cased charges shows good agreement for weapons which have contact with the exposed wall. Tamping has, therefore, only little effect on the damage produced by cased charges with wall contact.

In Figure 7 the demaging effects of bare and cased charges are compared. For a given wall thickness, the distance required to avoid perforation is four to ten times larger for cased charges than it is for uncased charges of the same explosive weight. Vice versa, given the charge weight and the distrans, the wall thickness required to avoid perfor inn is up to three times larger for cased then for uncased charges. Hence, it becomes evident that cimilating local effects of weapons with bare char-- as often done in tests for practical reasons - may lead to a considerable underestimation of the actual effects. Figure 8 gives a visual impression of the damage produced by two different types of charges placed at the same distance from a reinforced wall.

This investigation was sponsored by the Devense Technology and Procurement Group, TA 6, of the Swiss Federal Department of Defense. The results including numerous pictures from tests are published in the following reports which are available upon request:

- Amt für Bundesbauten: "Sprengversuche an Betonwänden", Ernst Basier & Partners, B 922,10, February 1980
- Gruppe für Rüstungsdienste, TA 6: "Sprengversuche an Betonplatten", Ernst Basier & Partners, 8 3113-1, June 1981
- Grupps für Rüstungsdienste, TA 6: "Lokale Schedenvirkungen an Betonplatten durch Sprengladungen", Ernst Basier & Partners, B 3113.10-1, Sep\*. 82

# Example: Target Areas for Different Dernage Categories

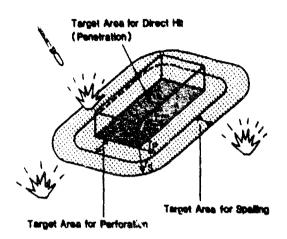
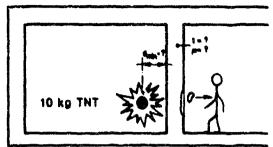


Figure 1: Assessment of target-area for aboveground building for different damage categories as a basis for estimating the probability of survival for a given type of attack.



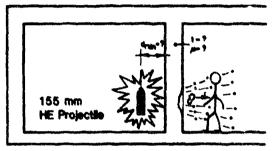


Figure ?: Example: Design of a Dividing Wall in an Ammunition Factory

# Definition of Damage Categories

Distance of Explosion from Wall	Characteristic Damages	Catality Demoke Catality
	ble injevent demege, ericks ev. snell grafts	
袋 [	erofor, deflections and eracks	0
	Spalling on book	
<b>發</b>	Heavy eacting on took	
袋	Pertersilge	
	Higny Perforation	

Figure 3: Definition of Damage-Categories

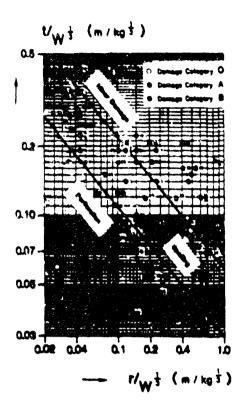
# Range of Expiseives Charges Covered by Decign Charts

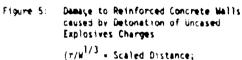
# Charge Visight

Uncased Charge     Cased Charge, not	0.01 kg - 2 0.3 kg -	-	
Total Weight	0.5 kg -	50 kg	
Charge Weight Ratio	13 % -	<b>60 %</b>	

Distance from Targe	đ	contact u	depth 1 of a
Thickness of Concre	delS etc	t a	1m - 12m
Reinforcement	Æ	60 kg/m <sup>8</sup>	- 180 kg/m³
Concrete Strandh	A	20 NAmm <sup>2</sup>	- 55 NAmm <sup>2</sup>

Figure 4: Range of Farameter Covered by Design Charts





(r/M''' = Scaled Distance; t/H<sup>1/3</sup> = Scaled Hall Thickness)

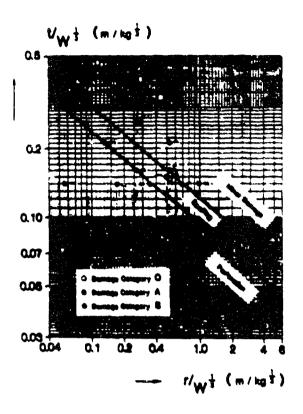


Figure 6: Damage to Reinforced Concrete Walls caused by Detonation of Cased Explosives Charges

(r/W<sup>1/3</sup> = Scaled Distance;

t/h1/3 = Scaled Hall Thickness)

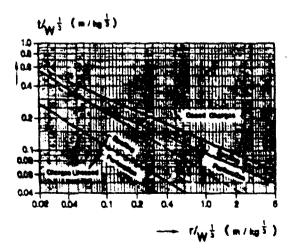


Figure 7: Comparison of Damage Caused by Uncased and Cased Explosives Charges

# Before Test

# After Test

10 kg THT

Distance r = 0.5 m

Hall Thickness t = 0.3 m Back of exposed well shows minor cracks



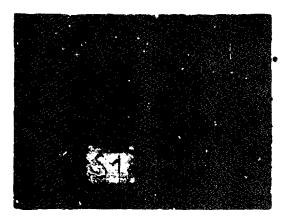


**Cased Charge** 

15.5 cm (6.85 kg TNT)

Distance r = 0.5 m

Hall Thickness t = 0.3 m Exposed wall completely destroyed



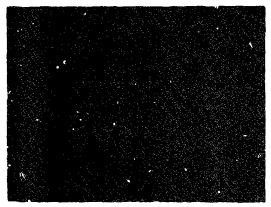


Figure 8: Visual comparison of the effects of bare and cased charges

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# THETE AND EVALUATIONS OF CLOSS-IN DETORATIONS

Haj F.C. Eropotachock

Federal Armed Ference for Studies and Exercises, FRG

# Abetreet

Some close-in detenation toots conducted in the PRG are described and methods to deternine the looding encode by blast and fragmentation are mentioned. After establishing the lood the local damage effects are explained theoretically. The problem of determining the blast lood ranged by cased cylindrical charges as well as the quostion of presents waves caused by fragmontation is mentioned. Finally the question of scaling fragmentation effects is concidered,

# 1. Introduction

Late in 1981 and in compor 1982 Federal Armed Ferses Office for Studies and Brareises - Special Infrastructure Tusks Division - did some experimental work someorming upgrading of underroinfered concrete walls of combardoned structures against a gives threat (Bef. 5 and 6). This test serice seems to be a good experimental beso-line for the subject I on going to deal with. Soverer, I am not going to talk about the different upgrading mystems we touted and we finally recommeded. This can be taken from the references given above. But what makes this series so important for us is the fact that we have been forced to identify the damage probabiles against which ve tried to provide protection. Thus, I am going to proceed the tools performed on wells vithest appreding only, totalling & shote out of about 25. 5 of those 6 shots were sealed tests and 4 of the 6 shots were our ducted with a cased wear

One of the etrectures which was tested in shown in Fig. 1. The clear height of the wall was 1.75 m. The percentage of the vertical reinfercement was 0.0856 for walls No. 3 and 4 and 0.176 for valls No. 1 and 2 with a stock quality of 500/350 N/mm<sup>2</sup> and 420/300 N/mm<sup>2</sup> respectively, according to German Standards. The concrete compressive strength was about 250/mm<sup>2</sup> for the other toots.

# 2. Brief Description of the Tosts

Fig. 2 shows a test with 26.6 kg Ch. Weing as equivalent weight feeter of 1.3 the scaled distance use 0.56g/kg 1/3. As it can be seen the wall use breached ever an area of about 1.5 s width and 60 on height. The first spalling layer use about 10 to 12 on thick.

Fig. 3 shows another test with an unescod verpes. In this case 30 kg fiff were used. This results in a seeled distance of C.46m/tg<sup>1/3</sup>. Besides a suchbing creter on the outside and some smaller eracks on the inside so further damage was observed.

Fig. 4 shows a test with a cased weapon. In this case the charge weight was the case as in test No. 2. The difference in result is significant. However, it should be considered that the coming had a square urean section. The wall was breached over an area of about 2.10 s width and 60 on height.

Fig. 5 shows a test similar to test No. 3. However, in this case the easing had a circular eroos section and the explosive consisted of 26.6. kg PETW. Voing an e-variatest weight factor of 1.3 the socied distance was the case as in shot No. 1. The wall was also breached. The reason for not obtaining a clearly localised breach might be that the wall acted like a cantolover because of the fact that the entrance opening was a week point in the lead-bowing system. The spalling layer had a the masse of about 10 cm.

Fig. 6 shows the result of the same test with a smaller veryon. The charge weight was 5.5 kg PETH. With this the scaled distance became about 0.46 m/kg<sup>1/3</sup>. The damage was a limited spall down to a depth of about 15 mm. The spalling layers had a thickness of about 7 cm. The area of damage was about 60 cm wide and 40 cm high.

Fig. 7 shows the result of a full scale test with a HES3. The charge weight was 202 kg Triteral which results is a scaled distance weight 1.0 as equivalent weight fector - of about 0.51 a/kg / . The damage was a limited spall down to a depth of about 10 on within an area of about 2.5 a by 40 cm.

Table 1 gives a suggesty of the test date.
As all tests showed more local effects than
everall reaction I on going to deal with the
local damage only.

### 3. Theerica

# 3.1 Looding of the Wall

A comparison of toots Ho. 2 and Ho. 3 (though with a square sesing) and Ho. 4 proves that the contribution to the total load applied to the well by fragmentation cannot be moglected. Changing one parameter only - 1.0. adding a case - the desage to the well inereages from almost so drange on the Lacide to a total breach of the wall. The aggre fact was also determined in Ref. 2. d chove a summery of the work which was Pig. done for that report and chous a comparison of the exient of decage for eased and waseand charges. Using this graph there is a fairly good agreement with the results. Only the full-meals test (No. 6) and the test value Ch (No. 1) do not catch. Test Ho. 6 should have yielded a breach instead of epalling. However, the deviation is not too drantic. The result of test Me. 1 does not match at all. Ascerding to the graph the rosels should have been spalling only; instead we got a breach. It abould be noted that this graph is etrictly based on toot results and thus :+rcais linications have to be observed. No variation of e.g. comercto quality, persontage of reinfercement, coming thickness etc. in ecuatored. Severer, the tendency of an inereased tesase when having fragmentation in also shows by this graph. Thus, the conclusion is that for further calculations a combined loading caused by black as well as by fragmentation has to be constdered.

# 3.2 Pressure-Time Ristory for a Cylindrical Charge

Due to the lack of reliable data to calculate the processro-time history for cylindrical charges can be to use other procedures. One possibility might be to use the graphs for healgyborical charges - e.g. Ref. ? - which give fairly good recelts. However, as it will be about later on it is important to have a good description of the processro with respect to the time.

in extended research work concerning this topic was perfermed in Germany and is described in Ref. 8. Secover, sees of the conclusions - especially the recommended tables are partially minimaleding. Therefore they have to be revised which will be done within the next couple of souths. In addition to this some work will be done to compare eased and ununsed sylindrical charges.

As there is no further theoretical or experimental work available to my knowledge, one has to rely on these experimental data. Sovery, very little data are available for the vespen/streeture configuration considered in

this paper, i.e. a seeled distance of about 0.5 m/kg<sup>1</sup>/2 (1.0ft,2b<sup>1</sup>/2), The problem of measuring data within this range is that we are still in the region of the fire bull and in addition - if fragmentstion is involved - very heavy decome is to be expected especially to the gages directly expecte the charge on the wall. Because of all those difficulties I am going to use a modified experimental promours-time history meing a free field measurement and multiplying it by the reflection factor reeconomied in Bef. 7. A susmary of all prosours data used for further consideration is given in Fig. 9. Ref. 3 shows that there is almost so difference between an expensatial and a triangular type of pressure distribution if spalling is conserned. Thue, for further saleulations the triangular preserve pulse - as shown in Fig. 9 with dotted lines - is used.

# 3.3 Load by Fragmontation

In addition to the black load the fragmentation contributes a considerable portion to the total load applied to the wall. The most appropriate way available at this time to calculate this load some to be the one described in Ref. 1 which is supposed to be a revised version of the corresponding chapters in Ref. 7. However, some research work is under progross in Germany to investigate the leading caused by fragmentation. But, because it is very difficult to find an abover due to the influence of statistical effects and the question may very well take a long time. Thus, using Ref. 1 we can calculate the general fragmentation parameters like fragmentation distribution,

fragmentation distribution, total number of primary fragments, initial velocity, area of impact assuming a certain angle of propagation.

After that the fragments are grouped according to their weight. For each group we can ealenlate

average fragment weight, impact velocity, arrival time, arrival time, ambor of fragments hitting the area considered, penetration depth, duration of penetration assuming that the fragment in decelorated linearly from its impact velocity at the surface to zero at a calculated penetration depth, pressure applied to the construction assuer

reculting from the powerration.
Sugmarizing all fragmentation groups one gots a prossure-time history econed by fragmentation only.

We have been using a computer program for the procedure described above. So us got a representative procesure-time bistory as about in Fig. 10.

It about be considered that this load to strictly based on theoretical considerations

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and that it represents a statistical everage. However, at the propent time it some to be the meet appropriate way to solve the problem, though it meeds to be verified by 'mperime\_tal work.

# 5.4 Combined Impulse

The combined pressure-time histories for tests No. 4, 5, and 5 are shown in Fig. 11 and give a general view comparing both pressure pul-

Is any sees the blast load sits the atmeture first. Thus, as it will be shown later on the fragments are bitting a possibly weakened structural moster.

It can also be seen that the lead caused by fragmentation is heartly dependent on the standerf distance. Though in all three leats considered in thir chapter the scaled distance - and with this the pock cleat pressure - is the case, the pressure peak as well as the arrival time and the duration of the pressure pulse caused by fragmentation vary considerably. Bef. 4 gives come parameters for scaling the penetration processes. Obviously is this case come of the boundary conditions are violated. Cortainly the shape and weight of the "ragments vary as well as the impact velocity.

Here research work has to be done to investigate the problem of osaling the loading suveed by fragmentation.

# 3.5 Spalling Hochalism

The most common theoretica, solution for calculating spalling effects to described e.g. is Rt. 3. The principles of the calculations are to reflect the pressure were after letting it travel through the etrustant sembert to the free inner surface. The negative of this reflected wave - a tensile wave might be sufficient to produce fractures near the surface. Ref. 3 gives a praphical method of solution as well as an embytical one. For a combined blast-fragmontation impuls it might be more appropriate to way the graphical one.

However, some assumptions have to be made to simplify the calculation. At first, at the free surface normal refrection will be considered only. Second, a change of the duration of the pressure wave will be neglected. Third, a certain attenuation will be considered which in assumed to be about 10% due to material proportion and geometrical confiserations.

To calculate the thickness of the spalling layer as well as the spalling velocity it is necessary to know the tensile strength of the netorial of the structurel member. As the tesm dealt with is this paper were conducted against concrete largets the dynamic tensile strength of concrete has to be determined. This is a difficult problem because of the fact that concrete is a very inhomogeneous material. Though there is a procedure to determine the concrete tensile strength the recalled are at least questionable.

Thus, one commonly assumes a lattic tassile strength of about 10% of the compressive atrength. As shown in Fig. 12 - taken from Ref. 9 - the dynamic compressive strength is dependent on the leading rate. For those tests one has to assume a pressure rise time which will be in the range of about 0.05 more. Thus, based on a peak pressure of about 400 her = 5690 pei the rate of atress is about 100. With this, we are subtied the range given in the graph and and has to extrapolate. The increase of the static tensile atrength will be about 300%. With this the tensile atrength becomes

r = 0.1 + 250 + 3.5 + 87.5kg/em²

for test No. 1 and

e\_ = 0.1 · 500 · 3.5 = 175+p/ea2

for tests He. 2 to 6. However, by calculating the spalling effects one has to observe that the limit velocity of the scarceta is not exceeded. The assumt of this limit velocity is about 15 m/sec. If this value is exceeded the scarcete will be blown out and a breach will be the result.

# 4. Application of the Theory

Accoming a triangular proseure distribution sten ese eveds begeitese as flow est midtle the pressure veve/structure configuration as shows in Fig. 13 e.g. for test No. 4. As can by seen, the damage mechanism counsed by the bleat wave takes place first and after that the preseure wave caused by fragmentation bits a weakened wall. This fact explains the inerease of damage by samed charges. To ealowlate the diseasions of the pressure wave, i.e. expecially the length, a seismic velocity for community of about 3400 m/sec was assumed. With the formulas gives in Rof. 3 one can easily calculate the thickness of the apalling layers as well as their velocities. Because of the fact that the rise time for the presence waves to assumed to be zero the thickness of the different spalling layers is equal and the velocity decreases by a fixed amount for each layer. Table 2 gives a general view of all tosts saluminted. The results agree fairly well with the test results. However, is so case the calculated spalling velocity exceeds the limit relocity as mentioned above. Tais table also shows that scaling of fragmentation effects in very questionable. Though all toots were conducted uning the nest scaled distance the yook load as well as the effect of the fragmentation varied considerably. Is a final step we have several possibilities for calculating the damage process going on ... seek appropriate may in to consider the innide wall reinferement acting as a nonbrems almost like a spall plate. However, one Tain problem is considering a combrace type reaction of the reinforcement in that we have to assume a sufficient cient embedment length. This might be very questionable especially as in the tests denit with in this paper the weapon was placed at the feeting of the well which apparently might be a vesk point in the structural design. Unfortunately the time does not allow to go into more detail concerning this calculation procedure.

Coaclusion and Recommendations

To my knowledge there is at present no better way of theoretically solving the problem of a close distance detonation. However, because this is a very common threat configuration is standard conventional weapone effects design such nese research theoretically and experimentally - should be performed to get a better knowledge in this area. Some work is under way e.g. within the US Air Force supported by the US Army Water-ways Experiment Station and we will have some more tests within the next year in Germany.

However, it should be mentioned that, though the tests described in this paper, produced considerable damage in some cases, we found a very easy-to-construct and sheap method to upgrade the wall by means of berms or concrete slabe. The main objectives of those upgrading mystems is to cut the peak of the blast pressure and prevent the fragments from hitting the wall by seems of an electic and compressible design.

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Test Re	weight of explosive		equivalent weight factor		thickness of casing		ncaled distance	vertical reinforcement	compress.
	kg				-	hap	m/kg <sup>1/3</sup>	1	<b>₽/==</b> 2
1	26.6	O4	1.3	urud	-	-	0.46	0.CR5	25
1	30	THE	1.0	1210004	•		84,0	0.19	×
,	×	TRE	1.0	08744	6	230	5.48	0.17	30
	3.3%	PETE	1.3	*****	6	200	0.46	0.085	<b>3</b> 0
5	5.5	PETH	1,3	ested	5	105	0.46	0.585	90
6	505	Tritonal	1.0	2444	9	360	0.91	0,3 about	<b>X</b> 0

Table 1: Summary of testdate

Test No	C.9.P		time of prival		ansumed duration		thickness of spalling layer		spelling velocity	
	blest	fragmen- tation		fragmen- tation	blest	fragues- tation	blast	fragmen- tation		
	bar	bar	3948	<b>5-80</b> 0		###G	C &	¢#	<b>1/10</b> 0	2/200
1	234	-	0.55	-	0.075	-	4.77		4.39	•
2	-	-	-	-	-		•	-	•	•
,	277	-	C.75		0.175	-	18.78		4,38	•
٠	360	396	0.4	0.8	6.2	0.15	16.53	11,27	6,29	7.12
5	<b>36</b> 0	495	0.25	0.5	0,15	0.13	12.40	7.81	6.29	9.41
6	360	288	6.8	1.4	0.3	0.3	41,32	×.99	6,29	4.63

Table &: Calculation results for spalling effects

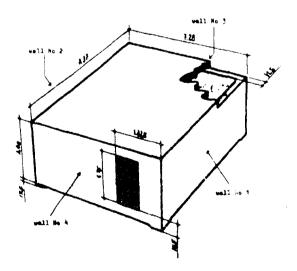


Fig 1:

Example for Modelstructure (seed in Test No 2 to 5)



Fig 2a : Test No1 - outside damage

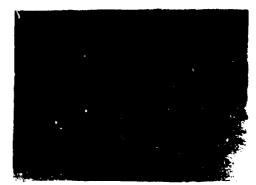


Fig 2b Test No1 - inside damage



Fig 3a - Test No2 - outside damage



Fig 3b - Test No2 - inside damage



Fig.4a: Test No3 - outside damage



Fig 4ti Test No3 - inside damage

Fig. 5a. Test No. 4 - Gutside damage



Fig. St. - Test No4 - inside damage.

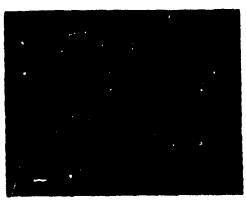


Fig 6a : Test No.5 - outside damage



FigSb Test NoS - inside damage



Fig 7a . Test No6 - outside damage

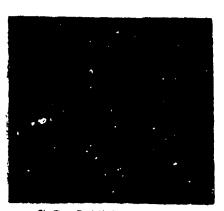
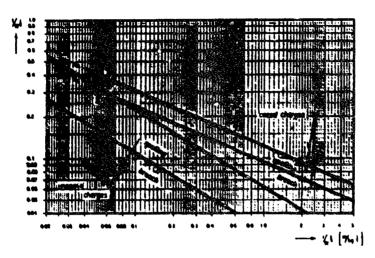


Fig 7b : Test No6 - inside damage



t = well thickness (m) w = charge weight (hg)

Fig 8: Damage Classification (according Ref. 2)

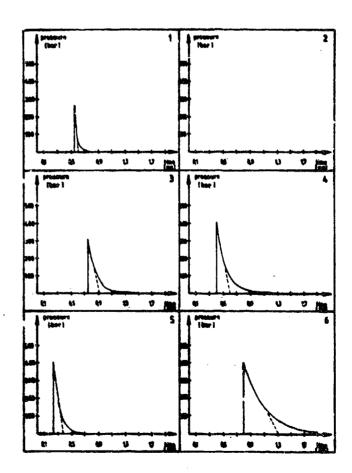


Fig 9: Procours-Time-Histories

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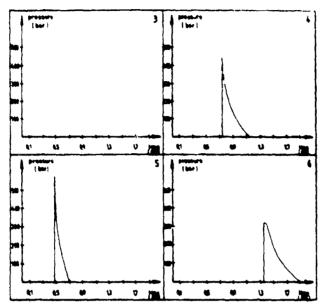


Fig 16: Pressure-Time-Ristories easest by frequentation

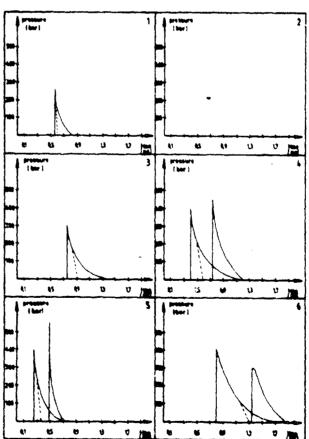


Fig 11: emblace Pressure-Tipe-Historice caused by bloom and framestation

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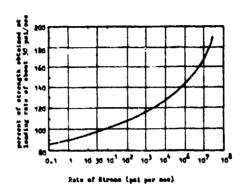
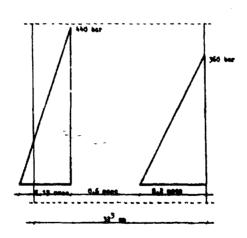


Fig 18: Affect of rate of atreauing on the compressive strongth of ecourate

(takes from Ref 9)



PLe 13:

Presourouse / Structure Configuration (e.g. Tool Bo 4)